Chapter 1

A Header

theory Demo = Main:

1.1 A Section

1.1.1 A subsection

A subsubsection

Here some text with some antiquotations:

'a list, x # xs, x # xs = y # ys, any text

$$\llbracket P \ []; \land a \ list. \ P \ list \Longrightarrow P \ (a \ \# \ list) \rrbracket \Longrightarrow P \ list$$

Keywords are printed bold, rest is just copied verbatim into the document:

lemma a = a

- not a difficult proof
- note that the double quotes do not appear in the ouptput

proof -

but we could still want to have a longer text in here and do LATEX tricks:

• show a = a by force

qed

end

Chapter 2

More On Locales

```
locale agroup = group +

assumes com: x \cdot y = y \cdot x
```

We are now in the agroup context where assumption com: $x \cdot y = y \cdot x$ is visible without any further premises.

All inherited and proved theorems of the *group* context are available as well:

```
x \cdot y \cdot z = x \cdot (y \cdot z)

\mathbf{1} \cdot x = x

x^{-} \cdot x = \mathbf{1}

x \cdot \mathbf{1} = x

x \cdot x^{-} = \mathbf{1}

etc.
```

Outside the context, these theorems would look like this. (for fun we replace \implies by \longrightarrow in LaTeX).

```
agroup prod one inv \longrightarrow prod x y = prod y x semi prod \longrightarrow prod (prod x y) z = prod x (prod y z) group prod one inv \longrightarrow prod one x = x group prod one inv \longrightarrow prod (inv x) x = one group prod one inv \longrightarrow prod x one = x group prod one inv \longrightarrow prod x (inv x) = one
```

Changing existing output syntax:

```
syntax (latex output)
Cons :: 'a \Rightarrow 'a \ list \Rightarrow 'a \ list \ (-\cdot/- [66,65] \ 65)
```

Now existing function definitios look different:

$$\begin{array}{l} map \ f \ [] = [] \\ map \ f \ (x \cdot xs) = f \ x \cdot map \ f \ xs \end{array}$$

Creating new symbols and changing output syntax:

$$\begin{array}{ll} \mathbf{syntax} \ (\mathit{latex}) \\ \mathit{notEx} & :: ('a => \mathit{bool}) => \mathit{bool} \ (\mathbf{binder} \ \neg \exists \ \mathit{10}) \\ \mathbf{translations} \\ \neg \exists x. \ P == \neg (\exists \ x. \ P) \end{array}$$

lemma
$$(\forall x. \neg P x) = (\neg \exists x. P x)$$
 by blast