

# XML and Databases

Lecture 6  
Node Selecting Queries: XPath 1.0

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## Outline

1. XPath Data Model: **7 types of nodes**
2. Simple Examples
3. Location Steps and Paths
4. Value Comparison, and Other Functions

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## XPath

- Query language to **select (a sequence of) nodes** of an XML document
- W3C Standard
- **Most important XML query language**: used in many other standards such as XQuery, XSLT, XPointer, XLink, ...
- Supported by *every modern web browser* for Java Script processing!
- Cave: version 2.0 is considerably more expressive than 1.0  
We study **XPath 1.0**

Terminology: Instead of XPath "query" we often say *XPath expression*.

(An expression is the primary construction of the XPath grammar; it matches the production [Expr](#) of the XPath grammar.)

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## Outline - Lectures

1. Introduction to XML, Encodings, Parsers
2. Memory Representations for XML: Space vs Access Speed
3. RDBMS Representation of XML
4. DTDs, Schemas, Regular Expressions, Ambiguity
5. XML Validation using Automata
6. Node Selecting Queries: **XPath**
7. Tree Automata for Efficient **XPath** Evaluation, Parallel Evaluation
8. **XPath** Properties: backward axes, containment test
9. Streaming Evaluation: how much memory do you need?
10. **XPath** Evaluation using RDBMS
11. XSLT – stylesheets and transform
12. XQuery – XML query language
13. Wrap up, Exam Preparation, Open questions, etc

XPath

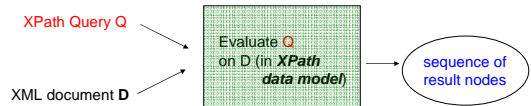
4

## Outline - Assignments

1. Read XML, using DOM parser. Create document statistics.
2. SAX Parse into memory structure: Tree and DAG
3. Map XML into RDBMS → **29. April**
4. **XPath evaluation** → **17. May**
5. **XPath** into SQL Translation → **31. May**

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## XPath Data Model



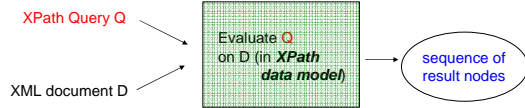
Document **D** is modeled as a **tree**.

THERE ARE SEVEN TYPES OF NODES in the XPath Data Model:

- 7 node types {
- root nodes
  - element nodes
  - text nodes
  - attribute nodes
  - namespace nodes
  - processing instruction nodes
  - comment nodes

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## XPath Data Model



Document D is modeled as a **tree**.

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- 7 node types
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- for rest of lecture: this is ALL you need to know about XML nodes! ☺

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## XPath Data Model

### 5.2.1 Unique IDs

An element node may have a unique identifier (ID).

- Value of the attribute that is declared in the DTD as type ID.
- No two elements in a document may have the same unique ID.
- If an XML processor reports two elements in a document as having the same unique ID (which is possible only if the document is invalid) then the second element in doc. order must be treated as **not** having a unique ID.

**NOTE:** If a document has no DTD, then no element will have a unique ID.

- root nodes
  - element nodes
  - text nodes
  - attribute nodes
  - namespace nodes
  - processing instruction nodes
  - comment nodes
- for rest of lecture: this is ALL you need to know about XML nodes! ☺

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## XPath Data Model

Document D is modeled as a **tree**.

For each node a **string-value** can be determined. (sometimes part of the node, sometimes computed from descendants, sometimes expanded-name: local name + namespace URI)

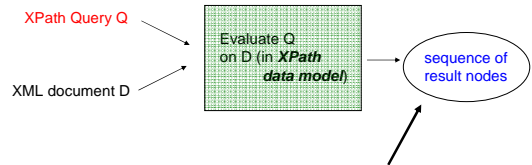
There is an order, **document order**, defined on all nodes. → corresponds to the position of the first character of the XML representation of the node, in the document (after entity expansion)

- Attribute and namespace nodes appear before the children of an element.
- Order of attribute and namespace nodes is *implementation-dependent*

Every node (besides root) has **exactly one parent** (which is a root or an element node)

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## XPath Result Sequences



- Ordered in **document order**
- Contains **no duplicates**

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## Simple Examples

In abbreviated XPath syntax.

**Q0:** / Selects the document root (always the parent of the document element)

Document: **<bib>**  
 <book>  
 <author>Abiteboul</author>  
 <author>Hull</author>  
 <author>Vianu</author>  
 <title>Foundations of Databases</title>  
 <year>1995</year>  
 </book>  
 <book>  
 <author>Ullmann</author>  
 <title>Principles of Database and Knowledge Base Systems</title>  
 <year>1998</year>  
 </book>  
 </bib>

**document root** is virtual and invisible, in this example.

If **<?xml version="1.0"?>** is present, then it is returned (as first entry) in the result of **Q0**.

**Note** XPath Evaluators usually return the full subtree of the selected node.

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## Simple Examples

In abbreviated syntax.

**Q1:** /bi b/book/year  
 → document element, if labeled **bi b**  
 → child nodes that are labeled **book**  
 → child nodes that are labeled **year**

Document: **<bib>**  
 <book>  
 <author>Abiteboul</author>  
 <author>Hull</author>  
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12

### Simple Examples

In abbreviated syntax.

Q1: `/bi b/book/year` → document element, if labeled **bi b**  
 → child nodes that are labeled **book**  
 → child nodes that are labeled **year**

Document:

```
<bib>
<book>
  <author>Abiteboul</author>
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</book>
</bib>
```

Result of query Q1 =  
 (element) nodes N1, N2  
 subtree at N1 is <year>1995</year>  
 and subtree at N2 is <year>1998</year>

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### Simple Examples

In abbreviated syntax.

Q2: `//author` → descendant or self nodes  
 → child nodes that are labeled **author**

relative to the  
 context-node  
 = root node

Document:

```
<bib>
<book>
  <author>Abiteboul</author>
  <author>Hull</author>
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  <title>Foundations of Databases</title>
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<book>
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</book>
</bib>
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// is short for /descendant-or-self::node()  
 For example, //author is short for /descendant-or-self::node()/child::author

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### Simple Examples

In abbreviated syntax.

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 that are labeled **author**

relative to the  
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</book>
<book>
  <author>Ullman</author>
  <title>Principles of Database and Knowledge Base Systems</title>
  <year>1998</year>
</book>
</bib>
```

Result of query Q2 =  
 sequence of (element) nodes  
 (N1, N2, N3, N4)

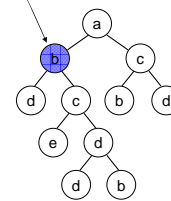
// is short for /descendant-or-self::node()  
 For example, //author is short for /descendant-or-self::node()/child::author

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### Simple Examples

In abbreviated syntax.

Q3: `/a/b//d` → "b-child of a-doc. element"



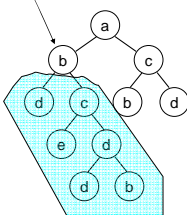
16

### Simple Examples

In abbreviated syntax.

Q3: `/a/b//d` → "b-child of a-doc. element"

ALL d-nodes  
 in these subtrees



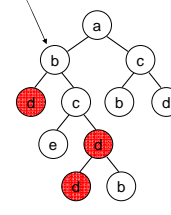
17

### Simple Examples

In abbreviated syntax.

Q3: `/a/b//d` → "b-child of a-doc. element"

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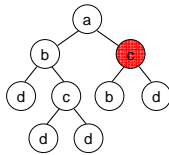


18

### Simple Examples

In abbreviated syntax.

Q4: `/* /c`

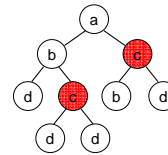


19

### Simple Examples

In abbreviated syntax.

Q5: `//c`

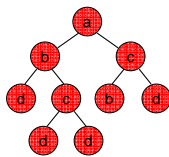


20

### Simple Examples

In abbreviated syntax.

Q6: `/**`



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### Abbreviations, so far

In abbreviated syntax.

`/a` is abbreviation for `/child::a`  
 An "Axis" (points to `/child::a`)  
 A "Nodetest" (points to `a`)

`//a` is abbreviation for `/descendant-or-self::node()/child::a`

→ Child and descendant-or-self are only 2 out of **12 possible axes**.

An "axis" is a **sequence of nodes**. It is evaluated relative to a **context-node**.

Other axes:

→ descendant	→ preceding-sibling
→ parent	→ attribute
→ ancestor-or-self	→ following
→ ancestor	→ preceding
→ following-sibling	→ self

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### Abbreviations, so far

In abbreviated syntax.

`/a` is abbreviation for `/child::a`  
 An "Axis" (points to `/child::a`)  
 A "Nodetest" (points to `a`)

`//a` is abbreviation for `/descendant-or-self::node()/child::a`  
`..` is abbreviation for `/descendant-or-self::node()/`  
`.` is abbreviation for `self::node()`  
`..` is abbreviation for `parent::node()`

→ Child and descendant-or-self are only 2 out of **12 possible axes**.

An "axis" is a **sequence of nodes**. It is evaluated relative to a **context-node**.

Other axes:

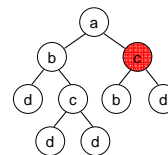
→ descendant	→ preceding-sibling
→ <b>parent</b>	→ attribute
→ ancestor-or-self	→ following
→ ancestor	→ preceding
→ following-sibling	→ <b>self</b>

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### Examples: Predicates

In abbreviated syntax.

Q7: `//c[./b]` "has b-child" (context-nodes are all c-nodes...)

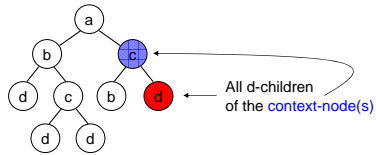


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### Examples: Predicates

In abbreviated syntax.

Q8: `//c[./b]/d` "has b-child"

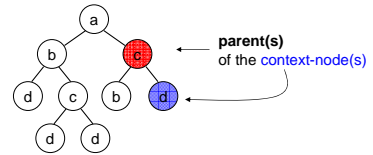


25

### Examples: Predicates

In abbreviated syntax.

Q9: `//c[./b]/d/..` "has b-child" select parent(s) of context-node(s)



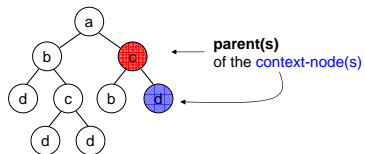
Q9 selects c-nodes that "have a b-child AND a d-child"

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### Examples: Predicates

In abbreviated syntax.

Q9: `//c[./b]/d/..` "has b-child" select parent(s) of context-node(s)



Q9 selects c-nodes that "have a b-child AND a d-child"

More direct way: `//c[./b and ./d]`

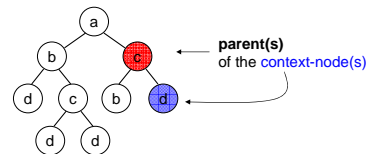
(same as `//c[./b]` on "this" tree..!)

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### Examples: Predicates

In abbreviated syntax.

Q9: `//c[b]/d/..` "has b-child" select parent(s) of context-node(s)



Q9 selects c-nodes that "have a b-child AND a d-child"

More direct way: `//c[b and d]`

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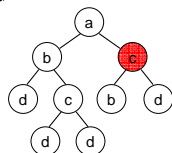
We do not need `"/b"` → `self::node()/child::b` equivalent to `b`

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### Examples: Predicates (or "Filters")

In abbreviated syntax.

`//c[b and d]` evaluates to true/false  
A "Filter"



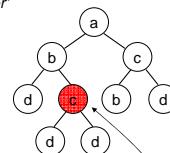
c-nodes that "have a b-child AND a d-child"

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### Examples: Predicates (or "Filters")

In abbreviated syntax.

`//c[b and d]` evaluates to true/false  
A "Filter"



Question

How to only select the other c-node?

Can use `"not( ... )"` in a filter!

`//c[not(b)]` "does not have a b-child"

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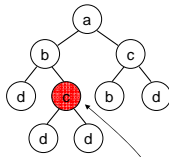
## Examples: Predicates

In abbreviated syntax.

`//c[b and d]`  
A "Filter" evaluates to **true/false**

### Question

How to only select the other c-node?



Many more possibilities, of course:

`//c[parent::b]`  
`//c[.../b]`  
`//c[.../d]`

CAVE: what does `//c[.../b]` give??

Can use "not( ... )" in a filter!

`//c[not(b)]`

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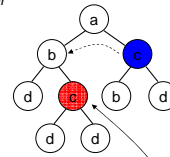
## Examples: Predicates

In abbreviated syntax.

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32

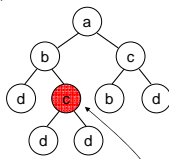
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In abbreviated syntax.

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`//c[.../d]`

Can use "not( ... )" in a filter!

`//c[not(b)]`

→ can you say "c-node that has only d-children"?

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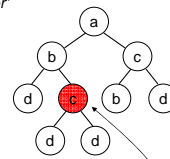
## Examples: Predicates

In abbreviated syntax.

`//c[b and d]`  
A "Filter" evaluates to **true/false**

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How to only select the other c-node?



Many more possibilities, of course:

`//c[parent::b]`  
`//c[.../b]`  
`//c[.../d]`

Can use "not( ... )" in a filter!

`//c[not(b)]`

→ can you say "c-node that has only d-children"?

YES! needs a bit of logic... `//c[not(child::*[not(self::d)])]`

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## Examples: Predicates

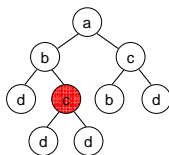
In abbreviated syntax.

`//c[not(b)]` same as .. on this tree `//c[not(child::*[not(self::d)])]`

"not the case that all children are not labeled d"

holds if and only if

"all children are labeled d"



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## Examples: Predicates

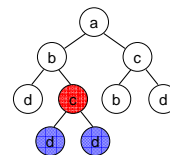
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Duplicate elimination context-nodes for parent selection (`/...`)

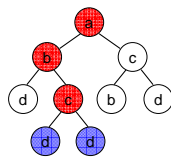
`//c[not(b)]/d/...`

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## Examples: Predicates

In abbreviated syntax.

`//c[not(b)]` same as .. on this tree `//c[not(chi1d::*[not(sel f::d)])]`



"not the case that all children are not labeled d"

holds if and only if

"all children are labeled d"

Duplicate elimination context-nodes for ancestor selection

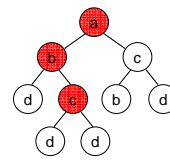
`//c[not(b)]/d/ancestor::*`

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## Examples: Predicates

In abbreviated syntax.

`//c[not(b)]` same as .. on this tree `//c[not(chi1d::*[not(sel f::d)])]`



"not the case that all children are not labeled d"

holds if and only if

"all children are labeled d"

maybe  
→ `//*[.//c[not(b)]]`

Duplicate elimination

`//c[not(b)]/d/ancestor::*`

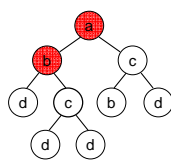
Equivalent one, without use of ancestor??

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## Examples: Predicates

In abbreviated syntax.

`//c[not(b)]` same as .. on this tree `//c[not(chi1d::*[not(sel f::d)])]`



"not the case that all children are not labeled d"

holds if and only if

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Duplicate elimination

`//c[not(b)]/d/ancestor::*`

No use of ancestor?

maybe  
→ `//*[.//c[not(b)]]`  
No.. ☹

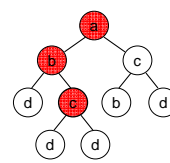
How to select the c-node?

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## Examples: Predicates

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`//c[not(b)]` same as .. on this tree `//c[not(chi1d::*[not(sel f::d)])]`



"not the case that all children are not labeled d"

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No.. ☹

Duplicate elimination

`//c[not(b)]/d/ancestor::*`

No use of ancestor?

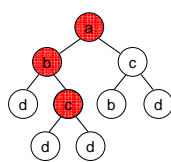
→ `//*[descendant-or-sel f::c[not(b)]]`

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## Examples: Predicates

In abbreviated syntax.

`//c[not(b)]` same as .. on this tree `//c[not(chi1d::*[not(sel f::d)])]`



"not the case that all children are not labeled d"

holds if and only if

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Duplicate elimination

`//c[not(b)]/d/ancestor::*`

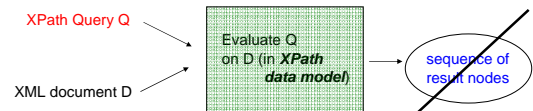
`//*[.//c[not(b)] or not(chi1d::*[not(sel f::d)]) and ./*]`  
"only d-children" "has child (not leaf)"

maybe  
→ `//*[.//c[not(b)]]`  
No.. ☹

How to select the c-node?

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## More Details



NOT correct (at least not for intermediate expr's)

An expression evaluates to an object, which has one of the following four basic types

- **node-set** (an unordered collection of nodes w/o duplicates)
- **boolean** (true or false)
- **number** (a floating-point number)
- **string** (a sequence of UCS characters)

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## Location Steps & Paths

→ A Location Path is a sequence of Location Steps

→ Initial Context will be root node

### Location Paths

- [1] LocationPath ::= RelativeLocationPath | AbsoluteLocationPath
- [2] AbsoluteLocationPath ::= '/' RelativeLocationPath? | AbbreviatedAbsoluteLocationPath
- [3] RelativeLocationPath ::= Step | RelativeLocationPath '/' Step | AbbreviatedRelativeLocationPath

### Location Steps

- [4] Step ::= AxisSpecifier NodeTest Predicate\* | AbbreviatedStep
- [5] AxisSpecifier ::= AxisName ':' | AbbreviatedAxisSpecifier

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## Location Steps & Paths

→ A Location Path is a sequence of Location Steps

→ A Location Step is of the form

axis :: **nodetest** [ Filter\_1 ] [ Filter\_2 ] ... [ Filter\_n ]

**Filters** (aka predicates, (filter) expressions)

→ evaluate to **true/false**

→ XPath queries, evaluated with

context-node = current node

Boolean operators: **and, or**

Empty string/sequence are converted to **false**

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## Location Steps & Paths

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→ A Location Step is of the form

axis :: **nodetest** [ Filter\_1 ] [ Filter\_2 ] ... [ Filter\_n ]

**Filters** (aka predicates, (filter) expressions)

evaluate to **true/false**

**nodetest**: \* or node-name (could be expanded → namespaces) or

- text()
- comment()
- processing-instruction(In)
- node()

Example child::text() "select all text node children of the context node"

→ the nodetest node() is true for any node.

attribute::\* "select all attributes of the context node"

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## Location Steps & Paths

→ A Location Path is a sequence of Location Steps

→ A Location Step is of the form

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**Filters** (aka predicates, (filter) expressions)

evaluate to **true/false**

**nodetest**: \* or node-name (could be expanded → namespaces) or

- text()
- comment()
- processing-instruction(In)
- node()

### 12 Axes

Forward Axes:

- self
- child
- descendant-or-self
- descendant
- following
- following-sibling

In doc order

Backward Axes:

- parent
- ancestor
- ancestor-or-self
- preceding
- preceding-sibling

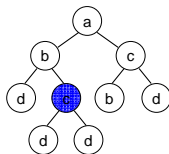
→ attribute

reverse doc order

46

## Location Steps & Paths

**Axis** = a sequence of nodes (is evaluated relative to context-node)



Forward Axes:

- self
- child
- descendant-or-self
- descendant
- following
- following-sibling

In doc order

Backward Axes:

- parent
- ancestor
- ancestor-or-self
- preceding
- preceding-sibling

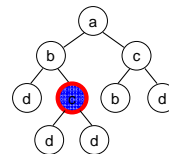
→ attribute

reverse doc order

47

## Location Steps & Paths

**Axis** = a sequence of nodes (is evaluated relative to context-node)



Forward Axes:

- self
- child
- descendant-or-self
- descendant
- following
- following-sibling

In doc order

Backward Axes:

- parent
- ancestor
- ancestor-or-self
- preceding
- preceding-sibling

→ attribute

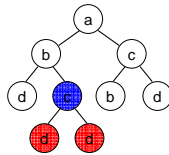
reverse doc order

48



### Location Steps & Paths

**Axis** = a sequence of nodes (is evaluated relative to **context-node**)



Forward Axes:

- self
- **child**
- descendant-or-self
- descendant
- following
- following-sibling

Backward Axes:

- parent
- ancestor
- ancestor-or-self
- preceding
- preceding-sibling

→ attribute

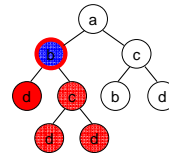
reverse doc order

In doc order

49

### Location Steps & Paths

**Axis** = a sequence of nodes (is evaluated relative to **context-node**)



Forward Axes:

- self
- child
- **descendant-or-self**
- descendant
- following
- following-sibling

Backward Axes:

- parent
- ancestor
- ancestor-or-self
- preceding
- preceding-sibling

→ attribute

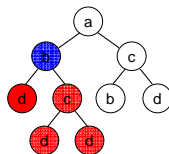
reverse doc order

In doc order

50

### Location Steps & Paths

**Axis** = a sequence of nodes (is evaluated relative to **context-node**)



Forward Axes:

- self
- child
- descendant-or-self
- **descendant**
- following
- following-sibling

Backward Axes:

- parent
- ancestor
- ancestor-or-self
- preceding
- preceding-sibling

→ attribute

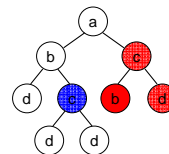
reverse doc order

In doc order

51

### Location Steps & Paths

**Axis** = a sequence of nodes (is evaluated relative to **context-node**)



Forward Axes:

- self
- child
- descendant-or-self
- descendant
- **following**
- following-sibling

Backward Axes:

- parent
- ancestor
- ancestor-or-self
- preceding
- preceding-sibling

→ attribute

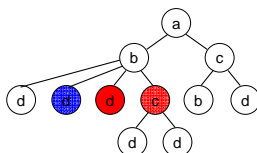
reverse doc order

In doc order

52

### Location Steps & Paths

**Axis** = a sequence of nodes (is evaluated relative to **context-node**)



Forward Axes:

- self
- child
- descendant-or-self
- descendant
- following
- **following-sibling**

Backward Axes:

- parent
- ancestor
- ancestor-or-self
- preceding
- preceding-sibling

→ attribute

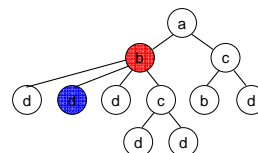
reverse doc order

In doc order

53

### Location Steps & Paths

**Axis** = a sequence of nodes (is evaluated relative to **context-node**)



Forward Axes:

- self
- child
- descendant-or-self
- descendant
- following
- following-sibling

Backward Axes:

- **parent**
- ancestor
- ancestor-or-self
- preceding
- preceding-sibling

→ attribute

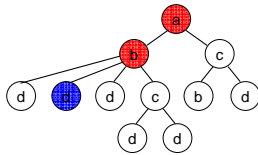
reverse doc order

In doc order

54

## Location Steps & Paths

**Axis** = a sequence of nodes (is evaluated relative to **context-node**)



Forward Axes:

→ self  
→ child  
→ descendant-or-self  
→ descendant  
→ following  
→ following-sibling

Backward Axes:

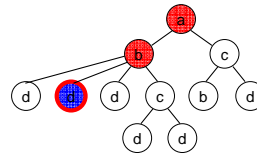
→ parent  
→ **ancestor**  
→ ancestor-or-self  
→ preceding  
→ preceding-sibling  
→ attribute

In doc order

55

## Location Steps & Paths

**Axis** = a sequence of nodes (is evaluated relative to **context-node**)



Forward Axes:

→ self  
→ child  
→ descendant-or-self  
→ descendant  
→ following  
→ following-sibling

Backward Axes:

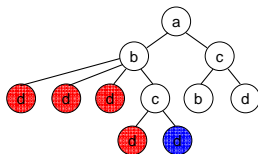
→ parent  
→ ancestor  
→ **ancestor-or-self**  
→ preceding  
→ preceding-sibling  
→ attribute

In doc order

56

## Location Steps & Paths

**Axis** = a sequence of nodes (is evaluated relative to **context-node**)



Forward Axes:

→ self  
→ child  
→ descendant-or-self  
→ descendant  
→ following  
→ following-sibling

Backward Axes:

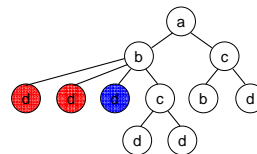
→ parent  
→ ancestor  
→ ancestor-or-self  
→ **preceding**  
→ preceding-sibling  
→ attribute

In doc order

57

## Location Steps & Paths

**Axis** = a sequence of nodes (is evaluated relative to **context-node**)



Forward Axes:

→ self  
→ child  
→ descendant-or-self  
→ descendant  
→ following  
→ following-sibling

Backward Axes:

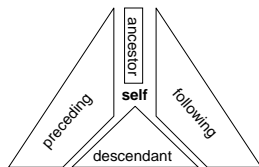
→ parent  
→ ancestor  
→ ancestor-or-self  
→ **preceding-sibling**  
→ attribute

In doc order

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## Location Steps & Paths

**Axis** = a sequence of nodes (is evaluated relative to **context-node**)



Forward Axes:

→ self  
→ child  
→ descendant-or-self  
→ descendant  
→ following  
→ following-sibling

Backward Axes:

→ parent  
→ ancestor  
→ ancestor-or-self  
→ preceding  
→ preceding-sibling  
→ attribute

In doc order

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## Location Path Evaluation

**Context** of an XPath evaluation:

- (1) context-node
- (2) context position and size (both non-negative integers)
- (3) set of variable bindings (= mappings from variable names to values)
- (4) function library (= mapping from function names to functions)
- (5) set of namespace declarations

(btw: context position is  $\leq$  context size)

Application determines the **Initial Context**.

If path starts with "/", then **Initial Context** has

- context-node = root node
- context-position = context-size = 1

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## Location Path Semantics

→ A Location Path **P** is a sequence of Location Steps

$a_1 :: n_1 [F_{1_1}] [F_{1_2}] \dots [F_{1_{n1}}]$   
 $/ a_2 :: n_2 [F_{2_1}] [F_{2_2}] \dots [F_{2_{n2}}]$   
 $/ a_m :: n_m [F_{m_1}] [F_{m_2}] \dots [F_{m_{nm}}]$

**S0** = initial sequence of context-nodes

- (1) (to each) context-node **N** in **S0**, apply axis **a<sub>1</sub>**: gives sequence **S1** of nodes
- (2) remove from **S1** any node **M** for which
  - test **n<sub>1</sub>** evaluates to false
  - any of filters **F<sub>1\_1</sub>, ..., F<sub>1\_{n1}</sub>** evaluate to false.

Apply steps (1)&(2) for step 2, to obtain from **S1** the sequence **S2**  
 3, **S2** **S3**  
 ...  
 m **S(m-1)** **Sm**

= result of **P** 61

## No Looking Back

Backward Axes are not needed!!

→ possible to rewrite most XPath queries into equivalent ones that **do not use backward axes**.

Very nice result!

Can you see how this could be done?

→ We saw an example of removing ancestor axis. But, of course the rewritten query must be the same ON EVERY possible tree!!

**Questions** how much larger does the query get, when you remove all backward axis?  
 Is this useful for efficient query evaluation?!

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## Attribute Axis

How to  
 → test **attribute** nodes

Examples

`//attribute::*`

Result:

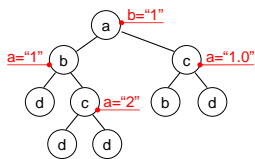
`b="1"`  
`a="1"`  
`a="2"`  
`a="1.0"`

Remember, these are just NODEs.

`//attribute::*/.` gives same result

And `//attribute::a/..` gives

`<b a="1"><d/><c a="2"><d/></c/></b>`  
`<c a="2"><d/></c/>`  
`<c a="1.0"><b/><d/></c/>`



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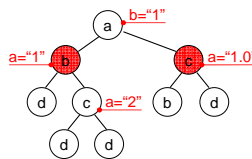
## Attribute Axis & Value Tests

How to  
 → test **attribute values**

Examples

`//*[attribute::a=1]`

(selects the two red nodes)



64

## Attribute Axis & Value Tests

How to  
 → test **attribute values**

Examples

`//*[attribute::a=1]`

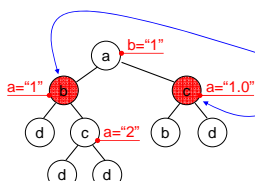
(selects the two red nodes)

Watch out

`//*[attribute::a="1"]` only gives

`//*[attribute::a="1.0"]` only gives

string comparison



65

## Attribute Axis & Value Tests

How to  
 → test **attribute values**

Examples

`//*[attribute::a=1]`

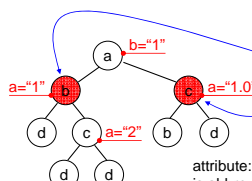
(selects the two red nodes)

Watch out

`//*[attribute::a="1"]` only gives

`//*[attribute::a="1.0"]` only gives

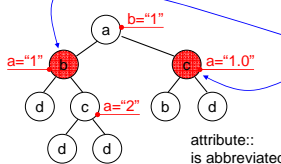
attribute:: is abbreviated by @  
 string comparison



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## Attribute Axis & Value Tests

How to  
→ test **attribute** values



`//*[@a!="1"]` selects both c-nodes  
`//*[@a>1]` selects only left c-node  
`//*[@a=//@b]` selects what?? (hint: "=" is string comp. here)

Examples

`//*[attribute::a=1]`

(selects the two red nodes)

Watch out

`//*[@attribute::a="1"]` only gives

`//*[@attribute::a="1.0"]` only gives

@  
string comparison

attribute::  
is abbreviated by @

number (float)  
comparison

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## Tests in Filters

- or
- and
- =, !=
- <=, <, >=, >

Boolean **true**  
coerced to a float 1.0

The operators are all left associative.  
For example,  $3 > 2 > 1$  is equivalent to  $(3 > 2) > 1$ , which evaluates to **false**.

But,  $3 > 2 > 0.9$  evaluates to **true**. Can you see why?

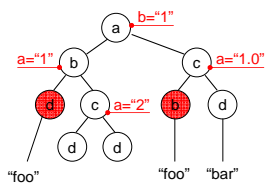
For two strings *u*, *v*

`u<=v`  
`u<v`  
`u>=v`  
`u>v` } Always return **false!**  
→ Unless both *u* and *v* are numbers.  
`["1.0">="1"]` evaluates to **true**.

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## Text Nodes

How  
→ test text nodes & values



`//text()`

Result:  
foo  
foo  
Bar

`//*[text()="foo"]`

Result: the two red nodes

Question:

What is the result for  
`//*[text()=//b/text()]`

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## Useful Functions (on Booleans)

→ `boolean(object): boolean` ("boolean" means {true/false})

Converts argument into **true/false**:

- a **number** is **true** if it is not equal to zero (or NaN)
- a **node-set** is **true** if it is non-empty
- a **string** is **true** if its length is non-zero
- for other objects, conversion depends on type

→ `not(true)=false`, `not(false)=true`

→ `true(): boolean`

→ `false(): boolean`

→ `lang(string): boolean`

Returns **true** if language specified by `xml:lang` attributes is same as string

Useful even for use with self-axis:

`child::*[self::chapter or self::appendix]`

chapter or appendix  
children of  
context node

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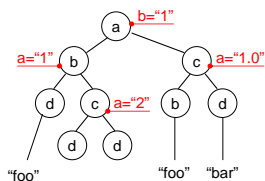
## Useful Functions (on Node Sets)

→ `count`

Counts number or results

`/a[count(//*[text()=//b/text()])=2]`

What is the result?



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## Useful Functions (on Node Sets)

→ `count`

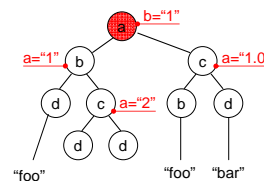
Counts number or results

`/a[count(//*[text()=//b/text()])=2]`

What is the result?

Same result as:

`/a[count(//*[text()="foo"])`  
`> count(//*[text()="bar"])]`



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### Useful Functions (on Node Sets)

→ **count**  
Counts number or results

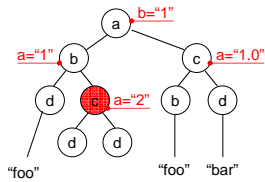
What is the result?

Same result as:

```
/a[count(/**[text()=//b/text()]=2)]
> count(/**[text()='bar'])]
```

What is the result for:

```
/**c[count(b)=0]
(same as /**[not(b)])
```



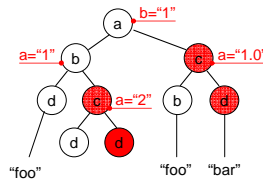
73

### Useful Functions (on Node Sets)

→ **last()**  
returns context-size from the evaluation context

→ **position()**  
Returns context-position from the eval. context

```
/**[position()=2]
```



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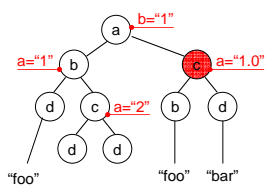
### Useful Functions (on Node Sets)

→ **last()**  
returns context-size from the evaluation context

→ **position()**  
Returns context-position from the eval. context

```
/**[position()=2]
```

```
/**[position()=2 and .../a]
Same as
/**[position()=2 and ./b]
```



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### Useful Functions (on Node Sets)

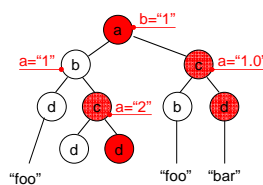
→ **last()**  
returns context-size from the evaluation context

→ **position()**  
Returns context-position from the eval. context

```
/**[position()=2]
```

```
/**[position()=2 and .../a]
Same as
/**[position()=2 and ./b]
```

```
/**[position()=last()]
```



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### Useful Functions (on Node Sets)

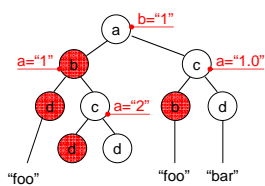
→ **last()**  
returns context-size from the evaluation context

→ **position()**  
Returns context-position from the eval. context

```
/**[position()=2]
```

```
/**[position()=2 and .../a]
Same as
/**[position()=2 and ./b]
```

```
/**[position()=last()-1]
```



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### Useful Functions (on Node Sets)

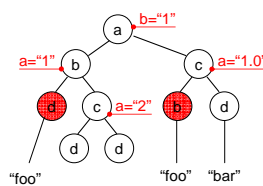
→ **last()**  
returns context-size from the evaluation context

→ **position()**  
Returns context-position from the eval. context

```
/**[position()=2]
```

```
/**[position()=2 and .../a]
Same as
/**[position()=2 and ./b]
```

```
/**[position()=last()-1
and ./text()='foo']
```

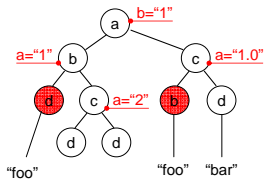


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### Useful Functions (on Node Sets)

→ `last()`  
returns context-size from the evaluation context

→ `position()`  
Returns context-position from the eval. context



```

/**[position()=2]
/**[position()=2 and .../a]
Same as
/**[position()=2 and ./b]

/**[position()=last()-1
and ./text()='foo']

```

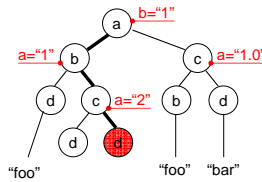
Useful:  
`child:.*[self::chapter or self::appendix][position()=last()]`  
 selects the last chapter or appendix child of the context node

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### Useful Functions (on Node Sets)

→ `last()`  
returns context-size from the evaluation context

→ `position()`  
Returns context-position from the eval. context



```

/**[position()=2]
/**[position()=2 and .../a]
Same as
/**[position()=2 and ./b]

/**[position()=last()-1
and ./text()='foo']

```

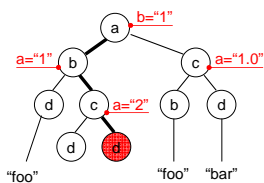
`.*[position()=1]/.*[position()=2]/.*[position()=2]`  
 → allows absolute location of any node (a la Dewey)

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### Useful Functions (on Node Sets)

→ `last()`  
returns context-size from the evaluation context

→ `position()`  
Returns context-position from the eval. context



```

/**[position()=2]
/**[position()=2 and .../a]
Same as
/**[position()=2 and ./b]

/**[position()=last()-1
and ./text()='foo']

```

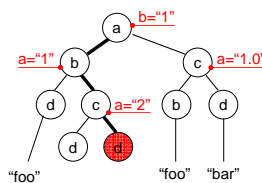
`.*[position()=1]/.*[position()=2]/.*[position()=2]`  
 Abbreviation: `.*[1]/.*[2]/.*[2]`

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### Useful Functions (on Node Sets)

→ `last()`  
returns context-size from the evaluation context

→ `position()`  
Returns context-position from the eval. context



```

/**[position()=2]
/**[position()=2 and .../a]
Same as
/**[position()=2 and ./b]

/**[position()=last()-1
and ./text()='foo']

```

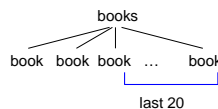
`.*[position()=1]/.*[position()=2]/.*[position()=2]`  
 Abbreviation: `.*[1]/.*[2]/.*[2]` → What is result for `.*[.]/.*[2]/.*[2]`

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### Useful Functions (on Node Sets)

→ `last()`  
returns context-size from the evaluation context

→ `position()`  
Returns context-position from the eval. context



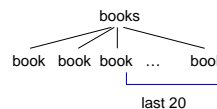
How do you select the  
last 20 book-children of books?

83

### Useful Functions (on Node Sets)

→ `last()`  
returns context-size from the evaluation context

→ `position()`  
Returns context-position from the eval. context



How do you select the  
last 20 book-children of books?

`/books/book[position()>last()-20]`

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## Useful Functions (on Node Sets)

- `last(): number`  
returns context-size from the evaluation context
- `position(): number`  
returns context-position from the eval. Context
- `id(object): node-set`  
`id("foo")` selects the element with unique ID foo
- `local-name(node-set?): string`  
returns the local part of the expanded-name of the node
- `namespace-uri (node-set?): string`  
returns the namespace URI of the expanded-name of the node
- `name(node-set?): string`  
returns a string containing a QName representing the expanded-name of the node

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## Useful Functions (on Node Sets)

Nodes have an identity XPath 2.0 has much clearer comparison operators!!

`<a>`  
`<b>tt</b>`  
`<b>tt</b>`  
`</a>`

Different nodes!

~~`//a[*[1]=*[2]]`~~  
gives empty result.

Sorry. This is **wrong**. Equality ("=") is based on string value of a node!  
→ Gives also a-node

But:  
`//a[contains(*[1], *[2])]`  
gives the a-node.  
string-value ("tt") is contained in "tt"

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## Useful Functions (on Node Sets)

Careful with equality ("=")

XPath 2.0 has much clearer comparison operators!!

`<a>`  
`<b>`  
`<d>red</d>`  
`<d>green</d>`  
`<d>blue</d>`  
`</b>`  
`<c>`  
`<d>yellow</d>`  
`<d>orange</d>`  
`<d>green</d>`  
`</c>`  
`</a>`

`//a[b/d = c/d]` selects a-node!!!

Sorry. This is **wrong**. Equality ("=") is based on string value of a node!  
→ Gives also a-node

there exists a node in the node set for `b/d` with same string value as a node in node set `c/d`

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## Useful Functions (on Node Sets)

Careful with equality ("=")

XPath 2.0 has much clearer comparison operators!!

`<a>`  
`<b>`  
`<d>red</d>`  
`<d>green</d>`  
`<d>blue</d>`  
`</b>`  
`<c>`  
`<d>yellow</d>`  
`<d>orange</d>`  
`<d>green</d>`  
`</c>`  
`</a>`

`//a[b/d = c/d]` selects a-node!!!

Sorry. This is **wrong**. Equality ("=") is based on string value of a node!  
→ Gives also a-node

there exists a node in the node set for `b/d` with same string value as a node in node set `c/d`

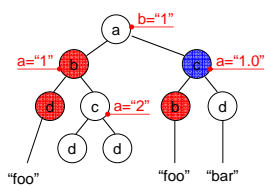
→ What about `//a[b/d != c/d]`

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## Useful Functions (Strings)

The string-value of an element node is the concatenation of the string-values of all text node descendants in document order.

`//*[. = "foo"]`  
`//*[. = "foobar"]`

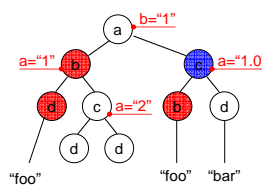


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## Useful Functions (Strings)

The string-value of an element node is the concatenation of the string-values of all text node descendants in document order.

`//*[. = "foo"]`  
`//*[. = "foobar"]`



→ `concat(st_1, st_2, ..., st_n) = st_1 st_2 ... st_n`  
→ `startswith("abcd", "ab") = true`  
→ `contains("bar", "a") = true`  
→ `substring-before("1999/04/01", "/") = 1999`  
→ `substring-after("1999/04/01", "19") = 99/04/01`  
→ `substring("12345", 2, 3) = "234"`  
→ `string-length("foo") = 3`

What is the result to this: `//*[contains(., "bar")]`

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## Useful Functions (Strings)

The **string-value** of an element node is the concatenation of the **string-values** of all text node **descendants** in document order.

```
/**[. ="foo"]
/**[. ="foobar"]
```

→ **normalize-space**(" foo bar a ") = "foo bar a"

→ **translate**("bar", "abc", "ABC") = BA r

returns the first argument string with occurrences of characters in the second argument string replaced by the character at the corresponding position in the third argument string

**NOTE:** The **translate** function is not a sufficient solution for case conversion in all languages

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## Useful Functions (Numbers)

→ **number(object): number**

**Operators on Numbers**  
+, -, \*, div, mod

Converts argument to a number

- the boolean true is converted to 1, false is converted to 0
- a string that consists of optional whitespace followed by an optional minus sign followed by a **Number** followed by whitespace is converted to the IEEE 754 number that is nearest to the mathematical value represented by the string.

→ **sum(node-set): number**

returns sum, for each node in the argument node-set, of the result of converting the **string-values** of the node to a number

→ **floor(number): number**

returns largest integer that is not greater than the argument

→ **ceiling(number): number**

returns the smallest integer that is not less than the argument

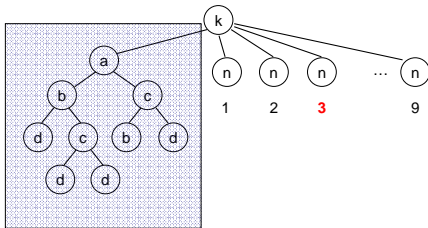
→ **round(number): number**

returns integer closest to the argument. (if there are 2, take above:  
**round(0.5)=1** and **round(-0.5)=0**)

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## Display Number Result...

```
/**[text()=7 mod (count(/b)+2)]/text()
```

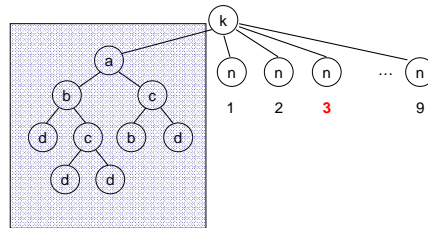


Use <http://b-cage.net/code/web/xpath-evaluator.html>

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## Display Number Result...

```
/**[text()=7 mod (count(/b)+2)]/text()
```



Similar for arbitrary large numbers / booleans, node-sets... Try it... ☺

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## XPath Query Evaluation

How to implement?

How expensive? complexity?

What are the most difficult queries?

**Next time**

Efficient Algorithms: *which queries run how fast?*

First, focus on *navigational queries*: only /, //, label-test, [ filters ]

(techniques for value comparison/queries already well-known from rel. DB's...)

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means year **2003**...

↓

## Experiments with current systems

Next 4 slides from  
Georg Gottlob and Christoph Koch "XPath Query Processing".  
Invited tutorial at DBPL **2003**  
<http://www.dbai.tuwien.ac.at/research/xmltaskforce/xpath-tutorial1.ppt.gz>



$$P[\pi_1/\pi_2](x) := \bigcup_{y \in P[\pi_1](x)} P[\pi_2](y)$$

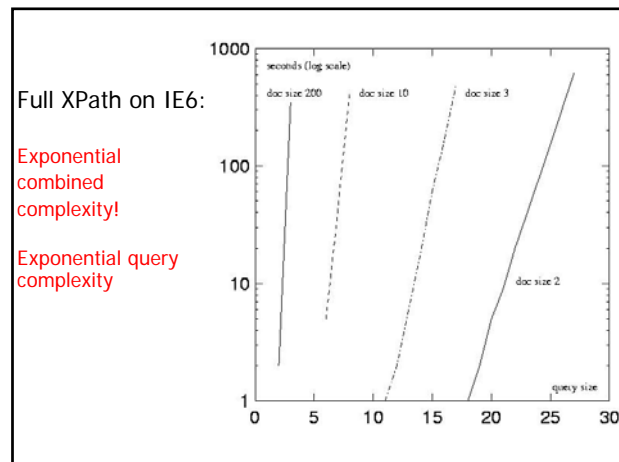
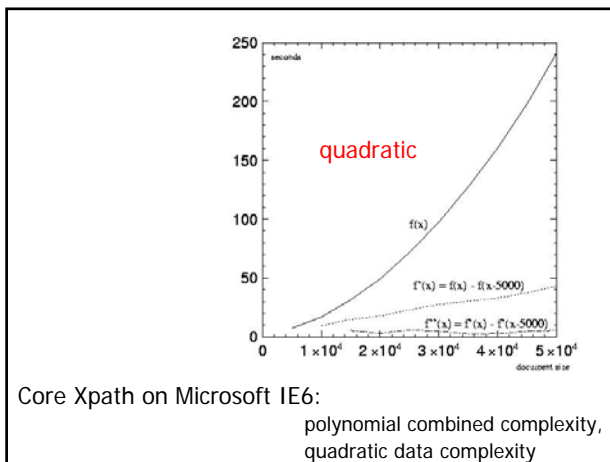
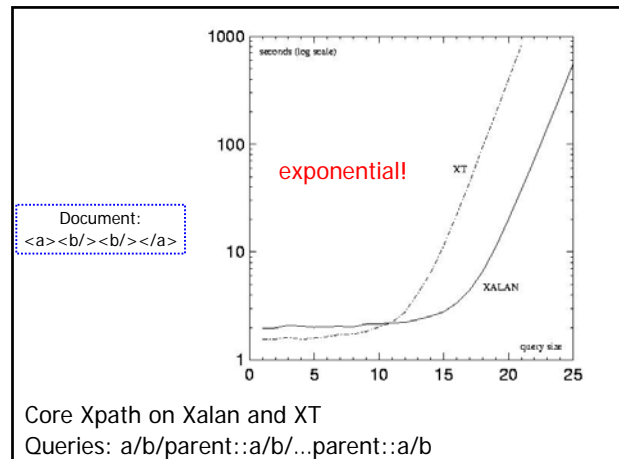
context node  
 $P[\pi_1/\pi_2](x) := \bigcup_{y \in P[\pi_1](x)} P[\pi_2](y)$

procedure process-location-step( $n_0, Q$ )  
 /\*  $n_0$  is the context node;  
 query  $Q$  is a list of location steps \*/  
 begin  
 node set  $S := \text{apply } Q.\text{first}$  to node  $n_0$ ;  
 if ( $Q.\text{tail}$  is not empty) then  
 for each node  $n \in S$  do  
 process-location-step( $n, Q.\text{tail}$ );  
 end

Document:  
 $\langle a \rangle \langle b \rangle \langle c \rangle \langle /a \rangle$

Xpath Query (relative to a):  
 child::\* / parent::\* / child::\* /  
 parent::\* / child::\*

Tree of nodes visited is of size  
 $O(|D|^{|\mathcal{Q}|})$  !!!



### XPath Query Evaluation

Static Methods (used, e.g., for Query Optimization...)

Given Xpath queries  $Q_1, Q_2$ :

- Is result set of  $Q_1$  included in result set of  $Q_2$ ?
- Are result sets equal?
- Is their intersection empty?

for all possible documents

(probably we will look at this in Lecture 8 or 9)

### Simple Examples

Is  
 $//c[\text{count}(d)=\text{count}(*)]$

equivalent to  
 $//c[\text{not}(\text{child::d}::*[\text{not}(\text{self::d})])]$

on all possible trees?

END  
Lecture 6

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