

XML and Databases

Efficient XPath evaluation

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Week 7

XPath

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All the p_i have the form:

$$p_i ::= [(a_{i1}, l_{i1}, []); \dots; (a_{in}, l_{in}, [])]$$

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Node Set Algorithm (1/6)

```
NodeSet eval(Path p, NodeSet nodes, bool all)
```

Given a set of nodes of `nodes` of a document apply the path `p` to the set of node and returns:

- ▶ All the nodes matching the query if `all` is true
- ▶ The first node matching the query if `all` is false

```
NodeSet eval_axis(Axis a, Label l, NodeSet nodes, bool all)
```

Given a set of nodes of `nodes` of a document returns the nodes in the axis `a` with label `l`

- ▶ if `all` is true, returns all the matching nodes.
- ▶ if `all` is false, returns the first matching node

Node Set Algorithm (2/6)

```
NodeSet eval(Path p, NodeSet nodes, bool all){
    NodeSet r = nodes;
    //we apply the steps one after another
    for each (a,l,f) in p {
        //we select all the node matching the axis and label
        r = eval_axis(a,l,r,all);
        if (filter != []) {
            r' = Empty;
            for each n in r
                if (eval(f,{ n },false) != Empty)
                    r' = add(r',n);
            r = r';
        };
    }
    return r;
}
```

Node Set Algorithm (3/6)

```
NodeSet eval_axis(Axis a, Label l, NodeSet n, bool all)
{
    switch (a){
        child:
            return eval_child(l, n, all);
        descendant:
            return eval_descendant(l, n, all);
        //continue for all the axes
        ...
    }
}
```

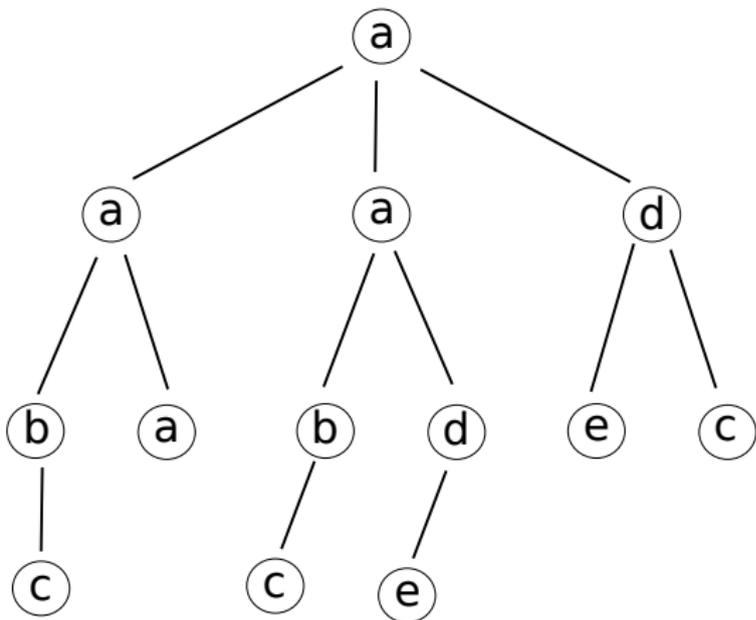
Node Set Algorithm (4/6)

```
NodeSet eval_descendant(Label l, NodeSet n, bool all)
{
    NodeSet r = Empty;
    for each t in n {
        for each tc in children(t) {
            if (label(tc) == l){
                r = add(r, tc);
                if (!(all)) //we only want the first result
                    return r;
            }
        }; //r contains all the children of t tagged l
        r = r  $\cup$  eval_descendant(l, children(t));
    }
    return r;
}
```

Node Set Algorithm (5/6)

Example: XPath expression `//a[d//e]/b//c`

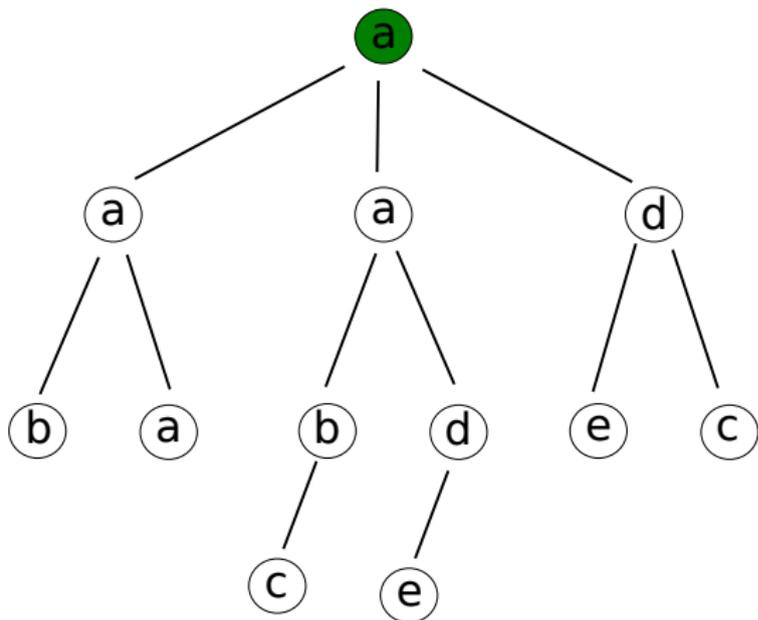
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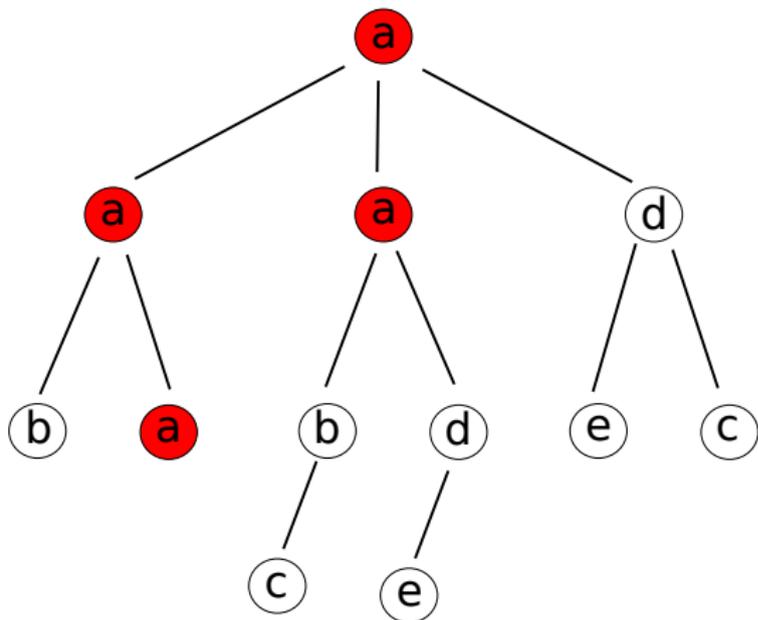
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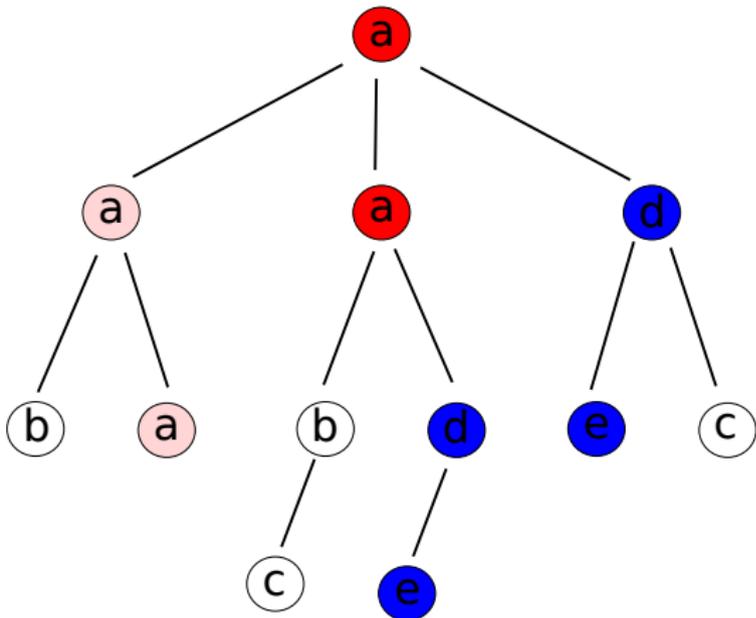


`eval_axis(desc,a,...,true)`

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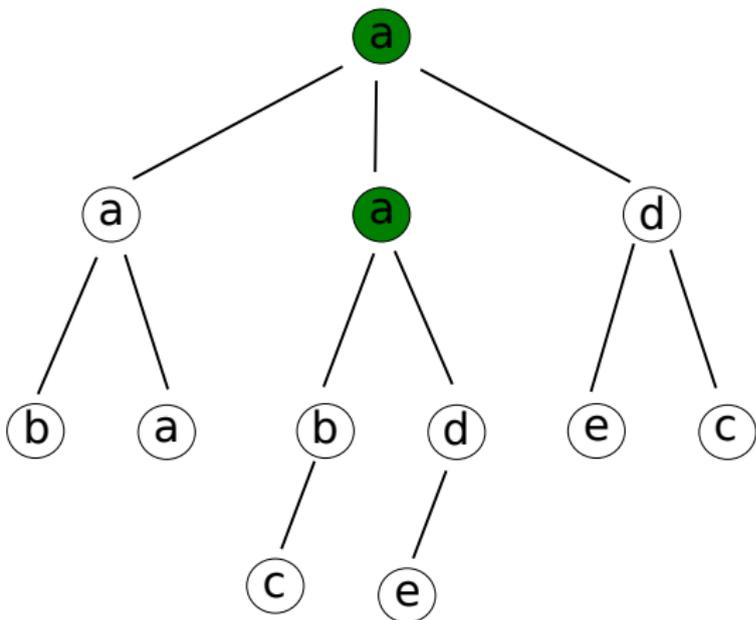


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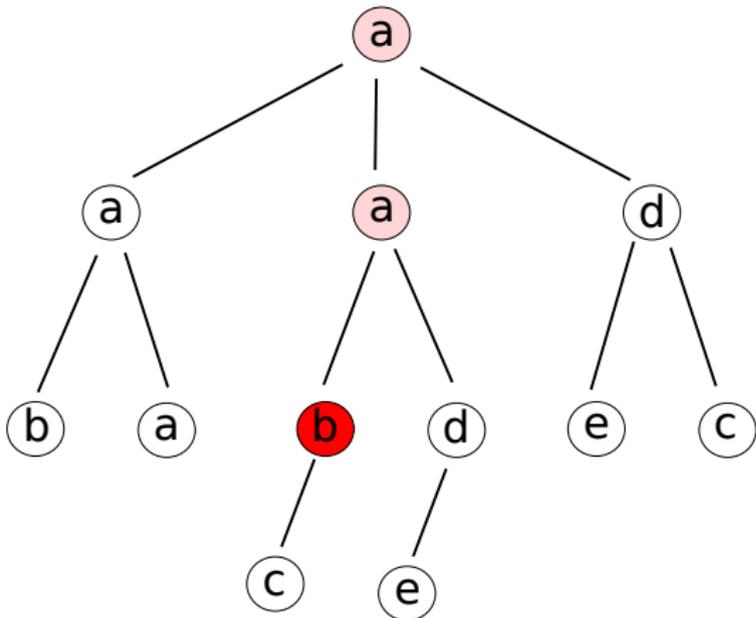
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Result of the first step

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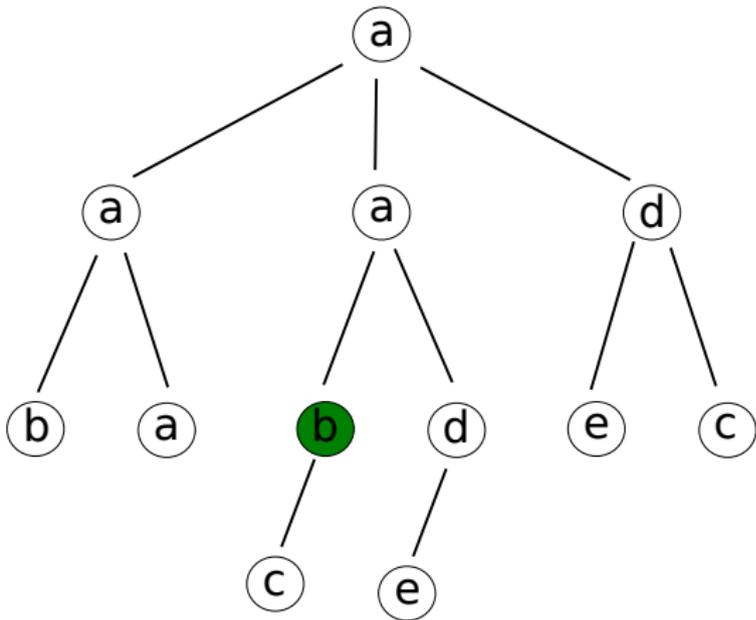
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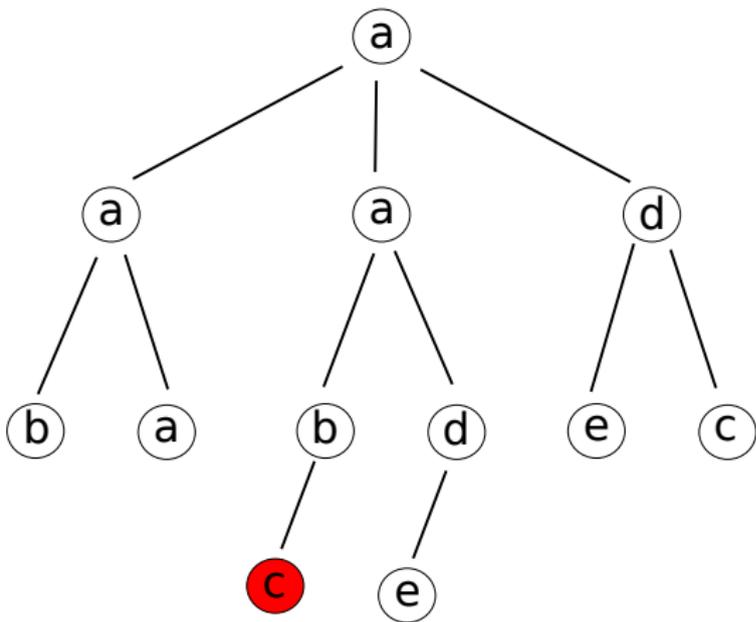
Result of the first step

`eval_axis(child,b,...,true)`
Result of the 2nd step

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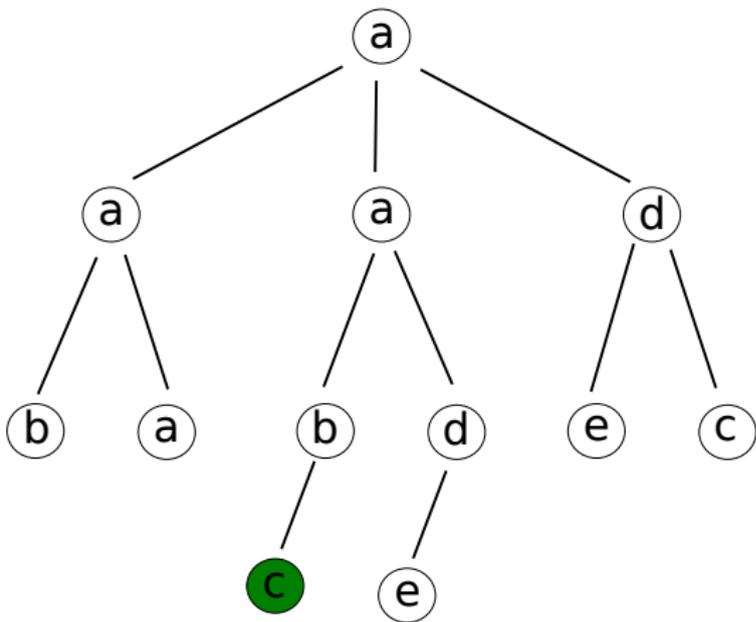
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Final result

Node Set Algorithm (6/6)

Pros and cons of the algorithm:

+ Easy to implement

Remains very inefficient: $O(|D|^2)$ for forward XPath, $O(2^{|\mathcal{Q}|} + |D|^2)$ for full XPath (cf. Lecture)

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- + Easy to implement
- + Can be extended to all XPath axes easily
 - May return several copies of the same node, thus either use a Set datastructure for the result, or sort and sieve the result at the end.
 - **Need to traverse many times the tree, cannot be done in streaming**

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Automata based algorithm

We proceed in two steps:

- ▶ first we see how this works for XPath expressions without filters

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The idea is to see the XPath expression as a regular expression matching the paths of the tree. The translation of a *forward* XPath expression into an NFA is straightforward:

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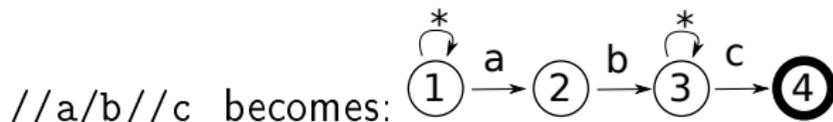
`//a/b//c` becomes:

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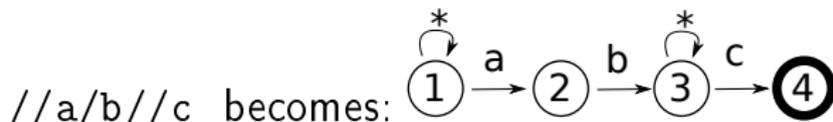


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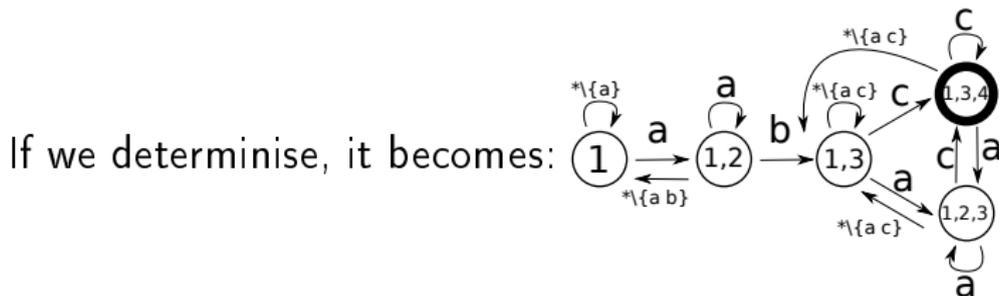
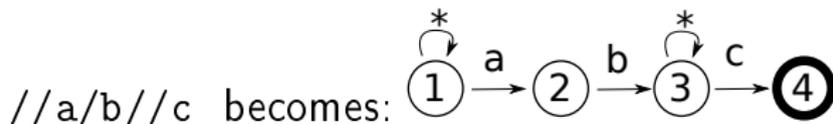
If we determinise, it becomes:

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Problems of determinisation:

- ▶ Exponential blow-up in the number of states

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Good news: we don't need to determinize!

Reference:

Processing XML streams with deterministic automata and stream indexes
By T.J. Green, A. Gupta, G. Miklau, M. Onizuka, D. Suciu, TODS 2004

Topdown XPath evaluation

```
// Takes a NFA, a set of states and a document node
// Returns the set of nodes matched by the automaton
NodeSet eval(Automaton a, States S, Node t){
    //The empty tree yields no result
    if (t == null) return Empty
    else { //Everything is done here, see next slide
        S'={q' |  $\forall q \in S$ , s.t.  $q, l \rightarrow q' \in a$ ,  $l = \text{label}(t)$  or *}
        r = Empty;
        for each t' in children(t) {
            r = r  $\cup$  eval(a, S', t');
        };
        if (finalstate(a)  $\in$  S')
            r = r  $\cup$  {t}
    };
    return r;
}
```

Topdown XPath evaluation

What does this do?

$$S' = \{q' \mid \forall q \in S, \text{ s.t. } q, l \rightarrow q' \in a, l = \text{label}(t) \text{ or } *\}$$

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For each state q of the NFA in S it computes the set of states in which we can go with the label of the current node t

- ▶ Then we recursively evaluate S' on all the children of t
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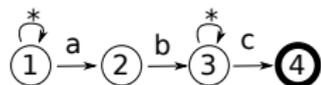
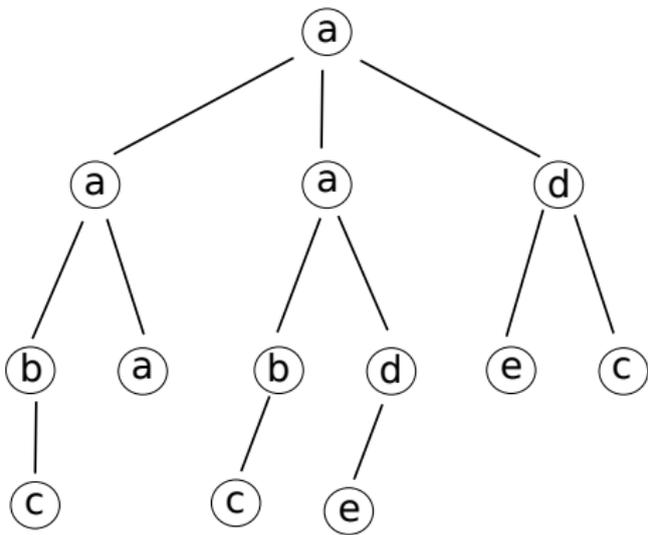
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To represent the NFA, we need:

- ▶ The set of all states, Q , the initial state I , the final state F
- ▶ a hash table mapping pairs of states \times labels to states

Topdown XPath evaluation



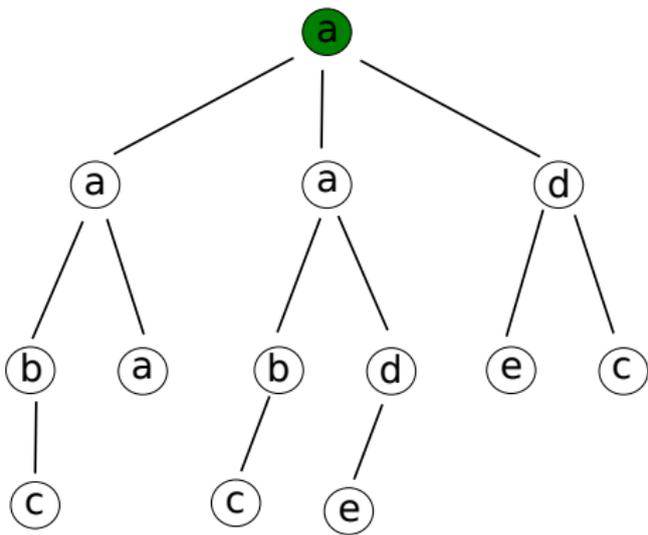
$Q = \{1, 2, 3, 4\}$

$I = \{1\}$

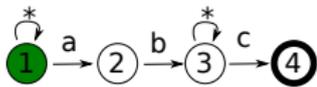
$F = \{4\}$

1	,	a	↦	2
1	,	*	↦	1
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Topdown XPath evaluation



We start on the root, with the initial state



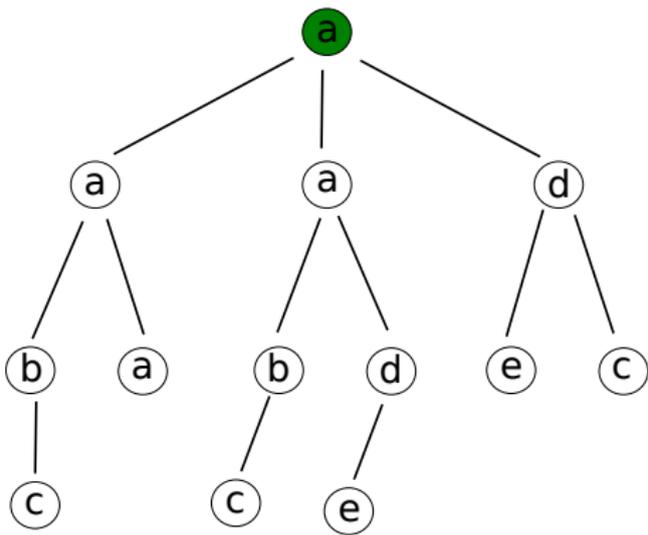
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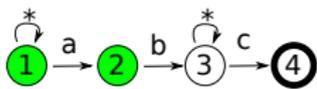
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Topdown XPath evaluation



For label "a" in state 1, the NFA can end up in two states, 1 and 2...



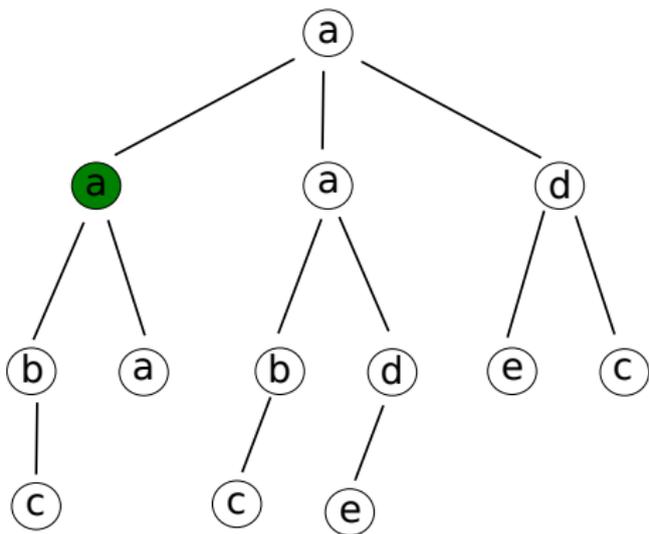
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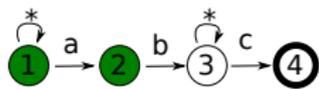
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Topdown XPath evaluation



So we call recursively,
with $S = \{1, 2\}$ on
the first child of the
root...



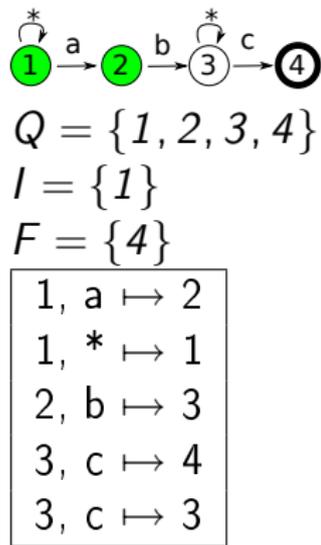
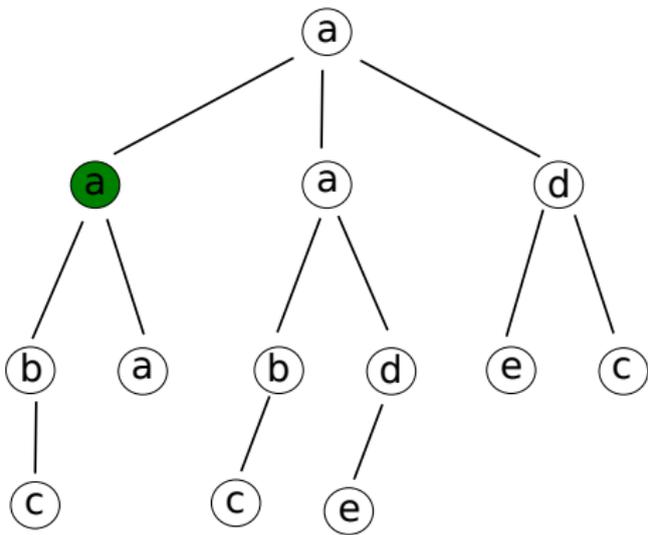
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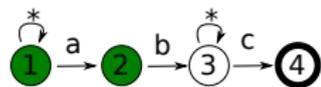
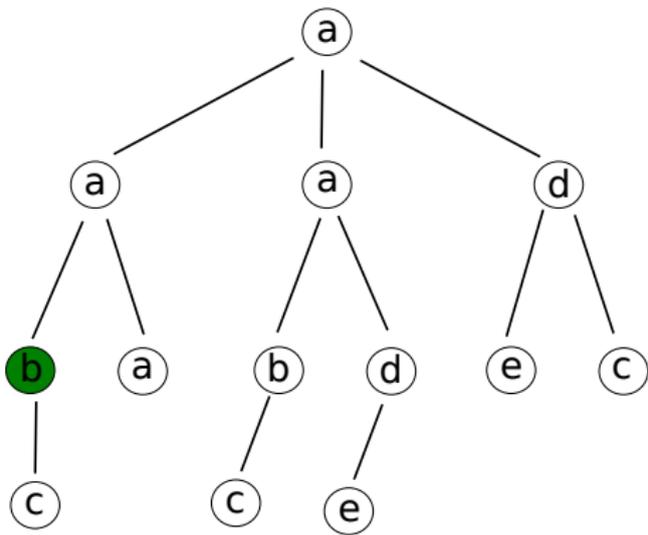
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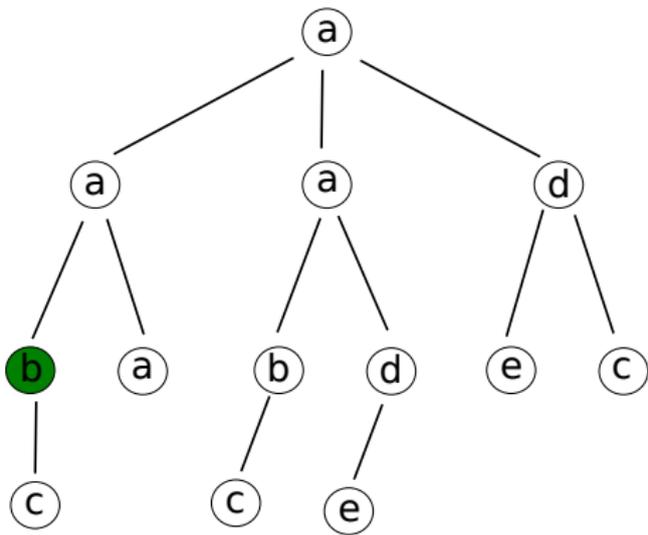
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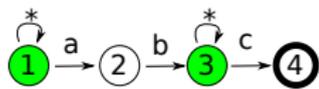
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Topdown XPath evaluation



Here label "b" allows us to go in state 3 and also stays in state 1



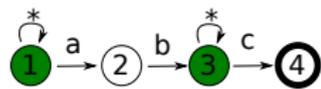
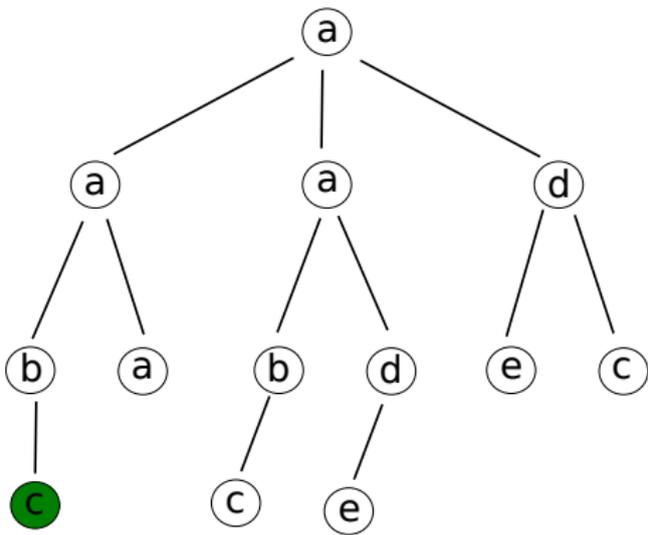
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Topdown XPath evaluation



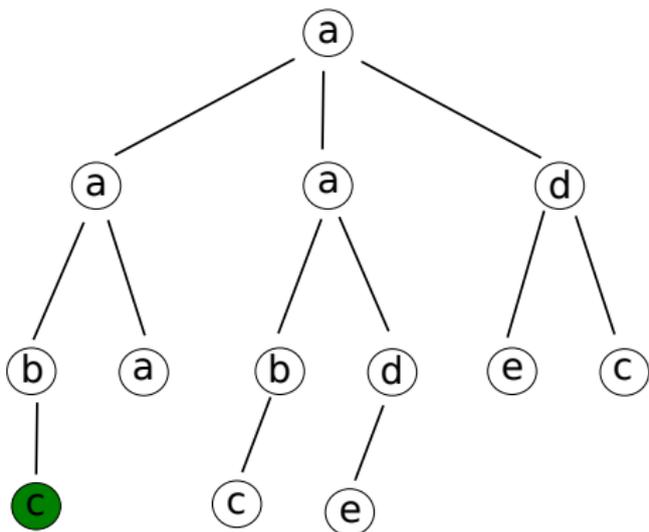
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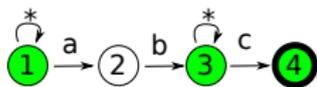
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Topdown XPath evaluation



We arrive in "c". The call on the children returns Empty. One of our state is final, so there is a run of the automaton which accepts this path, we mark the node as **selected**.



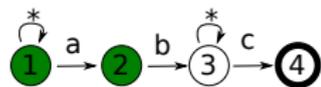
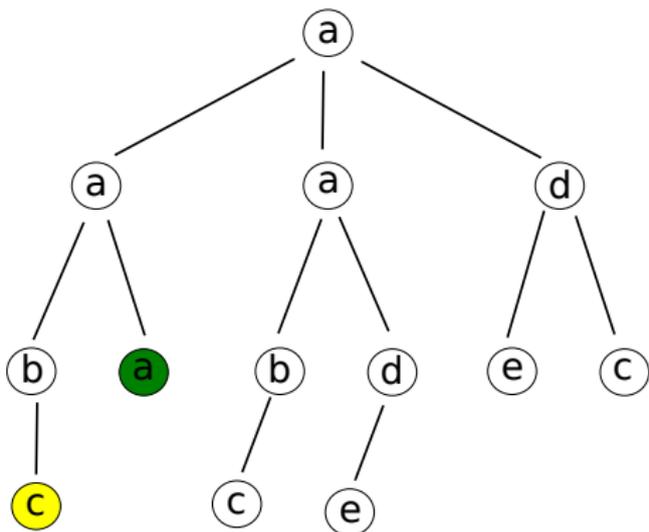
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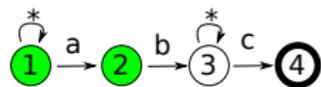
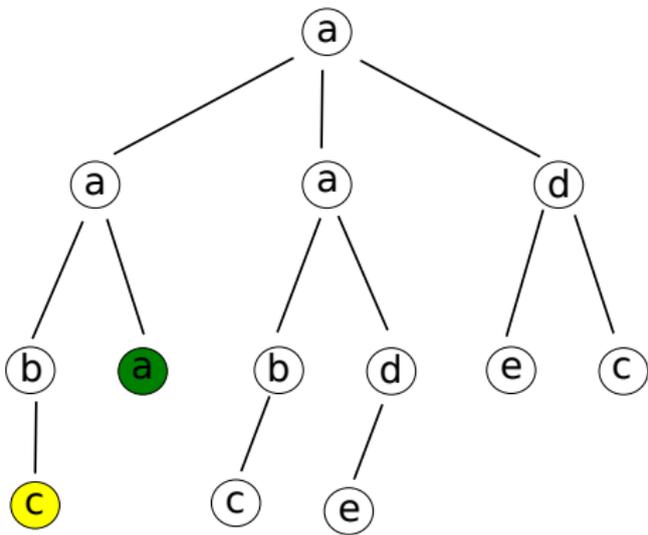
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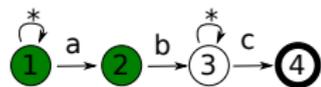
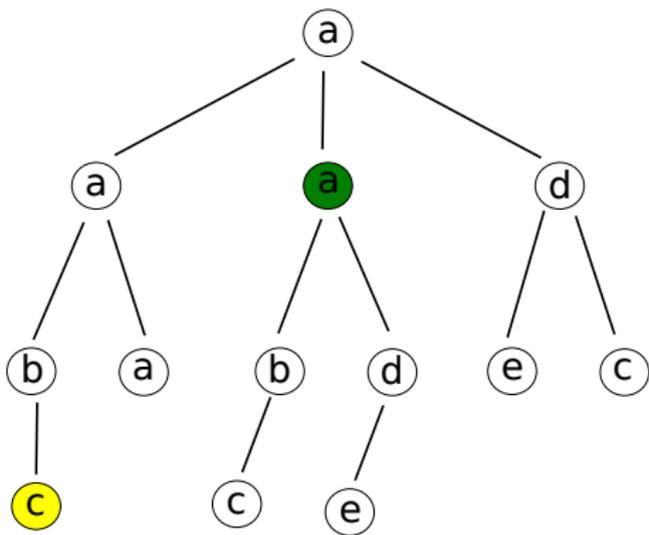
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Topdown XPath evaluation



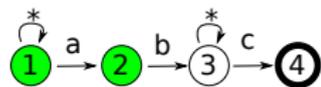
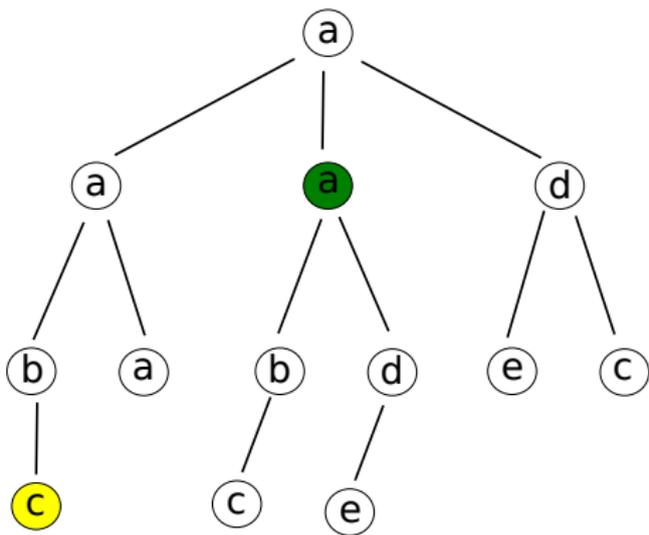
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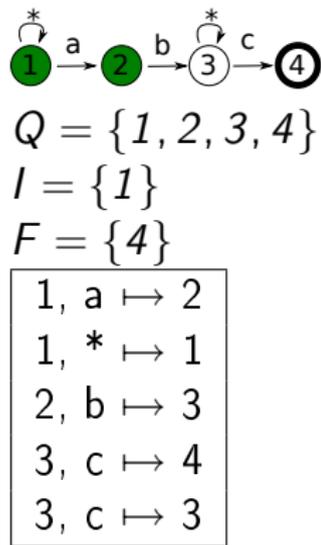
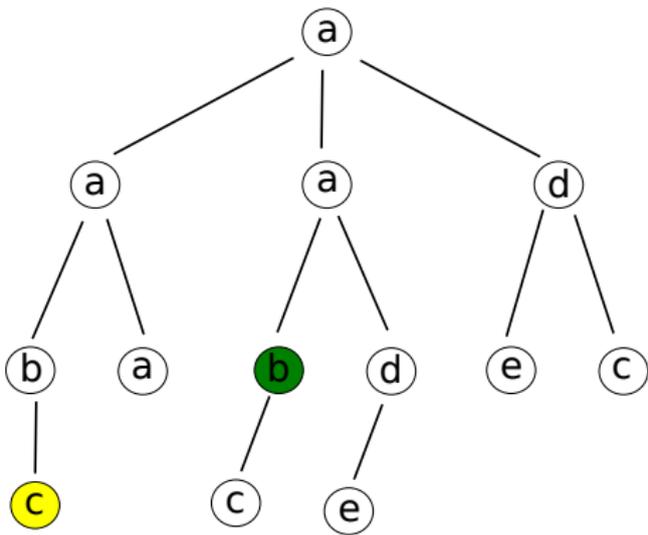
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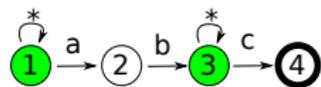
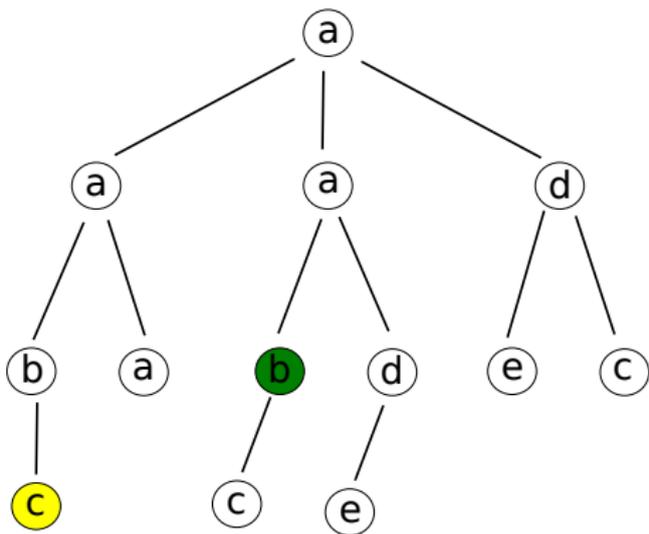
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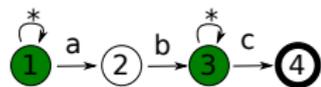
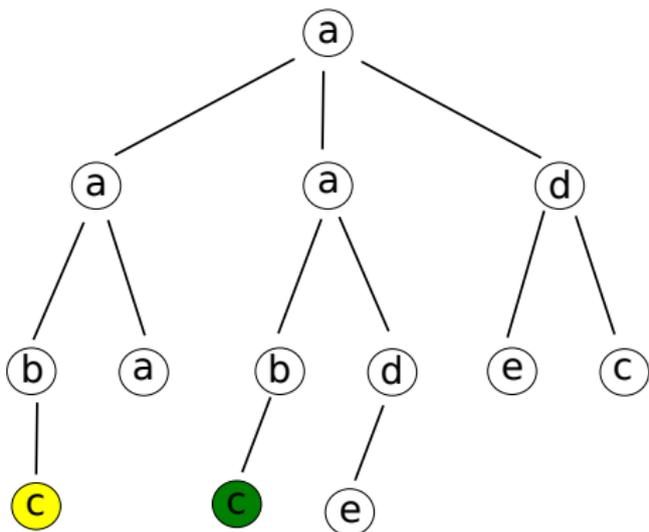
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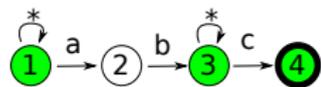
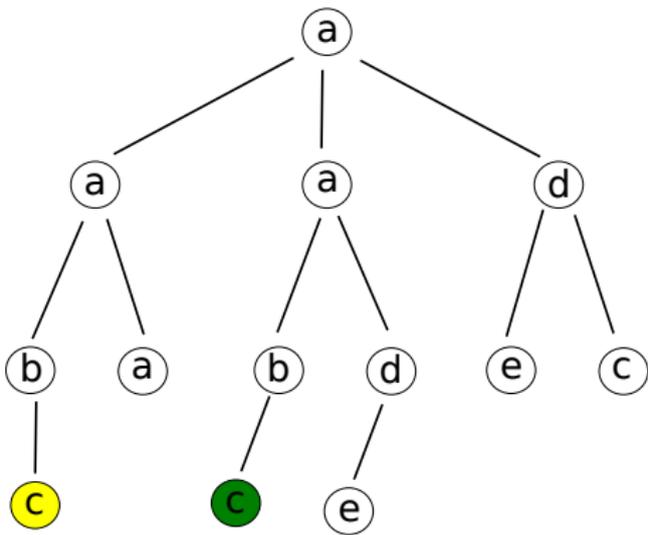
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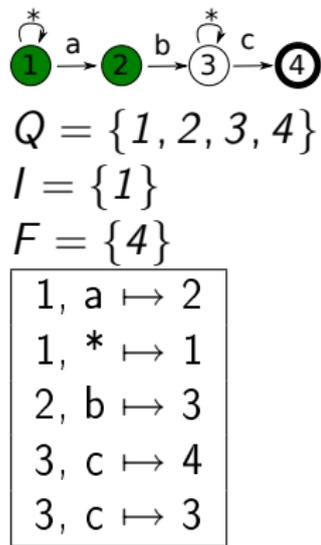
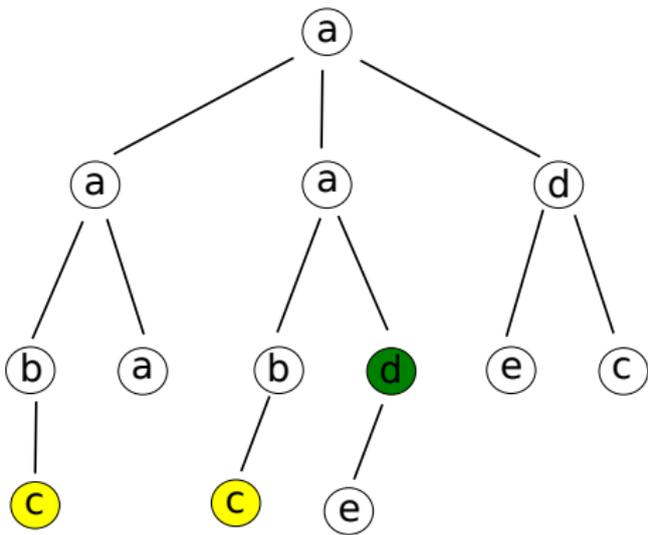
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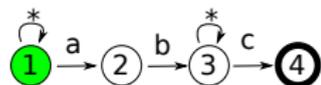
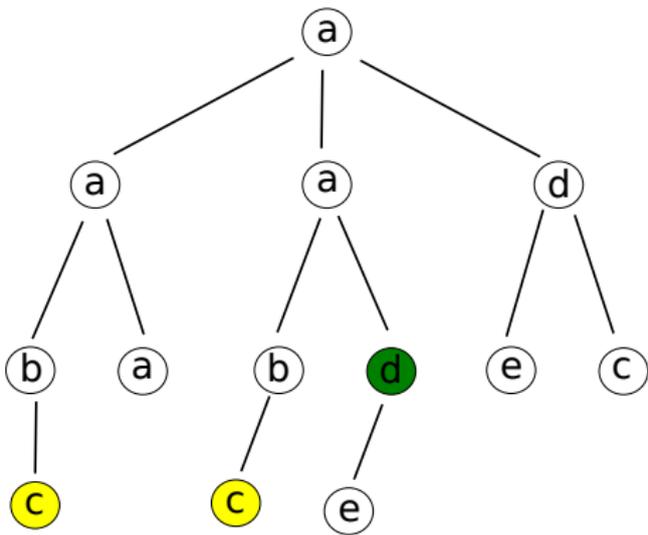
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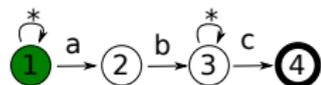
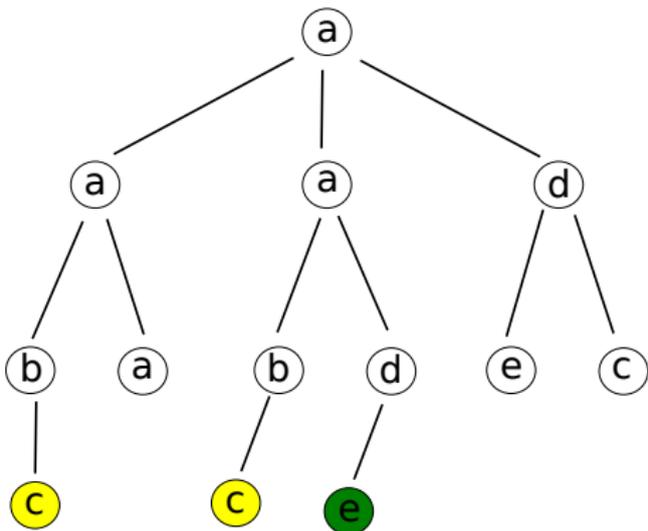
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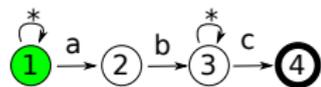
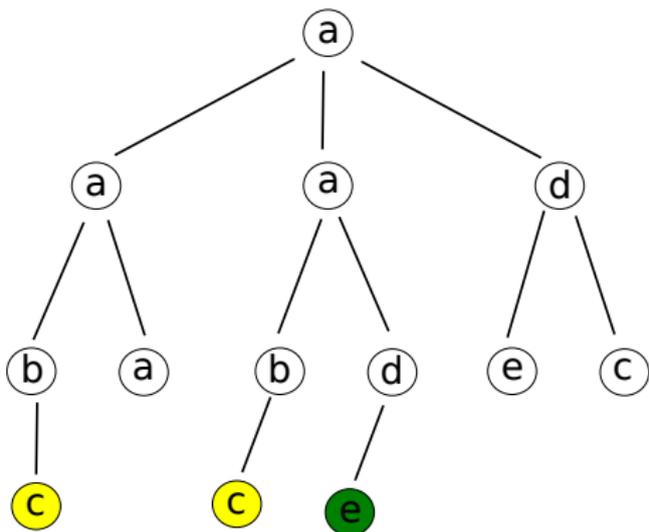
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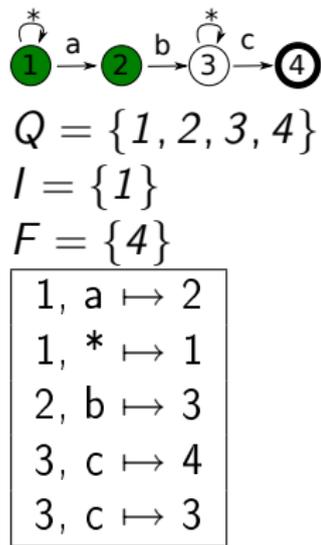
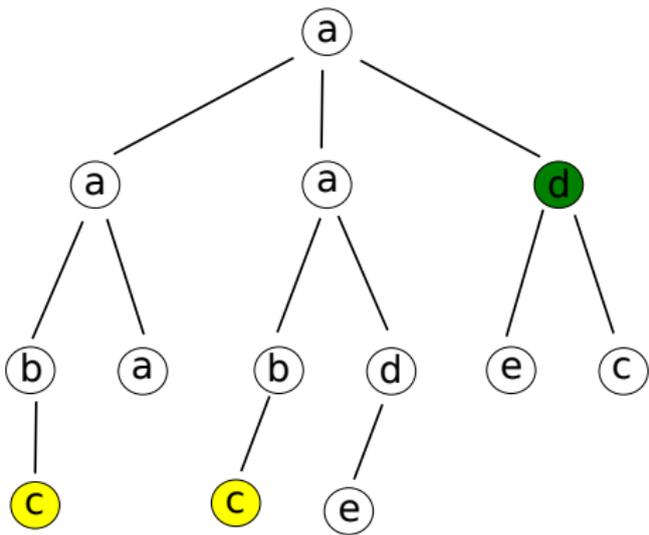
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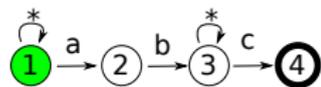
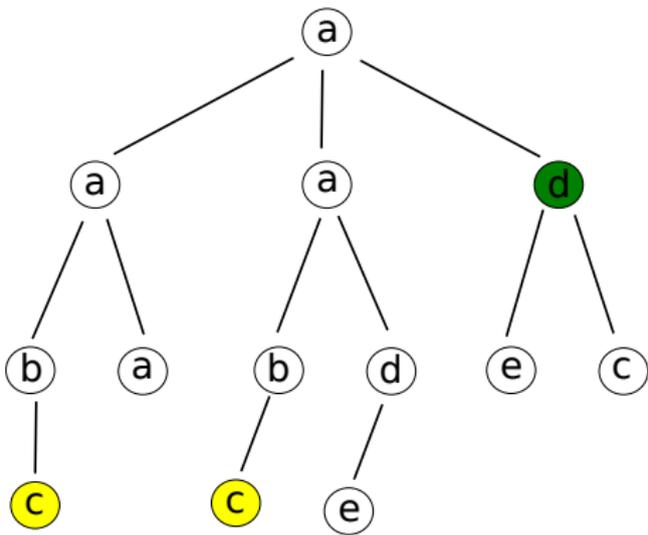
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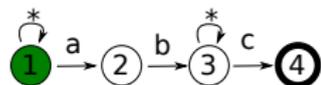
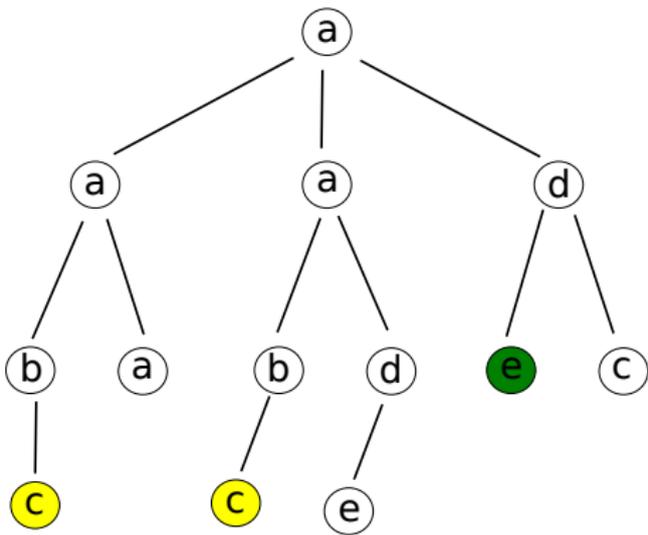
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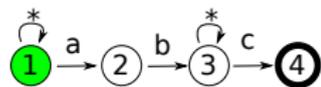
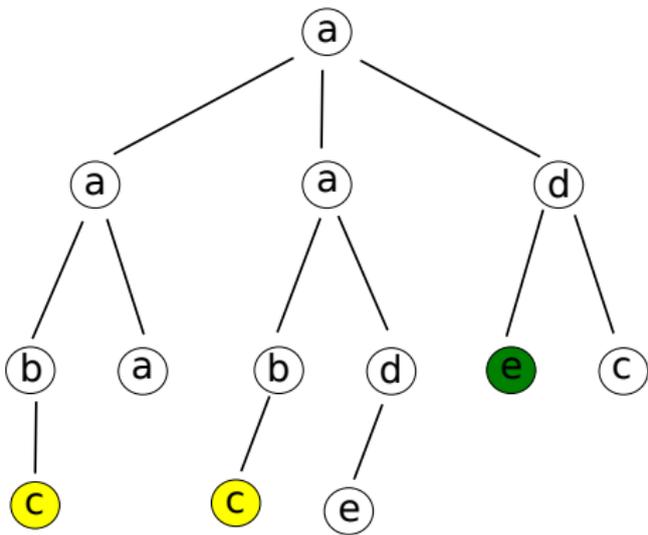
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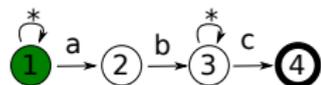
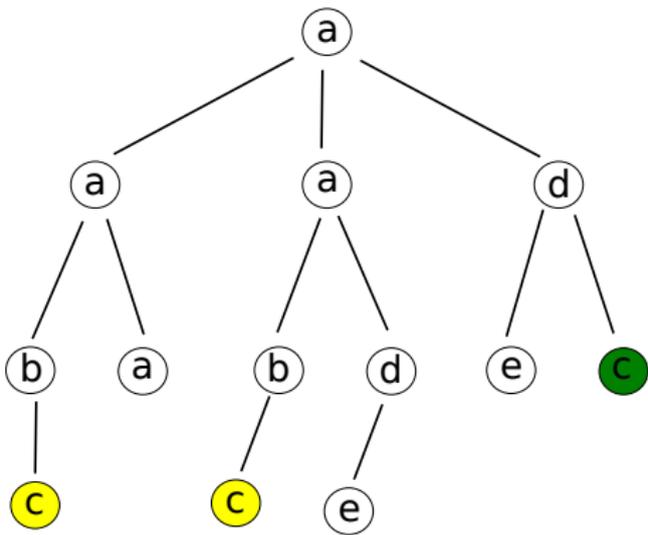
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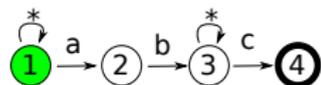
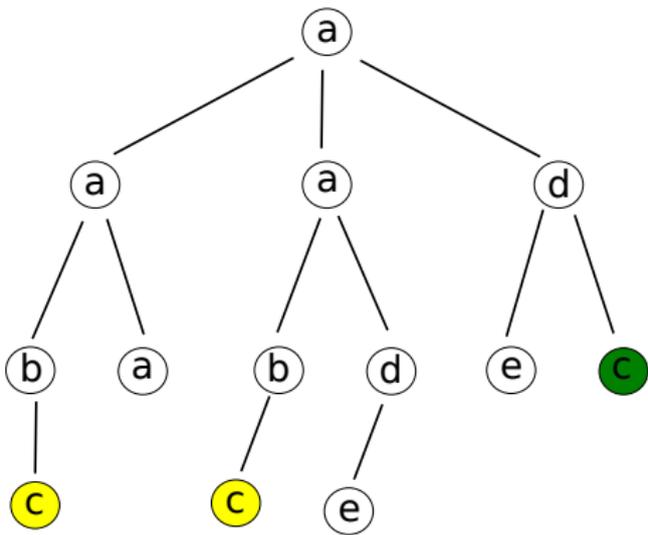
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Complexity is *combined linear time* $O(|Q| \times |D|)$, which is the best complexity for this problem (cf lecture).

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Consider:

```
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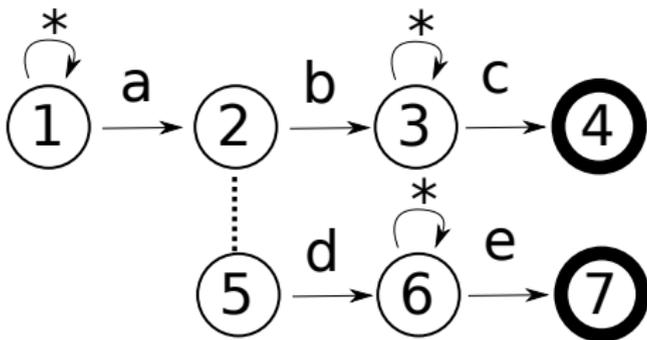
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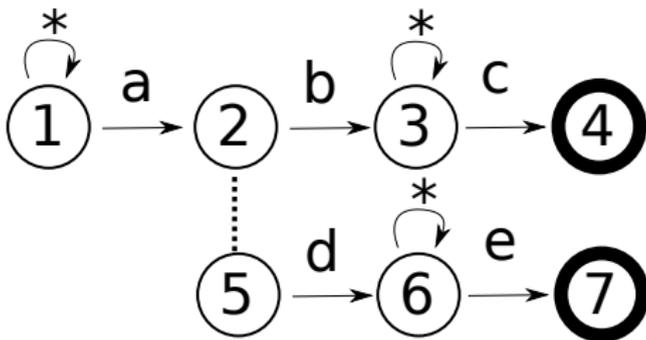
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Topdown XPath evaluation

```
NodeSet eval(Automata a, States S, Node t,
             FilterStack FS){
  if (t == null) return Empty, FS
  else {
    S' = {q' | q, l → q' ∈ a, l = label(t) or *}
    FilterSet f = {{InitState(FilterAuto(q))} | q ∈ S}
    FS' = push(f, FS);
    FS'' = EmptyStack;
    for each fs in FS' {
      fs' = Empty;
      for each (_, s) in fs
        fs' = fs' ∪ {s × {q' | q, l → q' ∈ a, l = label(t) or *}}
      push(FS'', fs');
    }
  }
}
```

...

Topdown XPath evaluation

```
r = Empty;
fs = Empty;
for each t' in children(t) {
    r', FS''' = eval(a, S', t', FS'');
    r = r ∪ r';
    fs''' = pop(FS''');
    fs'' = pop(FS'');
    for each (s, s') in fs'''
        if (finalstate(a') ⊆ s')
            remove (_, s) from fs'';
    FS'' = push(FS'', fs'');
};
```

Topdown XPath evaluation

```
fs = peek(FS");  
if (isempty(fs))  
    if (finalstate(a) ∈ S)  
        r = r ∪ {t};  
    else  
        r = Empty  
return (r, FS");
```

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