

# ENGG1811 Computing for Engineers

## **Week 5B:**

**Numpy: motivation, arrays, indexing, slicing, axes. Nested for loop.**

**Numpy functions: statistical, Boolean, logic, reshape, where**

# Motivating example

- The manager of a frozen food company approaches you with the following problem:
  - The company has installed 1,000 thermometers to monitor the temperature in its warehouses
  - They have collected 100,000 data points from each thermometer
  - The manager wants to know:
    - Has the temperature in any thermometer ever exceeded a threshold?
    - Which thermometers had readings exceeded the given threshold? How often did it happen?
    - Which thermometer had the highest average temperature?
- Typical modern day data processing problems:
  - Many sequences; each sequence has many data points

# Illustrative example: the data

- We assume:
  - There are 5 thermometers
  - Each thermometer has 10 temperature readings
- We store the data in a list of lists
  - The variable temp\_list (see below) is a list of 5 lists
  - Each entry of temp\_list is a list with 10 elements
- In general, you store
  - A data sequence in a list,
  - Multiple data sequences in a list of lists

```
temp_list = [[ 0.3, 0.4, 0.5, 0.5, 0.1, 0.8, 0.8, 0.5, 0.0, 0.7],  
             [ 0.2, 0.4, 0.8, 0.4, 0.8, 1.8, 0.9, 0.1, 1.4, 1.7],  
             [ 1.1, 0.1, 0.8, 0.9, 0.5, 0.3, 0.2, 0.2, 1.1, 0.4],  
             [ 0.4, 0.7, 0.6, 0.6, 0.4, 0.4, 0.5, 0.0, 0.1, 0.2],  
             [ 0.2, 0.1, 0.9, 0.9, 0.3, 0.5, 0.4, 0.7, 0.2, 0.7]]
```

Thermometer 0

Thermometer 2

# Illustrative example: the question

- Assuming that the threshold = 1
- For each thermometer, how many times have the readings exceeded the threshold?

```
temp_list = [[ 0.3, 0.4, 0.5, 0.5, 0.1, 0.8, 0.8, 0.5, 0.0, 0.7],  
             [ 0.2, 0.4, 0.8, 0.4, 0.8, 1.8, 0.9, 0.1, 1.4, 1.7],  
             [ 1.1, 0.1, 0.8, 0.9, 0.5, 0.3, 0.2, 0.2, 1.1, 0.4],  
             [ 0.4, 0.7, 0.6, 0.6, 0.4, 0.4, 0.5, 0.0, 0.1, 0.2],  
             [ 0.2, 0.1, 0.9, 0.9, 0.3, 0.5, 0.4, 0.7, 0.2, 0.7]]
```

# Two different solutions

- Classical programming solution
  - Nested for-loops
- Python numpy library
  - Num is short for numerical

# Nested for-loops

- A nested for-loop means a for-loop within a for-loop
  - You have seen nested if's before
- Example problem:
  - See illustration on the next slide for making a nested for-loop
  - Code in nested\_for\_prelim.py

```
temp_list = [[ 0.3, 0.4, 0.5, 0.5, 0.1, 0.8, 0.8, 0.5, 0.0, 0.7],  
             [ 0.2, 0.4, 0.8, 0.4, 0.8, 1.8, 0.9, 0.1, 1.4, 1.7],  
             [ 1.1, 0.1, 0.8, 0.9, 0.5, 0.3, 0.2, 0.2, 1.1, 0.4],  
             [ 0.4, 0.7, 0.6, 0.6, 0.4, 0.4, 0.5, 0.0, 0.1, 0.2],  
             [ 0.2, 0.1, 0.9, 0.9, 0.3, 0.5, 0.4, 0.7, 0.2, 0.7]]
```

threshold = 1

Expected answer = [0, 3, 2, 0, 0]

# Nested for-loops

For each thermometer

For a thermometer: # times the readings > threshold

← This task is a for-loop  
↓

For each reading in thermometer

Increment count if reading > threshold

Combine the code to get nested for-loop:

For each thermometer

For each reading in thermometer

Increment count if reading > threshold

# Nested-for loop code

Code in  
nested\_for\_prelim.py

```
# %% Development step 2:  
# Use a list within temp_list to col  
# exceeded  
thermometer_readings = temp_list[2]
```

```
count = 0    # number of times that  
for temp in thermometer_readings:  
    if temp > threshold:  
        count += 1
```

```
# %% Development step 3:  
count_exceeding = []
```

```
for thermometer_readings in temp_list:
```

```
    count = 0  
    for temp in thermometer_readings:  
        if temp > threshold:  
            count += 1
```

```
    count_exceeding.append(count)
```



# Why numpy?

- numpy has a lot of functions that can save you time in writing code
- If we want to solve the same problem of determining the number of readings in a thermometer exceeding a threshold in numpy, the code is in count\_exceed.py
- Line 35 uses the array of temperature and threshold to compute the answer that you want. You may not understand how to use numpy yet but we'd like you to appreciate that you can get the work done with merely 1 line of code

```
26 import numpy as np
27
28 # set the threshold
29 threshold = 1
30
31 # convert the list to an numpy array
32 temp_array = np.array(temp_list)
33
34 # count the number of data points exceeding the threshold per thermometer
35 count_exceeding = np.sum(temp_array > threshold, axis = 1)
```

# The numpy library

- The numpy library is a collection of functions which are very useful for data analysis, efficient computation
- Very often, a numpy function can replace many lines of code. Less lines of code means:
  - Shorter development time
  - less debugging
- You combine numpy functions with your coding skills to solve bigger problems
- Why don't we teach you numpy from the beginning?
  - The same reason why we don't give calculators to the primary school children

# numpy basic concepts

- Basic concepts:
  - Creation, slicing, assignments
  - Shape and indexing
  - Axes

# numpy arrays: creation, slicing, assignment

- Basic techniques
  - There are many ways to create numpy **arrays**
    - One way is to enter the arrays directly or convert them from a list
  - Accessing and modifying elements, slicing
    - Information on indexing 2-d arrays are on the next slide
- Code in `numpy_elements.py`

## 2-D array: shape and indexing

```
# a 2-dimensional array and
array2 = np.array([ [-1.2,  2, -3.1,  4.5],
                    [  4, -5,  3.5,  7.1],
                    [ 2.7,  9,  1.7,  3.4]])

# You can access individual elements
array2[0,3] # 4.5
array2[1,2] # 3.5
```

- The indexing for 2-D array is **similar to matrices** except the indices begin with zero
- We say the shape of this array is (3,4). If it were a matrix, you'd say a 3-by-4 matrix.

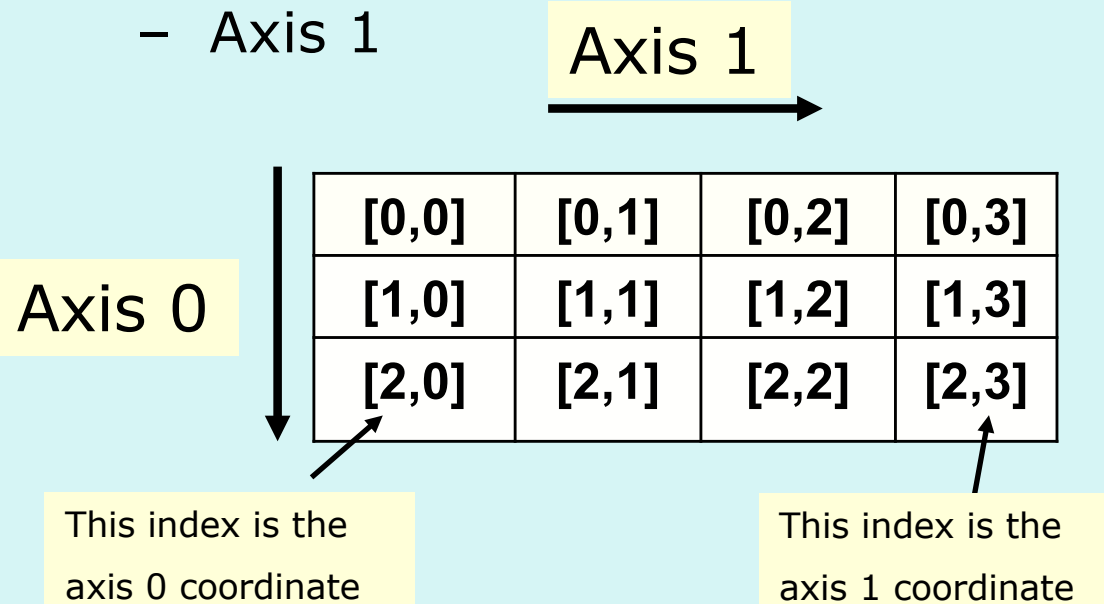
↓

Indices

|       |       |       |       |
|-------|-------|-------|-------|
| [0,0] | [0,1] | [0,2] | [0,3] |
| [1,0] | [1,1] | [1,2] | [1,3] |
| [2,0] | [2,1] | [2,2] | [2,3] |

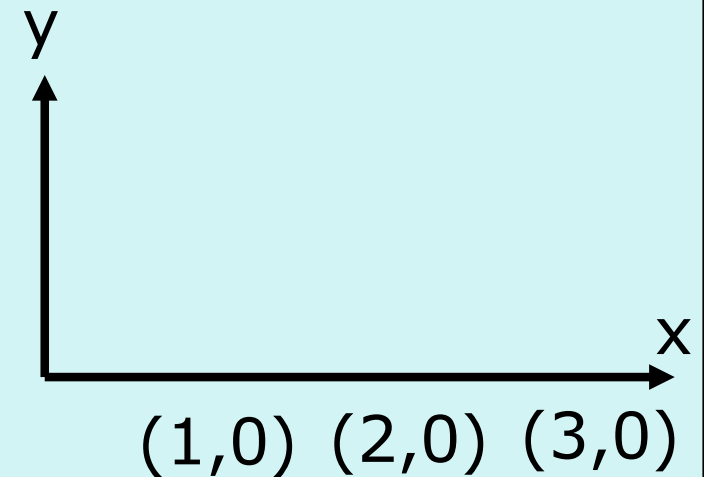
# Array axes

- A 2-D numpy array has 2-axes
  - Axis 0
  - Axis 1



- Along Axis 0, only Axis 0 coordinates change
- Mnemonic: *Downright*

## Cartesian co-ordinates



Along or parallel to x-axis, only the x-coordinates change

Rotate the x-y plane clockwise by  $90^\circ$

# Recap: numpy (1)

- Creating arrays, indexing, slicing, shape

```
# %% import numpy
import numpy as np
```

Column index

0      1      2      3

```
# Creating a 2-dimensional array and
array2 = np.array([ [-1.2,  2, -3.1,  4.5],
                    [  4, -5,  3.5,  7.1],
                    [ 2.7,  9,  1.7,  3.4]])
```

Row index

← 0

← 1

← 2

```
# Indexing, slicing, shape
array2[0,3] # 4.5
array2[1,:] # array([ 4. , -5. ,  3.5,  7.1])
array2.shape # (3, 4)
```

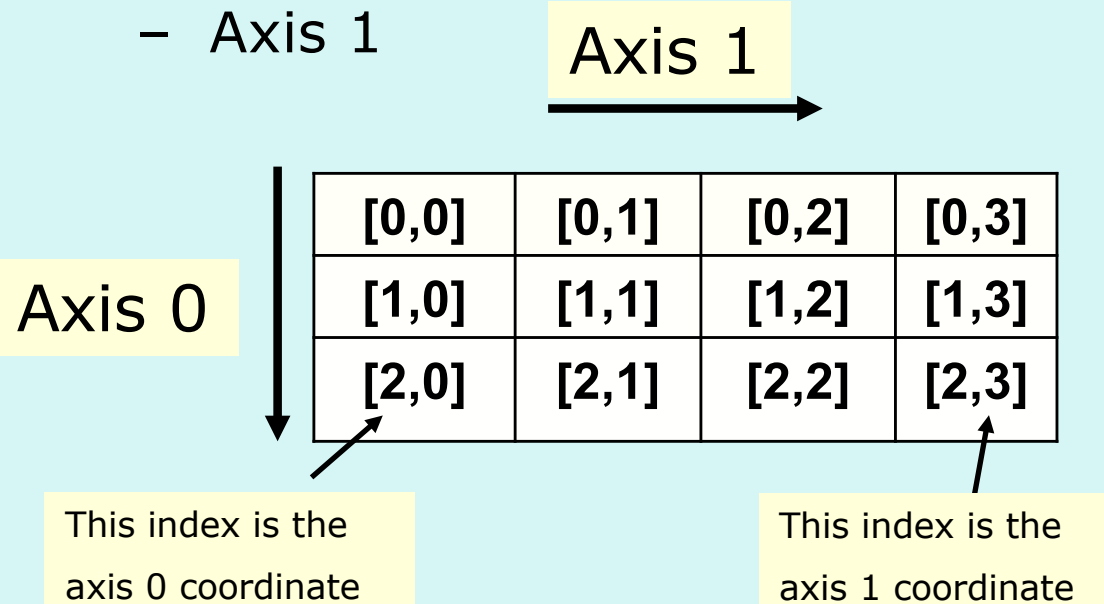


Indices

|       |       |       |       |
|-------|-------|-------|-------|
| [0,0] | [0,1] | [0,2] | [0,3] |
| [1,0] | [1,1] | [1,2] | [1,3] |
| [2,0] | [2,1] | [2,2] | [2,3] |

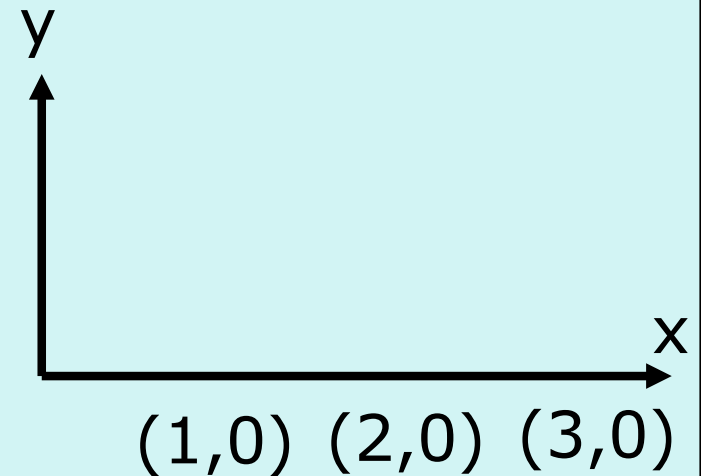
# Array axes (Recap)

- A 2-D numpy array has 2-axes
  - Axis 0
  - Axis 1



- Along Axis 0, only Axis 0 coordinates change
- Mnemonic: *Downright*

Cartesian co-ordinates



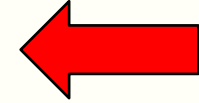
Along or parallel to x-axis, only the x-coordinates change

Rotate the x-y plane clockwise by  $90^\circ$



# numpy topics

- Functions for basic computation & statistics
- Boolean
- diff, dtype
- reshape(), ravel(), where()



# numpy: basic computation and statistics

- Need to prepend with numpy. or the short form that you use
- These functions can be applied to the whole array, or a particular axis

| numpy function      | What it does                          |
|---------------------|---------------------------------------|
| sum()               | sum                                   |
| mean(), median()    | Mean, median                          |
| average()           | Weighted average                      |
| std()               | Standard deviation                    |
| max(), min()        | Maximum, minimum                      |
| argmax(), argsort() | Argument that maximises / minimises   |
| cumsum(), cumprod() | Cumulative sum and cumulative product |
| sort(), argsort()   | sort                                  |

# numpy.sum() function

- File is numpy\_sum.py

- array1 is:

```
[ [-3.2,  0,  0.5,  5.8],  
  [  6, -4,  6.2,  7.1],  
  [ 3.8,  5,  2.7,  3.7]]
```

```
[ 3.1  15.3  15.2]
```

```
[ 6.6  1.  9.4 16.6]
```

```
17 print(np.sum(array1)) # default parameter value  
18                             # sum all values in the array  
19  
20 print(np.sum(array1, axis = 0)) # along axis 0  
21  
22 print(np.sum(array1, axis = 1)) # along axis 1
```

## Exercise: `max()`, `argmax()`

- Go through the file `numpy_max.py`
- See whether you can figure out what `max()` and `argmax()` do
- Hint: `argmax()` has something to do with where the maximum is located
- Note: `arg` is short for argument

## max() and argmax()

```
ay( [ [-3.2, 0, 6.2, 5.8],  
      [ 6, -4, 0.5, 7.1],  
      [ 3.8, 5, 2.7, 3.7] ] )
```

Row index

← 0

← 1

← 2

```
In [7]: np.max(array1, axis = 0)
```

```
Out[7]: array([6. , 5. , 6.2, 7.1])
```

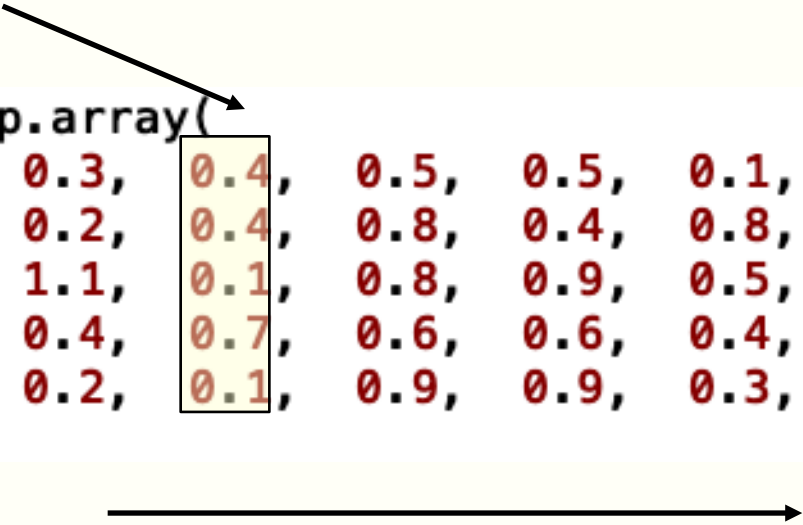
```
In [8]: np.argmax(array1, axis = 0)
```

```
Out[8]: array([1, 2, 0, 1])
```

# Exercise

- The file is numpy\_max\_prelim.py
- Temperature readings are stored in temp\_array
  - Each row corresponds to a thermometer, labelled as 0,1,....,4
  - Each thermometer has 10 readings
- Your tasks
  - Find the maximum temperature in each thermometer
  - Determine which thermometer has the highest temperature at this time?

temp\_array = np.array(  
[[ 0.3, 0.4, 0.5, 0.5, 0.1, 0.8, 0.8, 0.5, 0.0, 0.7],  
[ 0.2, 0.4, 0.8, 0.4, 0.8, 1.8, 0.9, 0.1, 1.4, 1.7],  
[ 1.1, 0.1, 0.8, 0.9, 0.5, 0.3, 0.2, 0.2, 1.1, 0.4],  
[ 0.4, 0.7, 0.6, 0.6, 0.4, 0.4, 0.5, 0.0, 0.1, 0.2],  
[ 0.2, 0.1, 0.9, 0.9, 0.3, 0.5, 0.4, 0.7, 0.2, 0.7]]  
)

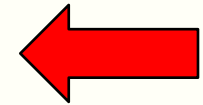


# Some commonly used functions

| <b>numpy function</b> | <b>What it does</b>                   |
|-----------------------|---------------------------------------|
| sum()                 | sum                                   |
| mean(), median()      | Mean, median                          |
| average()             | Weighted average                      |
| std()                 | Standard deviation                    |
| max(), min()          | Maximum, minimum                      |
| argmax(), argsort()   | Argument that maximises / minimises   |
| cumsum(), cumprod()   | Cumulative sum and cumulative product |
| sort(), argsort()     | sort                                  |

# numpy topics

- Functions for basic computation & statistics
- Boolean
- diff, dtype
- reshape(), ravel(), where()





# Boolean numpy arrays

- You can do **elementwise** comparison using `==`, `!=`, `>`, `<`, `>=`, `<=`
  - Try it out in `numpy_boolean_1.py`
  - The result is a numpy arrays of Boolean type

```
array1 = np.array([ [-3.2,  0,  0.5,  5.8],  
                   [  6, -4,  6.2,  7.1],  
                   [ 3.8,  5,  2.7,  3.7]])
```

```
In [8]: array1_cp0 = array1 > 2
```

```
In [9]: array1_cp0
```

```
Out[9]:
```

```
array([[False, False, False,  True],  
       [ True, False,  True,  True],  
       [ True,  True,  True,  True]])
```

# Counting the number of True's

- You can use `numpy.sum()` to count the number of True's
  - `numpy_boolean_1.py`
- At the beginning of the last lecture, we mentioned the problem of determining the number of readings in a thermometer exceeding a threshold
  - The code is in `count_exceed.py`

```
26 import numpy as np
27
28 # set the threshold
29 threshold = 1
30
31 # convert the list to an numpy array
32 temp_array = np.array(temp_list)
33
34 # count the number of data points exceeding the threshold per thermometer
35 count_exceeding = np.sum(temp_array > threshold, axis = 1)
```

# Boolean operators

- There are three numpy Boolean operators:
  - `numpy.logical_and()`
  - `numpy.logical_or()`
  - `numpy.logical_not()`
- Example (see next slide for a fuller explanation) and a quiz in `numpy_boolean_2_prelim.py`
- Forum exercise:
  - You know how to count the number of True's. How do you count the number of False's?

# Illustrating elementwise and

```
array1 = np.array([ [ 3.2, 0.5, 5.8],  
                   [ 6, -1.2, 7.1]])
```

```
array1_la = np.logical_and(array1 > 3, array1 < 7)
```

□ array1 > 3

□ array1 < 7

□ array([[ True, False, True],  
 [ True, False, True]])

□ array([[ True, True, True],  
 [ True, True, False]])

logical\_and()

(= apply logical and to corresponding elements in the 2 arrays)

□ array1\_la

array([[ True, False, True],  
 [ True, False, False]])

# Some useful logic functions

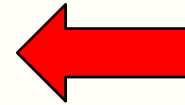
- The full list of logic functions are at:
  - <https://docs.scipy.org/doc/numpy-1.17.0/reference/routines.logic.html>

| numpy function                                   | What it does                                       |
|--|--|
| <code>all()</code>                               | True if all elements along an axis is True         |
| <code>any()</code>                               | True if at least one element along an axis is True |
| <code>allclose()</code> , <code>isclose()</code> | Are elements in two arrays within a tolerance?     |
| <code>array_equal()</code>                       | Same shape and equal elements for two arrays       |

Example and quiz are in `numpy_logic_prelim.py`

# numpy topics

- Functions for basic computation & statistics
- Boolean
- diff, dtype
- reshape(), ravel(), where()



# numpy.diff()

- The code is in numpy\_diff.py

```
np.array([ [-3,  0,  0,  5],  
          [ 6, -4,  6,  7],  
          [ 3,  5,  2,  3]])
```

Along axis 1

→

```
[[ 3  0  5]  
 [-10 10 1]  
 [ 2 -3 1]]
```

Along axis 0

↓

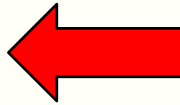
```
[[ 9 -4  6  2]  
 [-3  9 -4 -4]]
```

# dtype

- **All** the elements in a numpy array must have the same dtype. Possible dtype's are:
  - float
  - int
  - bool
- We will explore the implication of this in the file `numpy_dtype.py`



# numpy topics

- Functions for basic computation & statistics
- Boolean
- diff, dtype
- reshape(), ravel(), where() 

# reshape(), ravel()

- You can reshape the arrays using
  - `numpy.reshape()`
  - `numpy.ravel()`
- See examples in `numpy_reshape.py`
- Explanation on the next slide
- You will use `reshape()` to do something useful in the lab next week

```
b = np.array([[ 3,  9,  5,  1],
               [14, 51, 16,  7],
               [12, 39, 47, 11]])
```

```
b_flat = np.ravel(b)
```

The function `numpy.ravel()` takes a "row" (default) at a time and concatenate them

```
In [65]: b_flat
```

```
Out[65]: array([ 3,  9,  5,  1, 14, 51, 16,  7, 12, 39, 47, 11])
```

```
In [9]: b_4by3 = np.reshape(b, (4,3)); print(b_4by3)
[[ 3  9  5]
 [ 1 14 51]
 [16  7 12]
 [39 47 11]]
```

# numpy indexing

- We go back to the file `numpy_max.py`

```
30 # index_max = np.argmax(array1)
31 # indices = np.unravel_index(index_max, array1.shape)
```

- Uncomment these lines and run the file. You will find `index_max` is 7
- What is this number 7?
  - This is the “ravel” index
  - See next slide for explanation

```
array1 = np.array([ [-3.2, 0, 6.2, 5.8],  
                    [ 6, -4, 0.5, 7.1],  
                    [ 3.8, 5, 2.7, 3.7]])
```

↓ `ravel()`

```
In [69]: print(np.ravel(array1))  
[-3.2  0.   0.5  5.8  6.  -4.   6.2  7.1  3.8  5.   2.7  3.7]
```

↑ index of  
7.1 is 7

How do we get the original indices back? Let us go back to the previous slide.

# numpy.where()

- The code is at numpy\_where.py

↓ picture of array1 in numpy\_where.py

|    |    |   |   |
|----|----|---|---|
| -3 | 0  | 0 | 5 |
| 6  | -4 | 6 | 7 |
| 3  | 5  | 2 | 3 |

array1[1,3] is 7

```
print(np.where(array1 == 7))
```

```
(array([1]), array([3]))
```

# numpy.where()

- The code is at numpy\_where.py

↓ picture of array1

|    |    |   |   |
|----|----|---|---|
| -3 | 0  | 0 | 5 |
| 6  | -4 | 6 | 7 |
| 3  | 5  | 2 | 3 |

```
print(np.where(array1 >= 5))
```

The indices of the elements which are  $\geq 5$  are:

[0 , 3]

[1 , 0]

[1 , 2]

[1 , 3]

[2 , 1]

```
(array([0, 1, 1, 1, 2]), array([3, 0, 2, 3, 1]))
```

- Routines

- Array creation routines
- Array manipulation routines
- Binary operations
- String operations
- C-Types Foreign Function Interface ( `numpy.ctypeslib` )
- Datetime Support Functions
- Data type routines
- Optionally Scipy-accelerated routines ( `numpy.dual` )
- Mathematical functions with automatic domain ( `numpy.emath` )
- Floating point error handling
- Discrete Fourier Transform ( `numpy.fft` )
- Financial functions
- Functional programming
- NumPy-specific help functions
- Indexing routines
- Input and output
- Linear algebra ( `numpy.linalg` )
- Logic functions
- Masked array operations
- Mathematical functions
- Matrix library ( `numpy.matlib` )
- Miscellaneous routines
- Padding Arrays
- Polynomials
- Random sampling ( `numpy.random` )
- Set routines
- Sorting, searching, and counting
- Statistics
- Test Support ( `numpy.testing` )
- Window functions

# numpy has many functions

- The categories of functions that numpy has are listed here
  - <https://docs.scipy.org/doc/numpy/reference/>



# Summary

- Data as two-dimension numpy array
- Nested for-loops
- numpy basic concepts
  - Creation of arrays, indexing, slicing, axes
- numpy is ideal for data analysis
  - No need to use loops
  - Elementwise operation
  - Operation along an axis
- A vast collection of functions that can speed up your data analysis