

Hence we see that P_1 and P_4 are weakly rooted bisimilar and P_2 and P_5 are weakly rooted bisimilar.

- (d) P_1 and P_2 are not rooted branching bisimilar since the root of P_1 needs to be related to a non-root state of P_2 , but this is disallowed by the root condition.

P_1 and P_3 are not branching bisimilar and hence cannot be rooted branching bisimilar. For this very reason, P_3 cannot be rooted branching bisimilar to any other process.

P_1 and P_4 are rooted branching bisimilar by the same witness presented in part (a). P_4 cannot be rooted branching bisimilar to P_2

P_1 and P_5 are not rooted branching bisimilar as any witness would violate the root condition. P_5 cannot be rooted branching bisimilar to P_4 .

P_2 and P_5 are not rooted branching bisimilar as any witness would violate the root condition as seen in part (b).

Hence, we have that $P_1 =_{RBB} P_4$.

2.

$$\begin{aligned}
& \alpha.(\tau(P + Q) + Q) \\
&= \alpha.((\tau(P + Q) + (P + Q)) + Q) \\
&= \alpha.(((\tau(P + Q) + P) + Q) + Q) \\
&= \alpha.((\tau(P + Q) + P) + (Q + Q)) \\
&= \alpha.((\tau(P + Q) + P) + Q) \\
&= \alpha.(\tau(P + Q) + (P + Q)) \\
&= \alpha.(\tau(P + Q)) \\
&= \alpha.(P + Q)
\end{aligned}$$

Hence we have shown that $\alpha.(\tau(P + Q) + Q) = \alpha.(P + Q)$, which is the axiom B .