

# Outline

- 1. Recap: deterministic Reg Expr's / Glushkov Automaton
- 2. Complexity of DTD validation
- 3. Beyond DTDs: XML Schema and RELAX NG
- 4. Static Methods, based on Tree Automata

# **Previous Lecture**

### XML type definition languages

want to specify a certain subset of XML doc's = a "type" of XML documents

Remember

The specification/type definition should be simple, so that

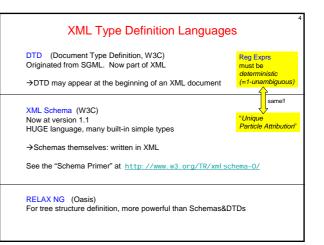
→ a validator can be built automatically (and efficiently)
→ the validator runs efficient on any XML input

(similar demands as for a parser)

→ Type def. language must be SIMPLE!

(similarly: parser generators use EBNF or smaller subclasses: LL / LR)

O(n^3) parsing



# XML Type Definition Languages

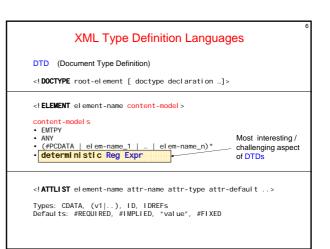
### DTD (Document Type Definition)

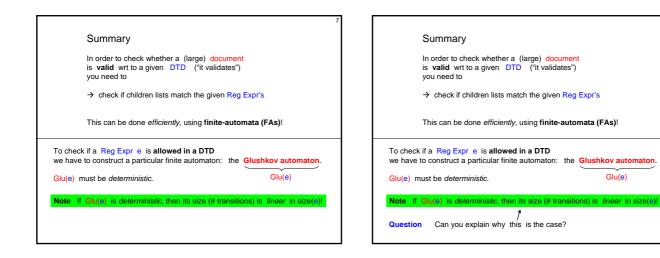
<! DOCTYPE root-element [ doctype declaration ...]>

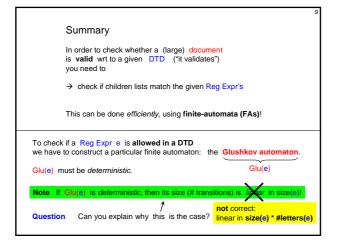
<! ELEMENT el ement-name content-model >

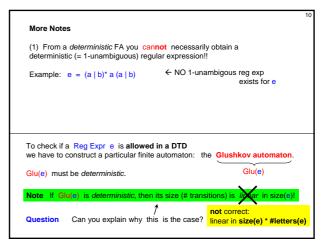
- content-models • EMTPY
- EMIFT ANY (#PCDATA | elem-name\_1 | ... | elem-name\_n)\* deterministic Reg Expr over element names

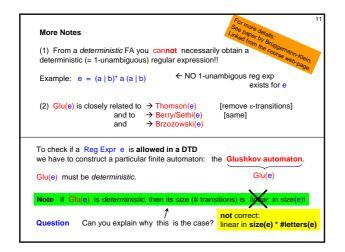
<! ATTLIST element-name attr-name attr-type attr-default ...> Types: CDATA, (v1|..), ID, IDREFs Defaults: #REQUIRED, #IMPLIED, "value", #FIXED

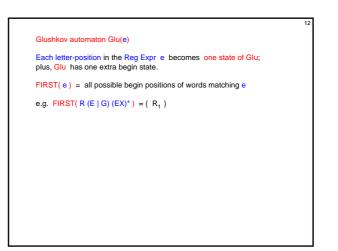




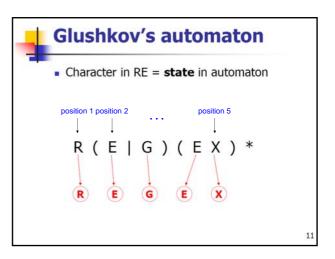


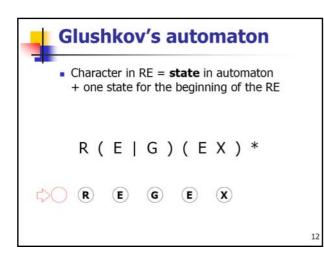


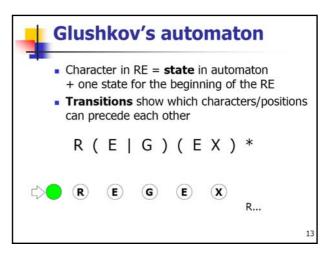


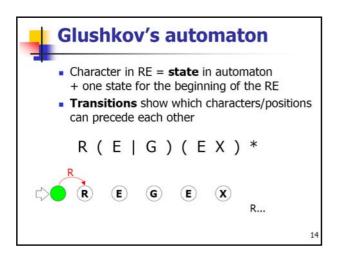


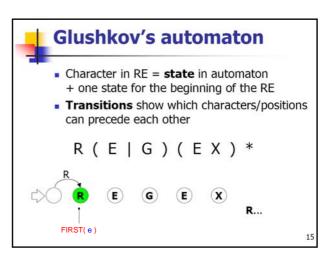


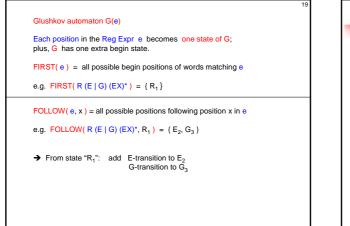


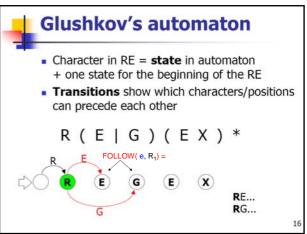


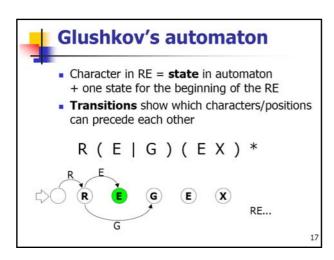


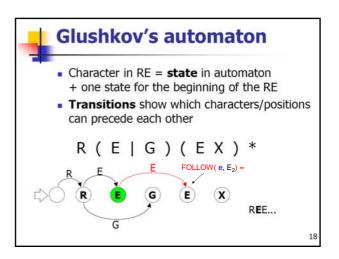


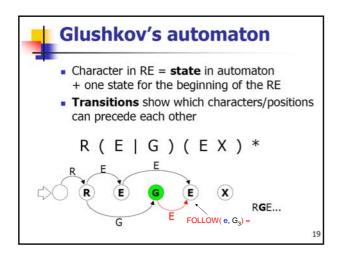


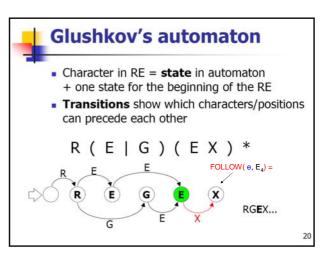


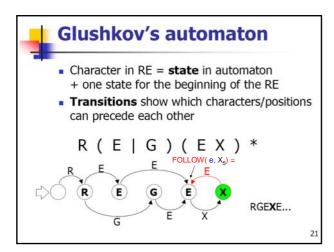


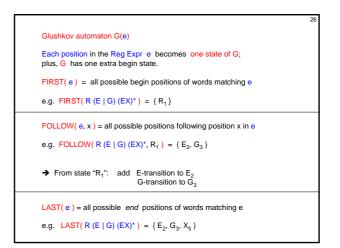


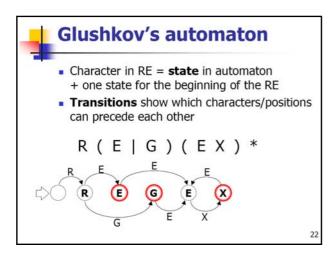


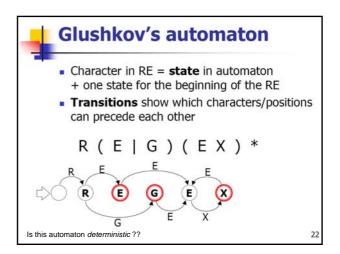


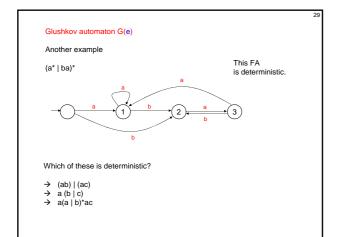


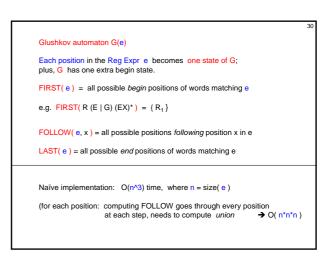






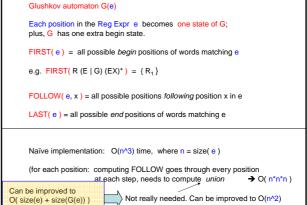


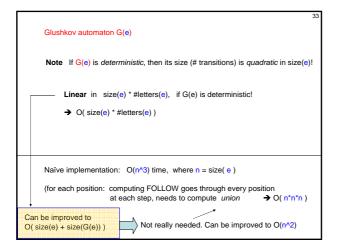


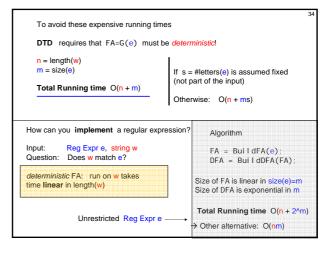


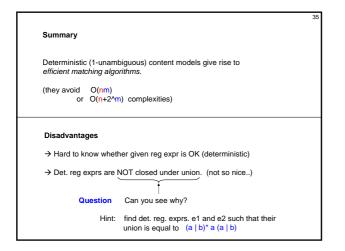
# Glushkov automaton G(e) Glushkov automaton G(e) Each position in the Reg Expr e becomes one state of G; plus, G has one extra begin state. FIRST(e) = all possible *begin* positions of words matching e e.g. FIRST(R (E | G) (EX)\*) = { R1 } FOLLOW(e, x) = all possible positions following position x in e I LAST(e) = all possible end positions of words matching e I Naïve implementation: O(n^3) time, where n = size(e) I (for each position: computing FOLLOW goes through every position at each step, needs to compute *union* $\rightarrow$ O(n\*n\*n)

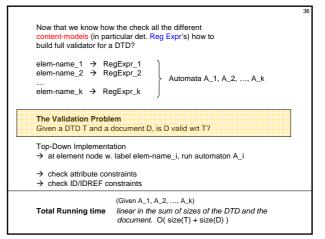
Not really needed. Can be improved to  $O(n^2)$ 

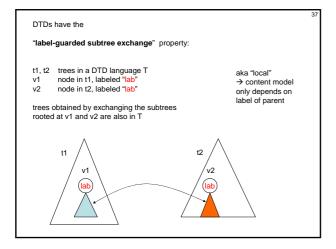


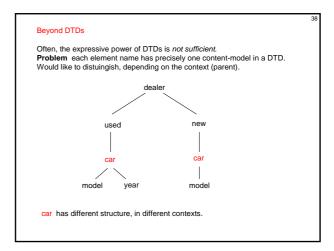


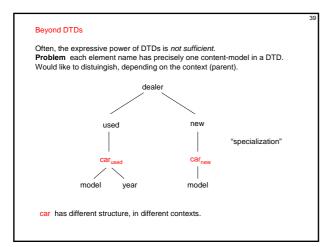


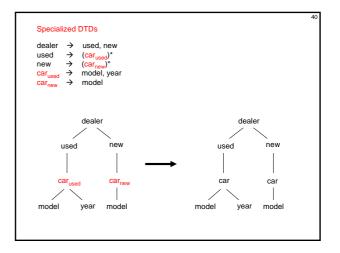


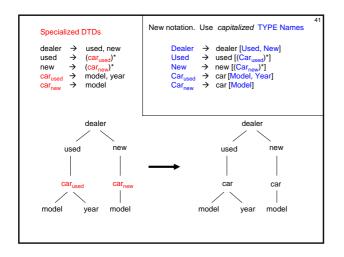


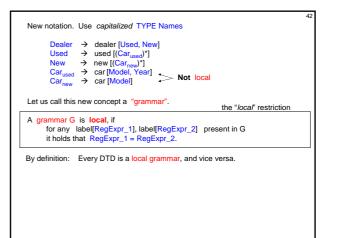


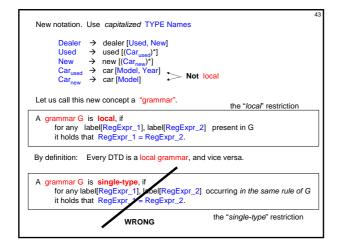


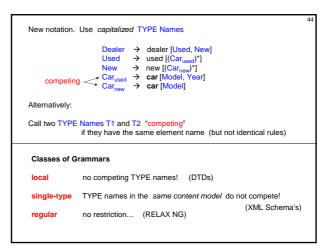






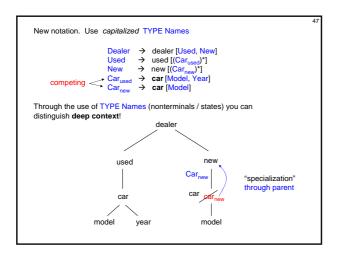


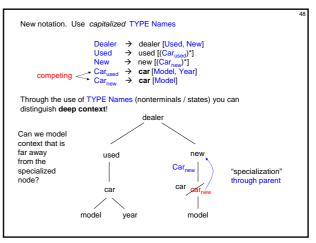


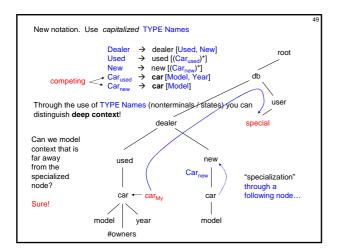


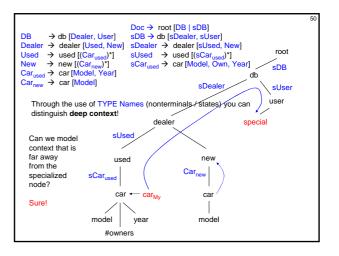
N		45
New notation.	Use capitalized TYPE Names	
competing	$\begin{array}{rcl} \text{Dealer} & \rightarrow & \text{dealer} \left[\text{Used}, \text{New}\right] \\ \text{Used} & \rightarrow & \text{used} \left[(\text{Car}_{\text{used}})^*\right] \\ \text{New} & \rightarrow & \text{new} \left[(\text{Car}_{\text{new}})^*\right] \\ \text{Car}_{\text{used}} & \rightarrow & \text{car} \left[\text{Model}, \text{Year}\right] \\ \text{Car}_{\text{new}} & \rightarrow & \text{car} \left[\text{Model}\right] \end{array}$	
Question	Are there single-type grammars (XML Schemas) which cannot be expressed by local grammars (DTDs).	
Classes of G	rammars	
local	no competing TYPE names! (DTDs)	
single-type	TYPE names in the same content model do not compete!	
regular	no restriction (RELAX NG) (XML Schema's)	

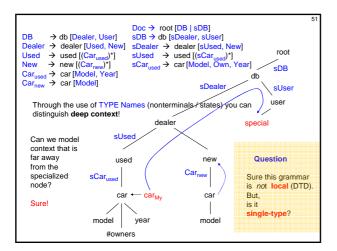
New notation.	Use capitalized TYPE Names	40
competing but are not in same content model!	Person → person [PersonName, Gender, Spouse?, Pet*] PersonName → name [First, Last] Pet → pet [Kind, PetName] PetName → name [#PCDATA] 	
Question	Are there single-type grammars (XML Schemas) which cannot be expressed by local grammars (DTDs). YES!	
Classes of G	rammars	
local	no competing TYPE names! (DTDs)	
single-type	TYPE names in the same content model do not compete!	
regular	no restriction (RELAX NG) (XML Schema's)	

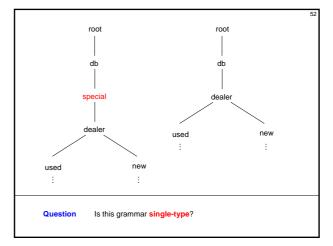


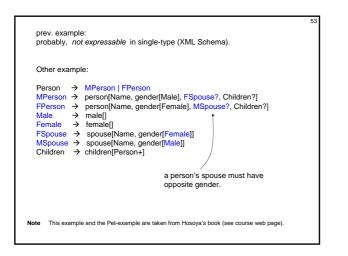


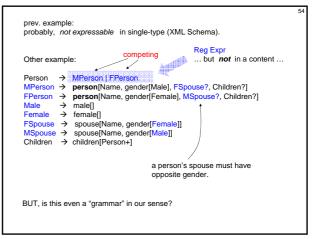


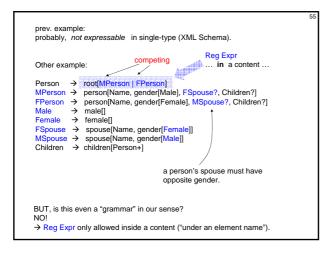


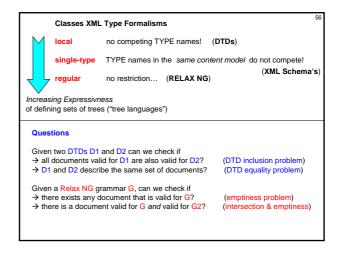


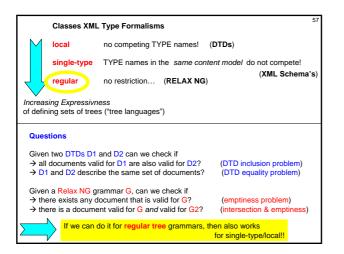


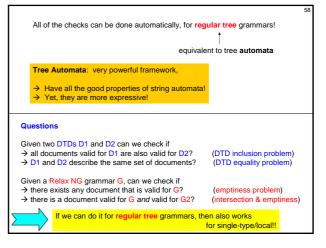




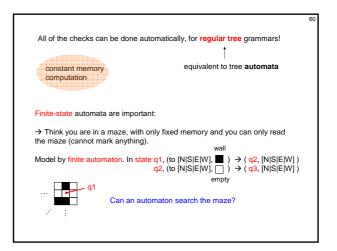


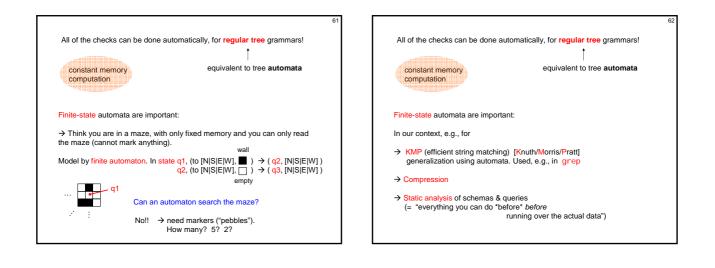


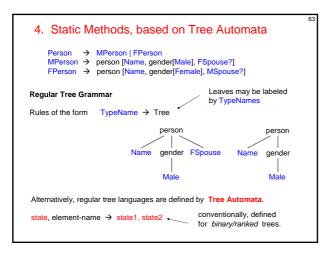


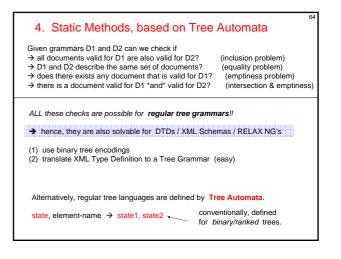


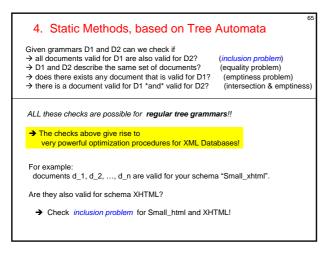
All of the checks can be	e done automatically, for regular tree grammars! equivalent to tree automata
Tree Automata: very p → Have all the good pr → Yet, they are more e	operties of string automata!
New	
	t sufficient to check DTDs / Schemas! r well-bracketed strings!
String automata are no	

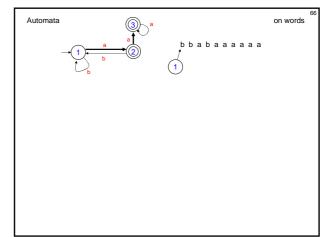


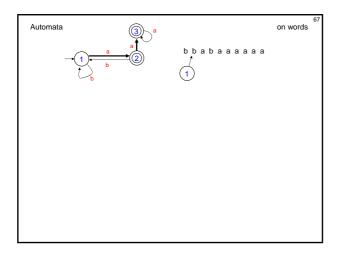


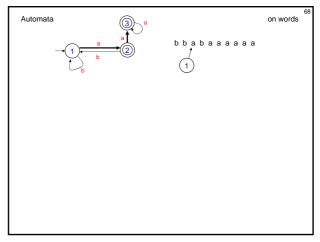


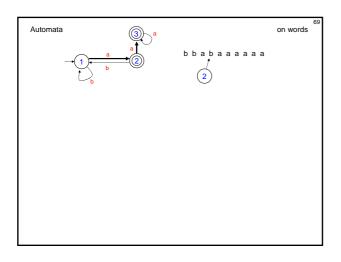


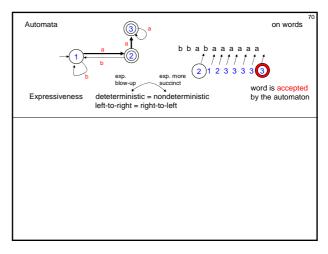


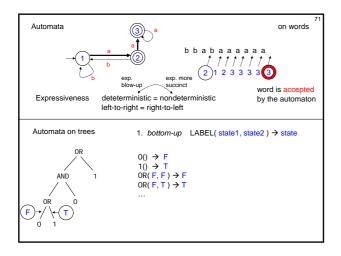


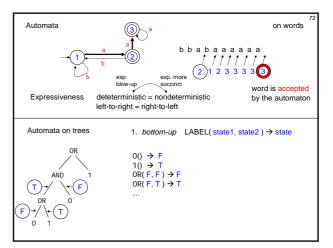


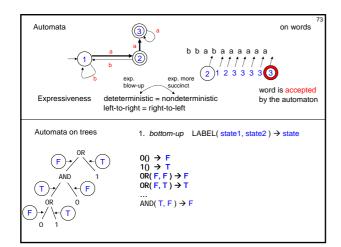


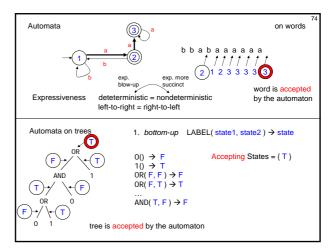


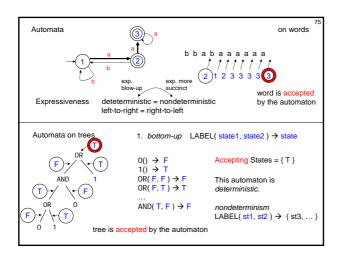


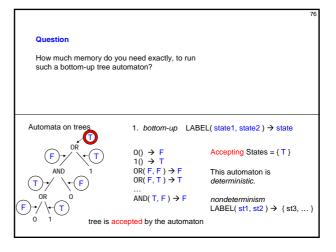


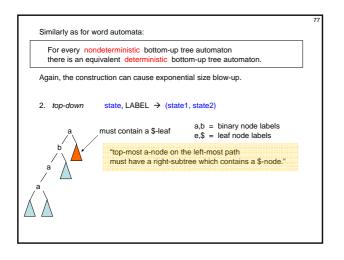


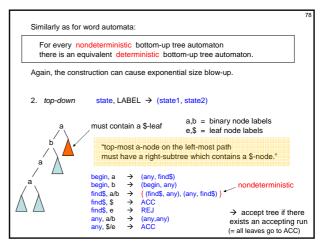


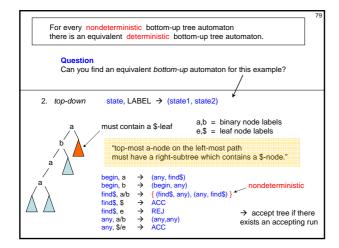


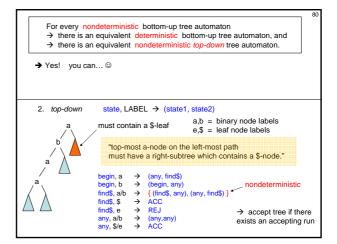


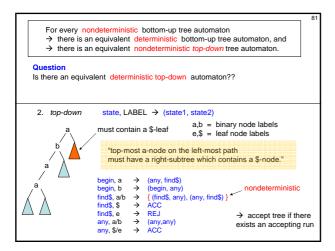


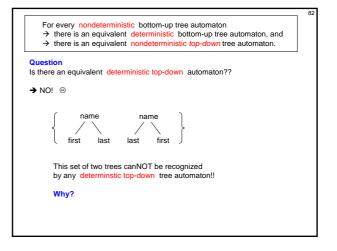


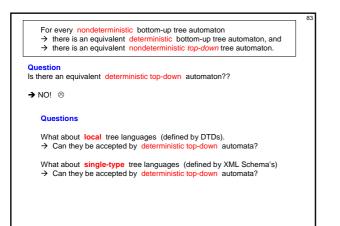


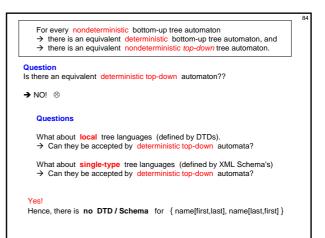












For every deterministic bottom-up tree automaton there exists a minimal unique equivalent one!

→ Equivalence is decidable

In fact, YOU have already produced minimal bottom-up tree automata!

The minimal DAG of a tree t can be seen as the minimal unique tree automaton that only accepts the tree t.

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→ Equivalence is decidable

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The minimal DAG of a tree t can be seen as the minimal unique tree automaton that only accepts the tree t.

### Question

How expensive (complexity) to find mininmal one?

→Same as for word automata?

