

# Recent Improvements to Action Language mA\*

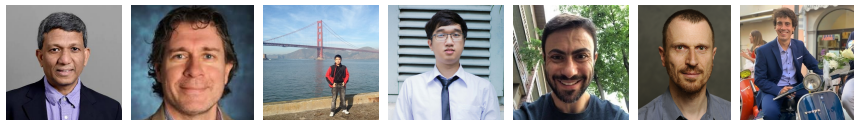
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# Outline

- 1 Background
- 2 Dealing with False Beliefs
- 3 Dealing with Second Order False Beliefs
- 4 Dealing with Untruthful Announcements
- 5 Summary

# Outline

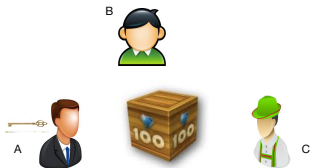
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A **high-level action specification language** for RAC in multi-agent domains that

- allows for the representation of different types of actions which are typically found in multi-agent domains
- allows for the representation of action observability
- has a transition function based semantics

From Baral et al. (2022):

- Nobody knows whether the coin lies heads or tails up;
- The box is locked; needs key to open; only *A* has the key of the box;
- Peeking into an open box will learn whether the coin lies heads or tails up;
- Observing another agent peeking into the box allows the observing agent to know that the action executor knows the status of the coin but does not change his knowledge about the status of the coin;
- Distracting an agent causes the distracted agent to not look at the box;
- Signaling an agent to look at the box causes this agent to look at the box;
- Announcing that the coin lies heads up will make this a common knowledge among the agents that are listening.



A question of interest:

Can *A* know the status of the coin,  
let *B* know that he knows it, and does not allow *C* to be aware of it?

Different types of actions:

- **Ontic action**: opening a box
- **Sensing action**: peeking into the box

Special for multi-agent environment

- **Announcement action**: announcing that the coin lies heads (or tails) up
- **Manipulating observability**: distracting another agents from watching self (or signaling another agents to watch self)
- **Manipulating beliefs**: peeking while other agents are looking

Defined over a set of agents  $\mathcal{A}$  and a set of fluents  $P$ .

Ontic action: opening a box

$open(X)$  **causes**  $opened$  and  
 $open(X)$  **executable**  $has\_key(X)$

Sensing action: peeking into the box

$peek(X)$  **determines**  $tail$  and  
 $peek(X)$  **executable**  $opened, looking(X)$

Announcement action: announcing that the coin lies head (or tail) up

$shout\_tail(X)$  **announces**  $tail$



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How about?

**Manipulating observability:** distracting/signaling another agents from watching self

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How about?

**Manipulating observability:** distracting/signaling another agents from watching self **this is ontic action!**

**Manipulating beliefs:** peeking while other agents are looking **sensing!**

Need: **specification of observability**

## Classification of observability

- **Full observers:** those who observe the action occurrence and fully aware of its effects
- **Partial observers:** those who observe the action occurrence but do not know of its effects
- **Oblivious:** those who are not aware of the action occurrence.

## Possible classification of observability

action type	full observers	partial observers	oblivious
<i>ontic actions</i>	✓		✓
<i>sensing actions</i>	✓	✓	✓
<i>announcement actions</i>	✓	✓	✓

## Three Agents and Coin Box

$X, Y \in \{A, B, C\}, X \neq Y$ :

$X$ <b>observes</b> $open(X)$	$X$ full observer
$X$ <b>observes</b> $peek(X)$	--
$Y$ <b>observes</b> $open(X)$ <b>if</b> $looking(Y)$	--
$Y$ <b>aware_of</b> $peek(X)$ <b>if</b> $looking(Y)$	$Y$ partially observer
$Y$ <b>observes</b> $shout\_tail(X)$	$X$ full observer
$\{X, Y\}$ <b>observes</b> $distract(X, Y)$	$X, Y$ full observer
$\{X, Y\}$ <b>observes</b> $signal(X, Y)$	--

- Epistemic logic language
- Kripke structure and epistemic state
- Satisfaction of formula in Kripke model and epistemic state
- Event model, update model, update template, and the  $\otimes$  operator

$\mathcal{A}$ : set of agents;  $P$ : set of propositions.

Multi-agent epistemic logic language  $L(P, \mathcal{A})$

$$\varphi \stackrel{\text{def}}{=} \top \mid \perp \mid p \mid \neg\varphi \mid \varphi \wedge \psi \mid \mathbf{B}_i\varphi \mid \mathbf{C}_X\varphi$$

where  $p \in P$ ,  $i \in \mathcal{A}$ ,  $X \subseteq \mathcal{A}$ .

$\mathbf{B}_i\varphi$ : “agent  $i$  knows/believes  $\varphi$ ” and

$\mathbf{C}_X\varphi$ : “ $\varphi$  is a common knowledge between the agents in  $X$ ”

Kripke structure

$\mathcal{M} = (W, R, \pi)$ , where (i)  $W$  is the domain, a **finite set of worlds** ( $\mathcal{M}[S]$ );  
 (ii)  $R : \mathcal{A} \rightarrow 2^{W \times W}$  assigns an **accessibility relation**  $R_i$  to each agent  
 $i \in \mathcal{A}$  ( $\mathcal{M}[i]$ ). (iii)  $\pi : P \rightarrow 2^W$ : **valuation of that variable**.

A **pointed Kripke structure** is a pair  $(\mathcal{M}, w)$  where  $\mathcal{M} = (W, R, \pi)$  and  
 $w \in W$ .

Given:  $(\mathcal{M}, w)$  with  $\mathcal{M} = (W, R, \pi)$  and a formula  $\varphi$ ,  $(\mathcal{M}, w) \models \varphi$  is defined as follows:

- $(\mathcal{M}, w) \models \top$  always;
- $(\mathcal{M}, w) \models \perp$  never;
- $(\mathcal{M}, w) \models p$  iff  $w \in \pi(p)$ ;
- $(\mathcal{M}, w) \models \neg\varphi$  iff  $(\mathcal{M}, w) \not\models \varphi$ ;
- $(\mathcal{M}, w) \models \varphi_1 \wedge \varphi_2$  iff  $(\mathcal{M}, w) \models \varphi_1$ ; and  $(\mathcal{M}, w) \models \varphi_2$ ;
- $(\mathcal{M}, w) \models K_i\varphi$  if for all  $v \in W$ , if  $wR_iv$  then  $(\mathcal{M}, v) \models \varphi$ ; and
- $(\mathcal{M}, w) \models C_X\varphi$  if for all  $v \in W$ , if  $w(\bigcup_{j \in X} R_j)^*v$  then  $(\mathcal{M}, v) \models \varphi$

where  $(\bigcup_{j \in X} R_j)^*$  is the transitive closure of  $\bigcup_{j \in X} R_j$ .

$\mathcal{M} \models \varphi$  if  $(\mathcal{M}, w) \models \varphi$  for each  $w \in W$ .

$\mathcal{M} = (S, R, \pi)$ : a Kripke model

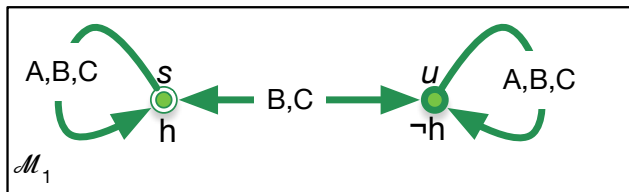
- **K**  $\stackrel{\text{def}}{=} \forall i \in \mathcal{A}, \varphi, \psi \in L(P, \mathcal{A}). [\mathcal{M} \models (K_i\varphi \wedge K_i(\varphi \Rightarrow \psi)) \Rightarrow K_i\psi]$ ;
  - **T**  $\stackrel{\text{def}}{=} \forall i \in \mathcal{A}, \psi \in L(P, \mathcal{A}). [\mathcal{M} \models K_i\psi \Rightarrow \psi]$ ;
  - **4**  $\stackrel{\text{def}}{=} \forall i \in \mathcal{A}, \psi \in L(P, \mathcal{A}). [\mathcal{M} \models K_i\psi \Rightarrow K_iK_i\psi]$ ;
  - **5**  $\stackrel{\text{def}}{=} \forall i \in \mathcal{A}, \psi \in L(P, \mathcal{A}). [\mathcal{M} \models \neg K_i\psi \Rightarrow K_i\neg K_i\psi]$ ; and
  - **D**  $\stackrel{\text{def}}{=} \forall i \in \mathcal{A}, \psi \in L(P, \mathcal{A}). [\mathcal{M} \models \neg K_i \perp]$ .
- 
- $\mathcal{M}$  is **T-** (**4-**, **K-**, **5-**, **D-**, respectively) model if it satisfies property **T** (**4**, **K**, **5**, **D**, respectively).
  - $\mathcal{M}$  is a **S5** model if it satisfies the properties **K**, **T**, **4**, and **5**.
  - $\mathcal{M}$  is a **KD45** model if it satisfies the properties **K**, **D**, **4**, and **5**.



An **epistemic state** is a pair  $(\mathcal{M}, W_d)$  where  $\mathcal{M} = (W, R, \pi)$  is a Kripke structure and  $W_d \subseteq W$ . A truth value of a formula  $\varphi$  with respect to an epistemic state  $(\mathcal{M}, W_d)$  is defined by

$$(\mathcal{M}, W_d) \models \varphi \quad \text{iff} \quad \forall w \in W_d. [(\mathcal{M}, w) \models \varphi]$$

$(\mathcal{M}_1, s)$ : an epistemic state of the three agents and a coin in the box



A knows that  $h$  (assuming that  $s$  is the true state)

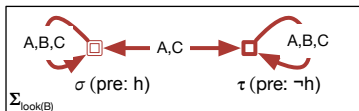
B and C do not know whether  $h$

An **update model** for  $L(P, \mathcal{A})$  is a quadruple  $\mathcal{E} = (E, Q, pre, sub)$  where:

- $E$  is a finite non-empty set of events;
- $Q : \mathcal{A} \rightarrow 2^{E \times E}$  assigns an **accessibility relation** to each agent  $i \in \mathcal{A}$ ;
- $pre : E \rightarrow L(P, \mathcal{A})$  assigns to each event a precondition; and
- $sub : E \rightarrow SUB(P, \mathcal{A})$  assigns to each event a **substitution** where each substitution is a set  $\{p \leftarrow \varphi \mid p \in P\}$ .

A pair  $(\mathcal{E}, E_d)$  consisting of an update model  $\mathcal{E} = (E, Q, pre, sub)$  and a non-empty set of designated events  $E_d \subseteq E$  is called an **epistemic action**.

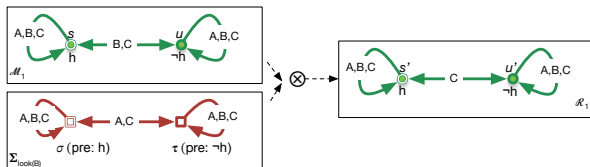
### Graphical Representation of an Epistemic Action



Given an epistemic action  $(\mathcal{E}, E_d)$  and an epistemic state  $(\mathcal{M}, W_d)$

- $(\mathcal{E}, E_d)$  is **executable** in  $(\mathcal{M}, W_d)$  if for each  $w \in W_d$  there exists at least one  $e \in E_d$  such that  $(\mathcal{M}, w) \models \text{pre}(e)$ .
- $(\mathcal{M}, W_d) \otimes (\mathcal{E}, E_d) = ((W', R', \pi'), W'_d)$  where
  - $W' = \{(w, e) \in W \times E \mid (\mathcal{M}, w) \models \text{pre}(e)\}$
  - $R'_i = \{((w, e), (v, f)) \in W' \times W' \mid wR_i v \text{ and } eQ_i f\}$
  - $\pi'(w, e)(p) = \top$  iff  $(\mathcal{M}, w) \models \text{sub}(e)(p)$
  - $W'_d = \{(w, e) \in W' \mid w \in W_d \text{ and } e \in E_d\}$
 if  $(\mathcal{E}, E_d)$  is *executable* in  $(\mathcal{M}, W_d)$ .

Example: Everyone watches while  $B$  is looking at the coin



$$s' = (s, \sigma) \text{ and } u' = (u, \tau)$$

## Domain

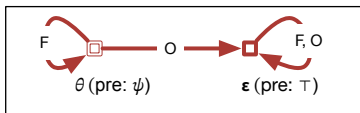
A set of statements about action effects and observability over the pair  $(P, \mathcal{A})$  is a **multi-agent domain**.

A multi-agent domain specifies a collection of epistemic actions defined as follows. Given a Kripke model  $(\mathcal{M}, s)$  and an action occurrence  $a$ ,

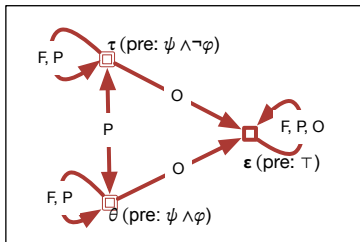
**Frame of reference**  $\rho = (F, P, O)$

- $F$  - the set of agents who are fully observer of the occurrence.  
 $F = \{i \mid i \text{ **observes** } a \text{ if } \varphi, (\mathcal{M}, s) \models \varphi\}$
- $P$  - the set of agents who are partially observer of the occurrence.  
 $P = \{i \mid i \text{ **aware_of** } a \text{ if } \varphi, (\mathcal{M}, s) \models \varphi\}$
- $O$  - the set of agents who are oblivious of the occurrence.  
 $O = \mathcal{A} \setminus (F \cup P)$

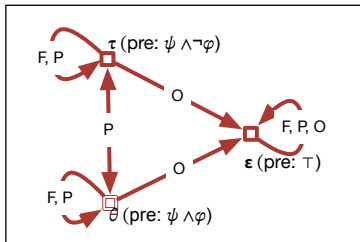
$(\mathcal{M}, s)$ ,  $a$  with executability condition  $\psi$ , frame of reference  $\rho = (F, P, O)$



$a$  causes  $\ell$



$a$  determines  $\varphi$



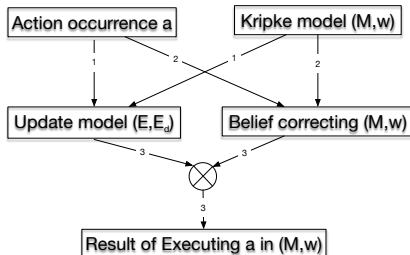
$a$  announces  $\varphi$

Automatically generated from the domain specification and  $(\mathcal{M}, s)$

Given a domain  $D$ , an action  $a$ , and a pointed Kripke model  $(M, s)$ ,  $\Phi_D$  defines a set of pointed Kripke models  $\Phi_D(a, (M, s))$  in three steps:

- Compute the update template  $(E, E_d)$  of the action occurrence  $a$  in  $(M, s)$
- Correct false beliefs of full observers of  $a$ : this creates a new pointed Kripke model  $(M', s')$
- Let  $\Phi_D(a, (M, s)) = (M', s') \otimes (E, E_d)$

## Illustration



## Dealing with False Beliefs

For a pointed Kripke model  $(M, s)$ , an agent  $i \in \mathcal{AG}$ , and a formula  $\varphi$ , we say that  $i$  has false belief about  $\varphi$  in  $(M, s)$  if

$$(M, s) \models \varphi \text{ and } (M, s) \models \mathbf{B}_i \neg \varphi.$$

For a set of agents  $S$ , a pointed Kripke model  $(M, s)$ , and a formula  $\varphi$ , such that  $(M, s) \models \varphi$ , let  $M[S, \varphi]$  be obtained from  $M$  by replacing  $M[i]$  with  $M[S, \varphi][i]$  where

- $M[S, \varphi][i] = (M[i] \setminus M[i]^S) \cup \{(s, s)\}$  for  $i \in S$  and  $(M, s) \models \mathbf{B}_i \neg \varphi$  where  $M[i]^S = \{(s, u) \mid (s, u) \in M[i]\}$ ; and
- $M[S, \varphi][i] = M[i]$  for other agents, i.e.,  $i \in \mathcal{AG} \setminus S$  or  $i \in S$  and  $(M, s) \not\models \mathbf{B}_i \neg \varphi$ .

- If  $a$  is not executable in  $(M, s)$  then  $\Phi_D(a, (M, s)) = \emptyset$
- If  $a$  is executable in  $(M, s)$  and  $(\mathcal{E}, E_d)$  is the representation of the occurrence of  $a$  in  $(M, s)$  then
  - $\Phi_D(a, (M, s)) = (M, s) \otimes (\mathcal{E}, E_d)$  if  $a$  is a ontic action instance;
  - $\Phi_D(a, (M, s)) = M_1[F_D(a, M_1, s), \varphi] \otimes (\mathcal{E}, E_d)$  where  $M_1 = M[P_D(a, M, s), \psi]$  if  $a$  is a sensing action instance that senses  $\varphi$  and  $(M, s) \models \varphi$ ;
  - $\Phi_D(a, (M, s)) = M_1[F_D(a, M_1, s), \neg\varphi] \otimes (\mathcal{E}, E_d)$  where  $M_1 = M[P_D(a, M, s), \psi]$  if  $a$  is a sensing action instance that senses  $\varphi$  and  $(M, s) \models \neg\varphi$ ; and
  - $\Phi_D(a, (M, s)) = M_1[F_D(a, M_1, s), \varphi] \otimes (\mathcal{E}, E_d)$  where  $M_1 = M[P_D(a, M, s), \psi]$  if  $a$  is an announcement action instance that announces  $\varphi$  and  $(M, s) \models \varphi$ .

Finally, for a set of pointed Kripke models  $\mathcal{M}$ ,

- if  $a$  is not executable in some  $(M, s) \in \mathcal{M}$  then  $\Phi_D(a, \mathcal{M}) = \emptyset$ ;
- if  $a$  is executable in every  $(M, s) \in \mathcal{M}$  then

$$\Phi_D(a, \mathcal{M}) = \bigcup_{(M, s) \in \mathcal{M}} \Phi_D(a, (M, s)).$$



# Properties of $\Phi_D$

Given the occurrence of an action

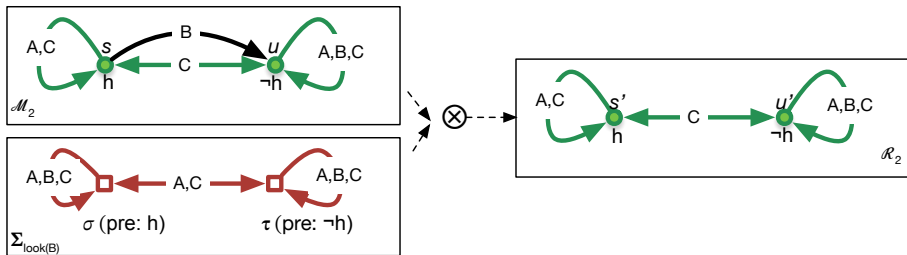
- **full observers** of the action occurrence know the true values of fluents that are affected (or determined) by the action occurrence;
- **partial observers** of the action occurrence do not know the true values of fluents but know that full observers know; and
- beliefs of **oblivious agents** do not change.

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This problem is not unique to  $m\mathcal{A}^*$ . It is a problem for all approaches using the product update model operator  $\otimes$ .

## Product Update ( $\otimes$ ) Sensitive to False Beliefs



$B$  looks at the coin and **becomes ignorant** — **undesirable**

Why is it undesirable for an agent to become ignorant?

- **Counter intuitive**: if an agent executes a sensing action then it should learn the true value of the sensed formula **and correct its false belief** instead of becoming ignorant!
- False belief is a nature part of multi-agent domain:
- Loss of **KD45** property because loss of **seriality**, which implies
  - reasoning about both knowledge and beliefs of agents is **impossible** if only one modality (belief) is used, i.e., **both** modalities are needed for reasoning about knowledge and beliefs of agents
  - it is desirable to reason about both knowledge and beliefs

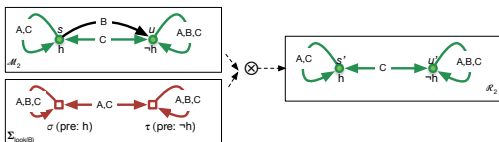
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  - it is desirable to reason about both knowledge and beliefs

**First Improvement**: new product update operator

- allow agents to correct false beliefs by executing actions
- maintains **KD45** property of a **KD45** state if the update model is also **KD45**

**Original**  $\otimes$ : If an agent  $a$  has a false belief about  $f$  then sensing  $f$  makes  $a$  ignorant.



Assume that  $s$  is the true state in  $\mathcal{M}_2$  ( $\mathbf{B}_B \neg h$ ,  $\mathbf{B}_A h$ ,  $\neg(\mathbf{B}_C h \wedge \mathbf{B}_C \neg h)$ , ...)  
 $B$  has false belief about  $h$

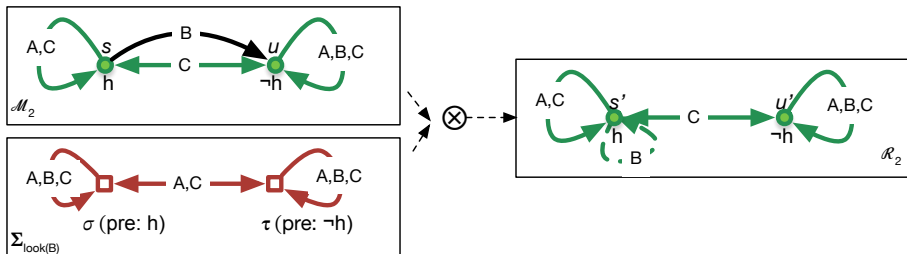
**Event:**  $look(B)$  "A, C watch while  $B$  executes the action *senses*  $h$ "

**Expectation:**  $\mathbf{B}_B h$ ,  $\mathbf{B}_A h$ ,  $\neg(\mathbf{B}_C h \wedge \mathbf{B}_C \neg h)$ ,  $\mathbf{B}_C(\mathbf{B}_B h \vee \mathbf{B}_B \neg h)$ ,

$\Sigma_{look(B)}$  is the update model for the **event**  $look(B)$

$$\mathcal{R}_2 = (\mathcal{M}_2, s) \otimes \Sigma_{look(B)}$$

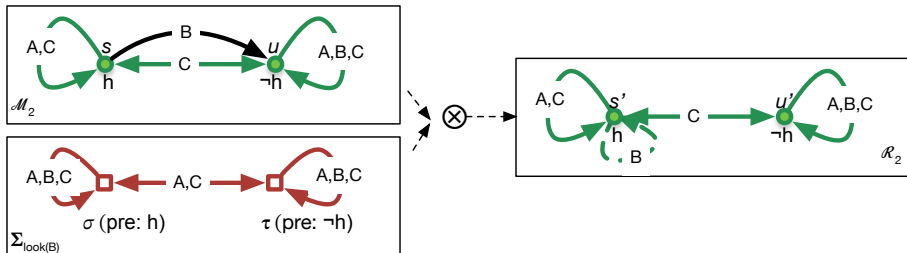
- $B$  becomes ignorant in  $\mathcal{R}_2$  **because** the link labeled  $B$  from  $s$  to  $u$  is not transferred to  $\mathcal{R}_2$  (because  $\otimes$ )  
**this is rightly so!**
- $B$  did not learn the value of  $h$ !  
**there should be a loop labeled  $B$  at  $s' = (s, \sigma)$  —  $\otimes$  never adds links**



## Change # 1

if  $(x, \sigma)$  is a new world and  $(\sigma, \sigma) \in R_i$  and  
 for every  $u$  such that  $(x, u) \in \mathcal{M}[i]$  there exists no  $\tau \in \Sigma$  such that  
 $(\sigma, \tau) \in R_i$  and  $(\mathcal{M}, u) \models \text{pre}(\tau)$

then  $((x, \sigma), (x, \sigma)) \in \mathcal{M}'[i]$



## Change # 1

if  $(x, \sigma)$  is a new world and  $(\sigma, \sigma) \in R_i$  ( $i$  considers that  $\sigma$  is possible) and for every  $u$  such that  $(x, u) \in \mathcal{M}[i]$  there exists no  $\tau \in \Sigma$  such that  $(\sigma, \tau) \in R_i$  and  $(\mathcal{M}, u) \models \text{pre}(\tau)$

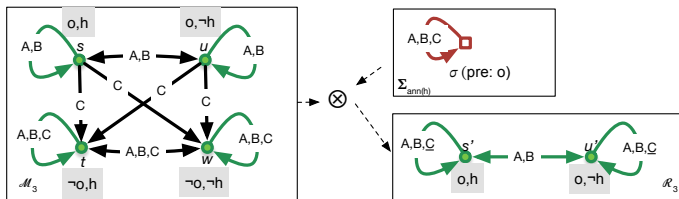
(no other event is compatible to  $\sigma$  at world  $x$ )

then  $((x, \sigma), (x, \sigma)) \in \mathcal{M}'[i]$

(for  $i$ ,  $x$  must be the true world if  $\sigma$  occurs)



**Change #1** helps but also introduces undesirable accessibility.



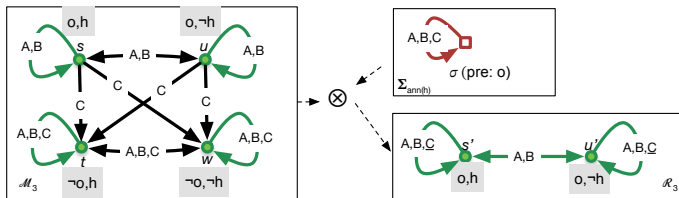
$\mathcal{M}_3$  and  $s$  is the true state of the world ( $\neg(\mathbf{B}_C h \vee \mathbf{B}_C \neg h)$ ,  $\mathbf{B}_C \neg o$ )  
 $A$  announces  $o$  —  $C$  miraculously knows  $h$  (with **Change #1**)

**Reason:** **Change #1** introduces loop labeled  $C$  around  $s' = (s, \sigma)$  and  $u' = (u, \sigma)$

$s$  and  $u$  are **connected** through un-directional links labeled  $C$

This connection must be maintained somehow.

**Change #1** helps but also introduces undesirable accessibility.



$\mathcal{M}_3$  and  $s$  is the true state of the world ( $\neg(\mathbf{B}_C h \vee \mathbf{B}_C \neg h)$ ,  $\mathbf{B}_C \neg o$ )  
 $A$  announces  $o$  —  $C$  miraculously knows  $h$  (with **Change #1**)

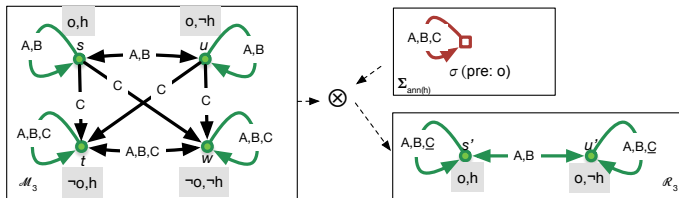
**Reason: Change #1** introduces loop labeled  $C$  around  $s' = (s, \sigma)$  and  $u' = (u, \sigma)$

$s$  and  $u$  are **connected** through un-directional links labeled  $C$

This connection must be maintained somehow.

**maintaining  $\neg(\mathbf{B}_C h \vee \mathbf{B}_C \neg h)$  requires links labeled between  $s'$  and  $u'$**

**Change #1** helps but also introduces undesirable accessibility.



$\mathcal{M}_3$  and  $s$  is the true state of the world ( $\neg(\mathbf{B}_C h \vee \mathbf{B}_C \neg h)$ ,  $\mathbf{B}_C \neg o$ )  
 A announces  $o$  —  $C$  miraculously knows  $h$  (with **Change #1**)

**Reason: Change #1** introduces loop labeled  $C$  around  $s'$  and  $u'$

**Change #2:** Assume  $\mathcal{M}' = \mathcal{M} \otimes \Sigma$

if  $x' = (x, \sigma)$  and  $y' = (y, \tau)$  are new worlds and  
 $(x', x')$  and  $(y', y')$  in  $\mathcal{M}'$  because of **Change #1**,  
 $(x, y) \notin \mathcal{M}[i]$ ,  $(y, x) \notin \mathcal{M}[i]$ , and  $x$  and  $y$  are **connected** by  $i$   
 then  $((x, \sigma), (y, \tau)) \in \mathcal{M}'[i]$ .

Kripke structure:  $\mathcal{M}$

Update model:  $\Sigma = \langle \Sigma, R_1, \dots, R_n, pre, sub \rangle$

$$\mathcal{M}' = \mathcal{M} \otimes \Sigma$$

- (i)  $\mathcal{M}'[S] = \{(s, \tau) \mid s \in \mathcal{M}[S], \tau \in \Sigma, (\mathcal{M}, s) \models pre(\tau)\}$ ;
- (ii) For  $(s, \tau)$  and  $(s', \tau')$  in  $\mathcal{M}'[S]$ ,  $((s, \tau), (s', \tau')) \in \mathcal{M}'[i]$  iff
  - (a)  $(s, s') \in \mathbf{B}_i$  and  $(\tau, \tau') \in R_i$ ; or
  - (b)  $(s, \tau) = (s', \tau')$ ,  $(\tau, \tau) \in R_i$ , and  $\mathbf{C}_i(s, \tau)$  is true;
  - (c)  $(s, \tau) \neq (s', \tau')$ ,  $\mathbf{C}_i(s, \tau)$  and  $\mathbf{C}_i(s', \tau')$  are true,  $(\tau, \tau), (\tau, \tau'), (\tau', \tau') \in R_i$ ,  $(s, s'), (s', s) \notin \mathcal{M}[i]$ , and  $s$  and  $s'$  are connected by  $i$ .
- (iii) For all  $(s, \tau) \in \mathcal{M}'[S]$  and  $f \in F$ ,  $\mathcal{M}'[\pi]((s, \tau)) \models f$  if  $f \rightarrow \varphi \in sub(\tau)$  and  $(\mathcal{M}, s) \models \varphi$ .

$\mathbf{C}_i(x, \tau)$  encodes “for every  $u$  such that  $(x, u) \in \mathcal{M}[i]$  there exists no  $\tau' \in \Sigma$  such that  $(\tau, \tau') \in R_i$  and  $(\mathcal{M}, u) \models pre(\tau')$ .”

For update models defined by the action language  $m\mathcal{A}^*$ , pointed Kripke structure  $(\mathcal{M}, s)$ , if  $i$  is a full observer of an action  $a$ ,

$$(\mathcal{M}', s') = (\mathcal{M}, s) \otimes \Sigma_a,$$

- $a$  is a sensing action ( $a$  **determines**  $\varphi$ ),  $(\mathcal{M}, s) \models \varphi$ , and  $(\mathcal{M}, s) \models \mathbf{B}_i \neg \varphi$  then  $(\mathcal{M}', s') \models \mathbf{B}_i \varphi$
- $a$  is an announcement action ( $a$  **announces**  $\varphi$ ),  $(\mathcal{M}, s) \models \varphi$ , and  $(\mathcal{M}, s) \models \mathbf{B}_i \neg \varphi$  then  $(\mathcal{M}', s') \models \mathbf{B}_i \varphi$
- $a$  is an ontic action with precondition  $\psi$ ,  $(\mathcal{M}, s) \models \psi$ , and  $(\mathcal{M}, s) \models \mathbf{B}_i \neg \psi$  then  $(\mathcal{M}', s') \models \mathbf{B}_i \psi$

New - Thanks to Michael and Mehdi for asking the difficult question!

For a full observer  $i$ , and a sensing/announcement action  $a$  such that

$$(\mathcal{M}, s) \models \varphi \wedge \mathbf{B}_i \neg \varphi$$

then for every fluent formula  $\varphi'$ ,

$$\text{if } (\mathcal{M}', s') \models \mathbf{B}_i \varphi' \text{ then } (\mathcal{M}', s') \models \varphi'$$

$$\text{if } (\mathcal{M}, s) \models \neg \varphi' \wedge \mathbf{B}_i \varphi' \text{ then } (\mathcal{M}', s') \not\models \mathbf{B}_i \varphi'$$

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$$\text{if } (\mathcal{M}', s') \models \mathbf{B}_i \varphi' \text{ then } (\mathcal{M}', s') \models \varphi'$$

**New belief is not false!**

$$\text{if } (\mathcal{M}, s) \models \neg \varphi' \wedge \mathbf{B}_i \varphi' \text{ then } (\mathcal{M}', s') \not\models \mathbf{B}_i \varphi'$$

**False belief is removed!**

New - Thanks to Michael and Mehdi for asking the difficult question!

For a full observer  $i$ , and a sensing/announcement action  $a$  such that

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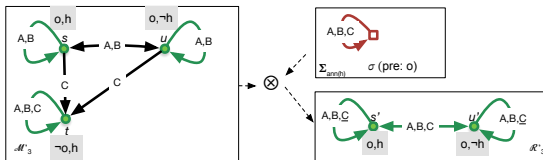
$$\text{if } (\mathcal{M}', s') \models \mathbf{B}_i \varphi' \text{ then } (\mathcal{M}', s') \models \varphi'$$

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False belief is removed!

It is not all good yet!  $(\mathcal{M}'_3, s) \models \mathbf{B}_{C,h}$  but  $(\mathcal{R}'_3, s') \not\models \mathbf{B}_{C,h}$



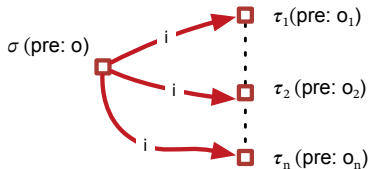
It seems that Change #2 must be applied more discretely!



Let  $\Sigma = \langle \Sigma, R_1, \dots, R_n, pre, sub \rangle$  be a **KD45** update model an update model.  $\Sigma$  is said to be **KD45 well-defined with respect to  $i$**  if for every  $\sigma \in \Sigma$ :

- $(\sigma, \sigma) \in R_i$ ; or
- $S_\sigma = \{pre(\tau) \mid (\sigma, \tau) \in R_i\}$  is **complete**

**complete** = for any possible world  $s$  and interpretation  $\pi$  over  $\mathcal{P}$ , there exists some  $\varphi \in S_\sigma$  such that  $\pi[s] \models \varphi$



**Intuition:** if  $\sigma$  is not an event for  $i$  then at any possible world, at least one of  $\tau_1, \dots, \tau_n$  is compatible with  $\sigma$  for  $i$

Let  $\Sigma = \langle \Sigma, R_1, \dots, R_n, pre, sub \rangle$  be a **KD45** update model an update model.  $\Sigma$  is said to be **KD45 well-defined with respect to  $i$**  if for every  $\sigma \in \Sigma$ :

- $(\sigma, \sigma) \in R_i$ ; or
- $S_\sigma = \{pre(\tau) \mid (\sigma, \tau) \in R_i\}$  is **complete**

$\Sigma$  is **well-defined** if it is well-defined with respect to all agents  $1, \dots, n$ .

- If  $\mathcal{M}$  is **KD45** Kripke structure and  $\Sigma$  is **KD45** well-defined then  $\mathcal{M} \otimes^{new} \Sigma$  is **KD45**
- all update models defined for the action language  $m\mathcal{A}^*$  are **KD45** well-defined

- Majority of work on dealing with false beliefs rely on belief revision, not aware of one that deals with update models
- Correcting false beliefs in the presence of update models:  $m\mathcal{A}^*$  paper by Baral et al. (2022) employs an ad-hoc method to correct false beliefs prior to the execution of an action  
This approach suffers from the problem that leads to **Change #2**

- Herzig et al. (2005): only ontic and sensing actions, assumes that actions are always executable  
can be verified that this paper only considers well-defined update models
- Son et al. (2015): primitive update models as sufficient condition for maintaining **KD45** property, update model of ontic action in  $m\mathcal{A}^*$  is not primitive  
can be verified that primitive update models are well-defined
- Aucher (2008): semantical condition on the initial Kripke structure that guarantees that the result of its update by a serial update model is serial  
our condition is applied on the update model
- Baltag and Renne (2016): the language of serial Public Announcement Logic (sPAL) that maintains the **KD45** of Kripke models after the execution of a truthful public announcement  
sPAL does not employ update models and requires that no agent has false belief about the announced formula before the action is executed

## Conclusions

Introducing a new product update operator  $\otimes$  that

- allows an agent to correct its false beliefs after the execution of an action
- maintains **KD45** property of a **KD45** state if the update model is also **KD45**

# Outline

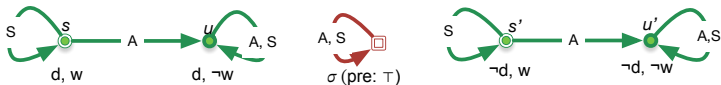
- 1 Background
- 2 Dealing with False Beliefs
- 3 Dealing with Second Order False Beliefs**
- 4 Dealing with Untruthful Announcements
- 5 Summary

Sally and Anne are in a room containing a box and a basket. Sally places a marble in a basket and leaves the room, but secretly watches the room without Anne knowing. Anne then takes the marble from the basket and places it in a box.

When Sally returns, a child is asked “where does Anne expect her to look for the marble?”

Because Sally observed Anne moving the marble, we know that Sally knows that the marble is in the box.

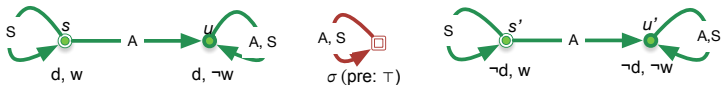
$mA^*$  outcome:



Sally and Anne are in a room containing a box and a basket. Sally places a marble in a basket and leaves the room, but secretly watches the room without Anne knowing. Anne then takes the marble from the basket and places it in a box.

When Sally returns, a child is asked “where does Anne expect her to look for the marble?” **in the basket is the correct answer!**  $B_{Anne}B_{Sally}d$   
 Because Sally observed Anne moving the marble, we know that Sally knows that the marble is in the box.

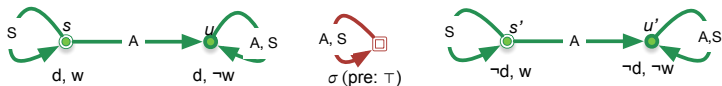
$mA^*$  outcome:  $B_{Anne}B_{Sally}\neg d$





Correct answer:  $\mathbf{B}_{Anne} \mathbf{B}_{Sally} d$

$m\mathcal{A}^*$  outcome:  $\mathbf{B}_{Anne} \mathbf{B}_{Sally} \neg d$



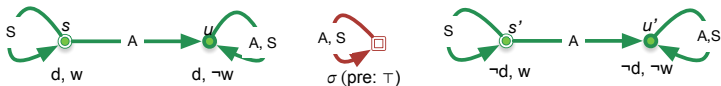
Sally **observes** Anne's action ( $\neg d$ ) **if** Sally is watching ( $w$ )

Reasons:

- Observability is globally computed in  $m\mathcal{A}^*$
- Observability **should be considered locally**

Correct answer:  $\mathbf{B}_{Anne} \mathbf{B}_{Sally} d$

$m\mathcal{A}^*$  outcome:  $\mathbf{B}_{Anne} \mathbf{B}_{Sally} \neg d$

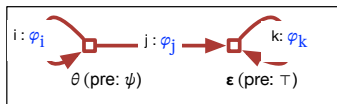
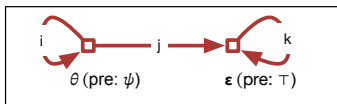


Sally **observes** Anne's action ( $\neg d$ ) **if** Sally is watching ( $w$ )

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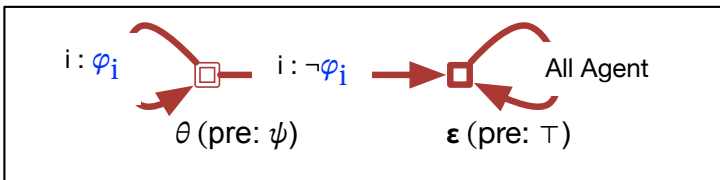
- Observability is globally computed in  $m\mathcal{A}^*$   
Both agents are full observers at  $s$  (**correct**) and this is common knowledge (**incorrect**)
- Observability **should be considered locally**  
To Anne, Sally is oblivious at  $u$ .

## Proposed by Bolander (2018)



- Introduction of a condition for accessibility relation between two events  $(\sigma, i: \varphi_i, \sigma')$  (e.g.,  $(\theta, i: \varphi_i, \theta)$ )
- **Change in construction of  $\mathcal{M}' = \mathcal{M} \otimes \Sigma$**   
 $((u, \sigma), (v, \sigma')) \in \mathcal{M}'[i]$  if  $(u, v) \in \mathcal{M}[i]$ ,  $(\sigma, i: \varphi_i, \sigma')$ ,  
**and**  $(\mathcal{M}, u) \models \varphi_i$

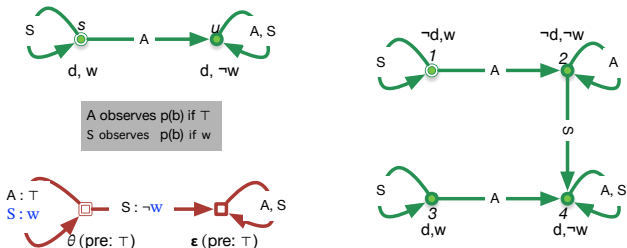
## Ontic Actions



$\varphi_i$  is the condition for  $i$  to be fully observer of the action

- accessibility relations in the resulting state are dynamically generated

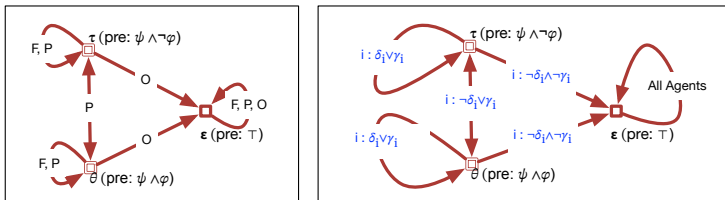
Reference. *Pham et al. (2022a)*



$p(b)$  **causes**  $\neg d$  ( $p(b)$  Anne put the marble in the box)

- $1 = (s, \theta)$ ,  $2 = (u, \theta)$ ,  $3 = (s, \epsilon)$ ,  $4 = (u, \epsilon)$
- $(1, 1) \in \mathcal{M}'[S]$ :  $(s, s) \in \mathcal{M}[S]$ ,  $(\theta, w : S, \theta)$ ,  $(\mathcal{M}, s) \models w$
- $(2, 2) \notin \mathcal{M}'[S]$ :  $(u, u) \in \mathcal{M}[S]$ ,  $(\theta, w : S, \theta)$ , **but**  $(\mathcal{M}, u) \not\models w$
- $(2, 4) \in \mathcal{M}'[S]$ :  $(u, u) \in \mathcal{M}[S]$ ,  $(\theta, \neg w : S, \epsilon)$ , **and**  $(\mathcal{M}, u) \models \neg w$
- $(1, 1) \notin \mathcal{M}'[A]$ :  $(s, s) \notin \mathcal{M}[A]$ ,
- ...

**Sensing action:** sensed formula  $\varphi$ , executability condition  $\psi$



(left: original  $m\mathcal{A}^*$ , right:  $m\mathcal{A}^*$  with edge-conditioned update model)

**(Truthful) announcement:** same structure, only differs in the designated events (only  $\theta$ )

Let  $\mathcal{T}$  be a  $m\mathcal{A}^*$  action domain,  $a$  an action, and  $\langle M, s \rangle$  a state. Assume that **(a)**  $a$  is executable in  $\langle M, s \rangle$  and  $\langle M', s' \rangle$  is the result of the execution of  $a$  in  $\langle M, s \rangle$  **(b)**  $i, j$  are full observers **(c)**  $i$  believes that  $j$  is oblivious. Then,  $i$  will have a second order false belief about  $j$  belief's about the effects of the action, e.g.,

- ① if  $a$  is an ontic action that makes  $l$  true and  $\langle M, s \rangle \models \mathbf{B}_i \mathbf{B}_j \neg l$  then  $\langle M', s' \rangle \models \mathbf{B}_i l \wedge \mathbf{B}_j l \wedge \mathbf{B}_i \mathbf{B}_j \neg l$ ;
- ② if  $a$  is a sensing action that senses  $\varphi$ ,  $\langle M, s \rangle \models \varphi^*$  ( $\varphi^* \in \{\varphi, \neg\varphi\}$ )  $\langle M, s \rangle \models \mathbf{B}_i \mathbf{B}_j \neg \varphi^*$  then  $\langle M', s' \rangle \models \mathbf{B}_i \varphi^* \wedge \mathbf{B}_j \varphi^* \wedge \mathbf{B}_i \mathbf{B}_j \neg \varphi^*$
- ③ similar for announcement actions

## Second approach: **employing the original update models**

When an ontic action occurs in  $(\mathcal{M}, s)$

- $\theta$ : the event for full observers
- $\epsilon$ : the event for oblivious agents

They are created based **on the evaluation of observability statements at  $s$**



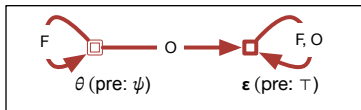
## Second approach: employing the original update models

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Generic update model for ontic action:



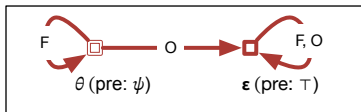
## Second approach: employing the original update models

When an ontic action occurs in  $(\mathcal{M}, s)$

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Generic update model for ontic action:



Similar events can be created for agents at different worlds:  $\theta_u, \theta_v, \epsilon_u, \epsilon_v,$

...

- How to characterize  $\theta_u$ ? What are the events of the update model?
- How should they connect to each other?

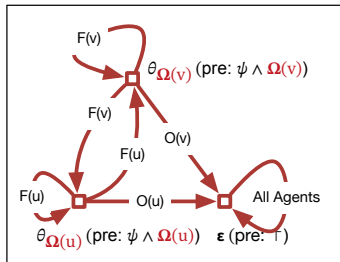
For a Kripke structure  $\mathcal{M}$  and a world  $u \in \mathcal{M}[S]$ , the frame of reference  $(F(u), P(u), O(u))$  can be characterized by

$$\begin{aligned} \Omega(u) &= \Omega(F(u), P(u), O(u)) = \\ &\left( \bigwedge_{i \in F(u)} \bigvee_{[i \text{ observes } a \text{ if } \varphi] \in D} \varphi \right) \wedge \left( \bigwedge_{i \in P(u)} \bigvee_{[i \text{ aware\_of } a \text{ if } \varphi] \in D} \varphi \right) \wedge \\ &\left( \bigwedge_{i \in O(u)} \bigvee_{[i \text{ observes } a \text{ if } \varphi] \in D \cup [i \text{ observes } a \text{ if } \neg\varphi] \in D} \varphi \right) \end{aligned}$$

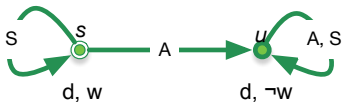
## Ontic Actions

Events are  $\{\theta_{\Omega(u)} \mid u \in \mathcal{M}[S]\} \cup \{\epsilon\}$

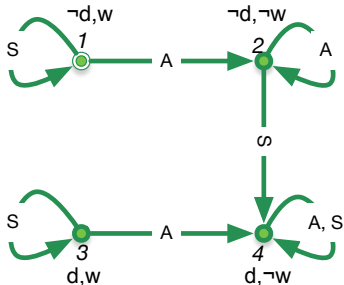
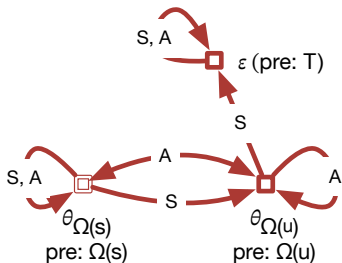
- $\theta_{\Omega(u)}$  and  $\theta_{\Omega(v)}$  should be connected by full observers
- $\theta_{\Omega(u)}$  and  $\epsilon_{\Omega(u)}$  should be connected by oblivious agents
- $\epsilon$  represents  $\epsilon_{\Omega(u)}$  for every  $u$



Update model with 2 worlds  $u$  and  $v$



$F(s) = \{S, A\}$  and  $O(s) = \{\}$   
 $F(u) = \{A\}$  and  $O(u) = \{A\}$

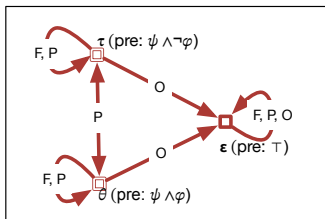
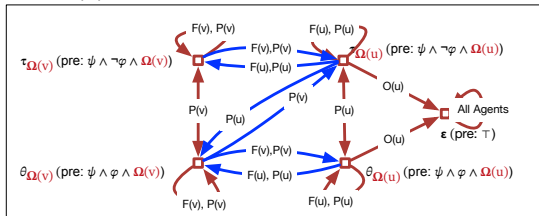


$1 = (s, \theta_{\Omega(s)})$ ,  $2 = (u, \theta_{\Omega(u)})$ ,  
 $3 = (s, \epsilon)$ , and  $4 = (u, \epsilon)$ .

$B_{Anne} \neg d$  and  $B_{Sally} \neg d$

$B_{Anne} B_{Sally} d$ ,  $B_{Sally} B_{Anne} B_{Sally} d$

## Sensing Actions (Announcement actions: similar)

Events:  $\{\theta_{\Omega(u)} \mid u \in \mathcal{M}[S]\} \cup \{\tau_{\Omega(u)} \mid u \in \mathcal{M}[S]\} \cup \{\epsilon\}$  $mA^*$ 

with local observability

Part of the update model for sensing action with 2 worlds  $u$  and  $v$  (Missing links between  $\tau_{\Omega(v)}$  and  $\theta_{\Omega(u)}$  and links from  $\tau_{\Omega(v)}$  and  $\theta_{\Omega(v)}$  to  $\epsilon$ )

Let  $\mathcal{T}$  be a  $m\mathcal{A}^*$  action domain,  $a$  an action, and  $\langle M, s \rangle$  a state. Assume that (a)  $a$  is executable in  $\langle M, s \rangle$  and  $\langle M', s' \rangle$  is the result of the execution of  $a$  in  $\langle M, s \rangle$  (b)  $i, j$  are full observers (c)  $i$  believes that  $j$  is oblivious. Then,  $i$  will have a second order false belief about  $j$  belief's about the effects of the action, e.g.,

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- ② if  $a$  is a sensing action that senses  $\varphi$ ,  $\langle M, s \rangle \models \varphi^*$  ( $\varphi^* \in \{\varphi, \neg\varphi\}$ )  $\langle M, s \rangle \models \mathbf{B}_i \mathbf{B}_j \neg \varphi^*$  then  $\langle M', s' \rangle \models \mathbf{B}_i \varphi^* \wedge \mathbf{B}_j \varphi^* \wedge \mathbf{B}_i \mathbf{B}_j \neg \varphi^*$   
 $\langle M, s \rangle \models \mathbf{B}_i (\neg(\mathbf{B}_j \varphi^* \vee \mathbf{B}_j \neg \varphi^*))$  then  
 $\langle M', s' \rangle \models \mathbf{B}_i \varphi^* \wedge \mathbf{B}_j \varphi^* \wedge \mathbf{B}_i (\neg(\mathbf{B}_j \varphi^* \vee \mathbf{B}_j \neg \varphi^*))$  for  $\varphi^* \in \{\varphi, \neg\varphi\}$   
 (not sure if this is correct for edge-conditioned update models)
- ③ similar for announcement actions

## Edge-conditioned vs. Local observability

- Edge-conditioned: number of events **smaller** (2 vs. many more, entailment checking is not required when creating the model)
- Local observability: computing the result is **simpler** (entailment checking is not required when computing the result)

Bolander (2018): two criteria for formalism based to deal with the second order false-belief tasks

- **Robustness**: applicable for generic theories  
( $m\mathcal{A}^*$  theories are sufficiently generic)
- **Faithfulness**, easy to understand (faithfulness).  
(models can be automatically generated from  $m\mathcal{A}^*$  theories)

Context: multi-agent epistemic planning or action languages

- Engesser et al. (2024): *repetition-free epistemic-doxastic* (REDA), for reasoning about actions with knowledge and belief focuses on formulas of modal depth at most two (REDA<sup>≤2</sup>) belief and knowledge operators assumes that the belief operator is serial, transitive, and euclidean maintains **KD45** property
- Buckingham et al. (2020): knowledge and belief operator, maintains **KD45** property
- Rajaratnam and Thielscher (2021): DER for representing and reasoning with event models for epistemic planning expressiveness of update models cannot deal with second order false beliefs
- Pham et al. (2022a): discussed in previous slide



# Outline

- 1 Background
- 2 Dealing with False Beliefs
- 3 Dealing with Second Order False Beliefs
- 4 Dealing with Untruthful Announcements**
- 5 Summary

## $m\mathcal{A}^*$ and many other work: only truthful announcements

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### The different facets of untruthful announcements

In the literature, often associated with

- **Lying:** Son tells everyone that he is a billionaire (everyone has a good laugh and nobody believes him!)
- **Misleading:** Son tells everyone that he is not attending (or attending) IJCAI-24 even though he is unsure whether he will be attending it (some might believe, some might not believe him!)

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The act of Son saying that he is a billionaire or telling everyone that he is attending IJCAI-24 is just **an announcement action**. Syntactically, it can be specified

Son **announces** Son-is-a-Billionaire

**Claim:** human makes untruthful announcements pretty often :-)

So, understanding when and why such an announcement is made is

- **interesting:** this will help us to understand the nature of untruthful announcements (besides being a difficult academic exercise!)
- **necessary:** if we were to build a computer system that works with human, it is necessary for the system to understand the intention of the human and react accordingly

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Syntactically, the act of Son saying that he is a billionaire can be specified by the  $m\mathcal{A}^*$  statement

Son **announces** Son-is-a-Billionaire

What is its update model?

When  $\varphi$  is announced, how does an agent behave if this is an untruthful announcement?

- **unaware of the announcement**: oblivious, nothing happens to this group of agents
- **full observer**
  - the agent can derive that the announcer(s) is untruthful
  - the agent happens to believe that  $\neg\varphi$
  - the agent does not believe whether  $\varphi$  nor does it believe whether  $\neg\varphi$
- **partial observer** - does not know what is announced but is aware that there are interactions among full observers

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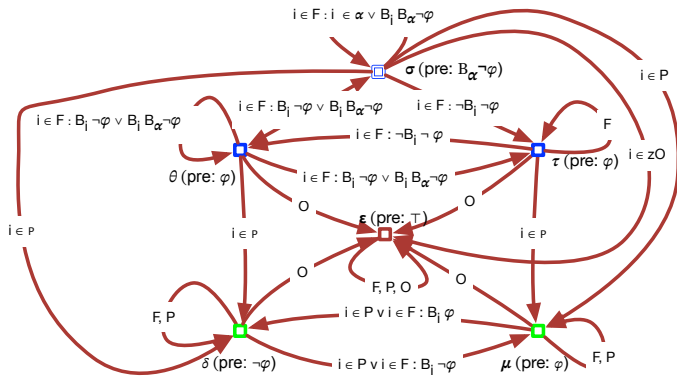
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**Several possibilities for each scenario!**

- (**A1: agents are opinionated**) if an agent is certain about the truth of a formula, even if it is incorrect in the actual world, or if she realizes that the announcement is untruthful (i.e. she knows that the announcers make a false statement) then she will not change her belief about the formula, regardless of what the announcers say;
- (**A2: agents are eager to remove their uncertainties**) if an agent is uncertain about the truth of a formula and cannot reason that the announcers are untruthful then she will believe what the announcers say.

An announcement  $a$  by  $\alpha$  of  $\varphi$  is made in  $(\mathcal{M}, s)$

- $i$  is a full observer
  - ①  $(M, s) \models \mathbf{B}_i \mathbf{B}_\alpha \neg \varphi$ :  
 $i$  realizes that it is a lie so  $i$  will not change its belief about  $\varphi$
  - ②  $(M, s) \models \mathbf{B}_i \neg \varphi$  or  $(M, s) \models \mathbf{B}_i \varphi$ :  
by **(A1)**, the belief of  $i$  should not be changed;
  - ③  $(M, s) \models \neg(\mathbf{B}_i \varphi \vee \mathbf{B}_i \neg \varphi) \wedge \neg \mathbf{B}_i \mathbf{B}_\alpha \neg \varphi$ :  
by **(A2)**, the belief of  $i$  about  $\varphi$  should be changed and  $\mathbf{B}_i \varphi$  is true after the announcement.
- $i$  is a partial observer  
 $i$  is unaware of the (truth value of the) announced formula  
 $i$ 's belief about  $\varphi$  does not change  
 $i$ 's belief about fully observers changes
- $i$  is not aware of the execution of action  $a$ : nothing changes for  $i$ .



$\Sigma_a$  - update model for lying about  $\varphi$  in  $(M, s)$

- $\sigma, \theta, \tau$ : events for full observers
- $\alpha$  or  $B_i B_\alpha \neg \varphi$ : no belief change
- $\delta, \mu$ : partial observers
- $\epsilon$ : oblivious agents

**$a$  announces  $\varphi$**

$a$  occurs in  $(M, s)$  with  $(M, s) \models \mathbf{B}_\alpha \neg\varphi$

Assume that  $(M', s') = (M, s) \otimes \Sigma_a$

- ①  $(M', s') \models \mathbf{C}_{F_t} \neg\varphi$  where  $F_t = \{i \in F \mid (M, s) \models \mathbf{B}_i \neg\varphi\}$ ;
- ②  $(M', s') \models \mathbf{C}_{F_{uf}} \varphi$  where  $F_{uf} = \{i \in F \mid (M, s) \models \neg \mathbf{B}_i \neg\varphi\}$ ;
- ③  $(M', s') \models \mathbf{C}_P(\mathbf{C}_{F_u} \varphi \vee \mathbf{C}_{F_u} \neg\varphi)$  where  
 $F_u = \{i \in F \mid (M, s) \models \neg(\mathbf{B}_i \varphi \vee \mathbf{B}_i \neg\varphi)\}$ ;
- ④  $(M', s') \models \mathbf{C}_F(\mathbf{C}_P(\mathbf{C}_{F_u} \varphi \vee \mathbf{C}_{F_u} \neg\varphi))$ ;
- ⑤  $(M', s') \models \mathbf{B}_j \eta$  iff  $(M, s) \models \mathbf{B}_j \eta$  for a formula  $\eta$  and  $j \in O$ ; and
- ⑥  $(M', s') \models \mathbf{B}_i \mathbf{B}_j \eta$  iff  $(M, s) \models \mathbf{B}_i \mathbf{B}_j \eta$  for a formula  $\eta$ ,  $i \in F \cup P$  and  $j \in O$ .

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- preliminary implementation in an epistemic planner Pham et al. (2023)
  - update models for misleading announcements Pham et al. (2022b)
  - This results might need to be revisited with local observability

# Outline

- 1 Background
- 2 Dealing with False Beliefs
- 3 Dealing with Second Order False Beliefs
- 4 Dealing with Untruthful Announcements
- 5 Summary

# Summary

$m\mathcal{A}^*$  with

- false beliefs
- second order false beliefs
- untruthful announcements
- **not in this talk**: other extensions such as non-deterministic actions, uncertainty in observability, etc.



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