# COMP4161 Advanced Topics in Software Verification



C

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#### **Last Time**

- → Deep and shallow embeddings
- → Isabelle records
- → Nondeterministic State Monad with Failure
- → Monadic Weakest Precondition Rules



#### Content

→ Foundations & Principles	
<ul> <li>Intro, Lambda calculus, natural deduction</li> </ul>	[1,2]
<ul> <li>Higher Order Logic, Isar (part 1)</li> </ul>	[2,3 <sup>a</sup> ]
Term rewriting	[3,4]
→ Proof & Specification Techniques	
<ul> <li>Inductively defined sets, rule induction</li> </ul>	[4,5]
<ul> <li>Datatype induction, primitive recursion</li> </ul>	[5,7]
<ul> <li>General recursive functions, termination proofs</li> </ul>	[7]
<ul> <li>Proof automation, Isar (part 2)</li> </ul>	[8 <sup>b</sup> ]
<ul> <li>Hoare logic, proofs about programs, invariants</li> </ul>	[8,9]
<ul> <li>C verification</li> </ul>	[9,10]
<ul> <li>Practice, questions, exam prep</li> </ul>	[10 <sup>c</sup> ]



<sup>&</sup>lt;sup>a</sup>a1 due; <sup>b</sup>a2 due; <sup>c</sup>a3 due

### wp

apply (wp extra\_wp\_rules)

Tactic for automatic application of weakest precondition rules

- → Developed for the seL4 verification proofs
- → Knows about a huge collection of existing wp rules for monads
- → Works best when precondition is a schematic variable
- → related tool: wpc for Hoare reasoning over case statements

When used with **AutoCorres**, allows automated reasoning about C programs.

Today we will learn about AutoCorres and C verification.



# DEMO

INTRODUCTION TO AUTOCORRES AND WP

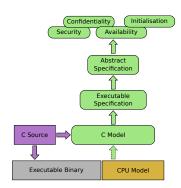
## Some Context: The L4.verified Project

The seL4 microkernel was verified functionally correct using Isabelle/HOL.

- Project by "NICTA" @ UNSW.
- One of the largest proof projects, Isabelle projects, etc.

Initial proof (completed 2009).

- 3 encodings of seL4 in Isabelle.
- 2 proofs of simulation/refinement.
  - Involve corres & ccorres.



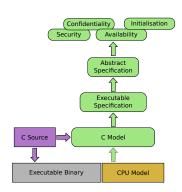


## Relating L4.verified to Best Practice

The L4.verified project is a bit specialised, but some of these concepts are universal:

- abstract spec: describes the system as seen by an external party.
- executable spec: describes the algorithms of the system somewhat abstractly.
- implementation: ground model: encodes the semantics of the real system in detail.

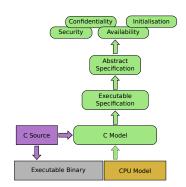
Think about a binary search tree. Where would its invariants go?



#### The AutoCorres Idea

#### The big idea of the AutoCorres project:

 Can we handle one layer automatically?



## A BRIEF OVERVIEW OF C AND SIMPL

#### Main new problems in verifying C programs:

- expressions with side effects
- → more control flow (do/while, for, break, continue, return)
- → local variables and blocks
- → functions & procedures
- → concrete C data types
- → C memory model and C pointers

C is not a nice language for reasoning.

Things are going to get ugly.

AutoCorres will help.

## C Parser: translates C into Simpl

**Simpl:** deeply embedded imperative language in Isabelle.

- → generic imperative language by Norbert Schirmer, TU Munich
- → state space and basic expressions/statements can be instantiated
- → has operational semantics
- → has its own Hoare logic with soundness and completeness proof, plus automated vcg

#### **C Parser:** parses C, produces Simpl definitions in Isabelle

- → written by Michael Norrish, NICTA and ANU
- → Handles a non-trivial subset of C
- → Originally written to verify seL4's C implementation
- → AutoCorres is built on top of the C Parser



## **Commands in Simpl**

```
datatype ('s, 'p, 'f) com =
    Skip
    Basic "'s ⇒ 's"
    Spec "('s * 's) set"
    Seq "('s, 'p, 'f) com" "('s, 'p, 'f) com"
    Cond "'s set" "('s, 'p, 'f) com" "('s, 'p, 'f) com"
    While "'s set" "('s, 'p, 'f) com"
    Call 'p
    DynCom "'s ⇒ ('s, 'p, 'f) com"
    Guard 'f "'s set" "('s, 'p, 'f) com"
    Throw
    Catch "('s, 'p, 'f) com" "('s, 'p, 'f) com"
```

's = state, 'p = procedure names, 'f = faults



## **Expressions with side effects**

```
a = a * b; x = f(h); i = ++i - i++; x = f(h) + g(x);
```

- → a = a \* b Fine: easy to translate into Isabelle
- $\rightarrow$  x = f(h) Fine: may have side effects, but can be translated sanely.
- → i = ++i i++ Seriously? What does that even mean? Make this an error, force programmer to write instead:
  - i0 = i; i++; i = i i0; (or just i = 1)
- → x = f(h) + g(x) Ok if g and h do not have any side effects ⇒ Prove all functions in expressions are side-effect free
  - Trove all functions in expressions are side-effect free

#### Alternative:

Explicitly model nondeterministic order of execution in expressions.



#### Control flow

```
do { c } while (condition);
automatically translates into:
                  c; while (condition) { c }
Similarly:
            for (init; condition; increment) { c }
becomes
           init; while (condition) { c; increment; }
```

## More control flow: break/continue

```
while (condition) {
   foo;
   if (Q) continue;
   bar;
   if (P) break;
}
```

Non-local control flow: **continue** goes to condition, **break** goes to end.

Can be modelled with exceptions:

- → throw exception 'continue', catch at end of body.
- → throw exception 'break', catch after loop.



#### Break/continue

#### Break/continue example becomes:

```
try {
    while (condition) {
        try {
            foo;
            if (Q) { exception = 'continue'; throw; }
            bar;
            if (P) { exception = 'break'; throw; }
        } catch { if (exception == 'continue') SKIP else throw; }
}
catch { if (exception == 'break') SKIP else throw; }
```

#### This is not C any more. But it models C behaviour!

Need to be careful that only the translation has access to exception state.



#### Return

```
if (P) return x;
foo;
return y;
```

Similar non-local control flow. Similar solution: use throw/try/catch

```
try {
    if (P) { return_val = x; exception = 'return'; throw; }
    foo;
    return_val = y; exception = 'return'; throw;
} catch {
    SKIP
}
```

# **AUTOCORRES**

#### **AutoCorres**

AutoCorres: reduces the pain in reasoning about C code

- → Written by David Greenaway, NICTA and UNSW
- → Converts C/Simpl into (monadic) shallow embedding in Isabelle
- → Shallow embedding easier to reason about than Simpl

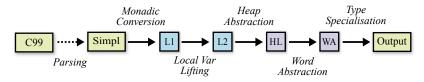
**Is self-certifying:** produces Isabelle theorems proving its own correctness

For each Simpl definition *C* and its generated shallow embedding *A*:

- → AutoCorres proves an Isabelle theorem stating that *C* refines *A*
- → Every behaviour of C has a corresponding behaviour of A
- → Refinement guarantees that properties proved about A will also hold for C.
- → (Provided that A never fails. c.f. Total Correctness)



#### **AutoCorres Process**



L1: initial monadic shallow embedding

**L2:** local variables introduced by  $\lambda$ -bindings

HL: heap state abstracted into a set of typed heaps

WA: machine words abstracted to idealised integers or nats

Output: human-readable output with type strengthening, polish

## On-the-fly proof:

Simpl refines L1 refines L2 refines HL refines WA refines Output



## Example: C99

We will use the following example program to illustrate each of the phases.

```
unsigned some_func(unsigned *a, unsigned *b, unsigned c) {
  unsigned *p = NULL;

if (c > 10u){
   p = a;
} else {
   p = b;
}

return *p;
}
```

## **Example: Simpl**

```
some_func_body =
TRY

'p :== ptr_coerce (Ptr (scast 0));
IF 0xA < 'c THEN
    'p :== 'a
ELSE
    'p :== 'b
FI;;
Guard C_Guard {c_guard 'p}
    (creturn global_exn_var_'_update ret__unsigned_'_update
        (\lambda s. h_val (hrs_mem (t_hrs_' (globals s))) (p_' s)));;
Guard DontReach {} SKIP</pre>
CATCH SKIP END
```

## Example: L1 (monadic shallow embedding)

State type is the same as Simpl, namely a record with fields:

- → globals: heap and type information
- → a\_', b\_', c\_', p\_' (parameters and local variables)
- → ret\_unsigned\_', global\_exn\_var\_' (return value, exception type)



## **Example: L2 (local variables lifted)**

```
\label{eq:local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_
```

#### State is a record with just the **globals** field

- → function now takes its parameters as arguments
- → local variable **p** now passed via  $\lambda$ -binding
- → L2\_gets annotated with local variable names
- → This ensures preservation by later AutoCorres phases



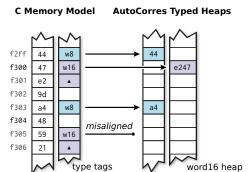
## **Example: HL (heap abstracted into typed heaps)**

State is a record with a set of **is\_valid\_** and **heap\_** fields:

- → These store pointer validity and heap contents respectively, per type
- → above example has only 32-bit word pointers



## **Heap Abstraction**



#### C Memory Model: by Harvey Tuch

heap values

→ **Heap** is a mapping from 32-bit addresses to bytes: 32 word  $\Rightarrow$  8 word

word8 heap

→ Heap Type Description stores type information for each heap location



## **Example: WA (words abstracted to ints and nats)**

## Word abstraction: C int $\rightarrow$ Isabelle int, C unsigned $\rightarrow$ Isabelle nat

- → Guards inserted to ensure absence of unsigned underflow and overflow
- → Signed under/overflow already has guards (it has undefined behaviour)

#### In the example, the **unsigned** argument **c** is now of type **nat**

- → The function also returns a nat result
- → The heap is not abstracted, hence the call to unat



## Example: Output (type strengthening and polish)

#### Type Strengthening:

- → Tries to convert output to a more restricted monad
- → The above is in the option monad because it doesn't modify the state, but might fail
- → The type of the option monad implies it cannot modify state

#### Polish:

- → Simplify output as much as possible
- → The condition has been rewritten to a return because the condition 10 < c doesn't depend on the state</p>



## **Type Strengthening**

#### Example:

```
unsigned zero(void){ return Ou; }
```

Monad Type	Kind	Туре	Example
pure	Pure function	'a	0
gets	Read-only, non-failing	$s \Rightarrow a$	$\lambda$ s. 0
option	Read-only function	$s \Rightarrow a$ option	oreturn 0

Effect information now encoded in function types

Later proofs get this information for free!

Can be controlled by the **ts\_force** option of AutoCorres



## (Reader) Option Monad

Another standard monad, familiar from e.g. Haskell

Return:

oreturn 
$$x \equiv \lambda s$$
. Some  $x$ 

Bind:

obind  $a b \equiv \lambda s$ . case a s of None  $\Rightarrow$  None | Some  $r \Rightarrow b r s$ 

→ Infix notation: |>>>

→ Do notation: DO ... OD

**Hoare Logic:** 

ovalid 
$$P f Q \equiv \forall s r. P s \land f s = \text{Some } r \longrightarrow Q r s$$

ovalid 
$$(P x)$$
 (oreturn  $x$ )  $P$  
$$\frac{\bigwedge r. \text{ ovalid } (R r) \ (g r) \ Q \quad \text{ovalid } P f R}{\text{ovalid } P \ (f \mid \gg g) \ Q}$$

## **Exception Monad**

**Exceptions** used to model early return, break and continue.

**Exception Monad**:  $\dot{s} \Rightarrow ((\dot{e} + \dot{a}) \times \dot{s}) \text{ set } \times \text{ bool }$ 

- → Instance of the nondeterministic state monad: return-value type is sum type 'e + 'a
- → Sum Type Constructors: InI ::  $\dot{e} \Rightarrow \dot{e} + \dot{a}$  Inr ::  $\dot{a} \Rightarrow \dot{e} + \dot{a}$
- → Convention: Inl used for exceptions, Inr used for ordinary return-values

## **Basic Monadic Operations**

```
returnOk x \equiv \text{return (Inr } x) throwError e \equiv \text{return (Inl } e) lift b \equiv (\lambda x. \text{ case } x \text{ of Inl } e \Rightarrow \text{throwError } e \mid \text{Inr } r \Rightarrow b r)
```

**bindE:**  $a \gg = E b \equiv a \gg = (lift b)$  **Do notation:** doE ... odE



## **Hoare Rules for Exceptions**

New kind of Hoare triples to model normal and exceptional cases:

#### **Weakest Precondition Rules:**

## Today we have seen

- → The automated proof method wp
- → The C Parser and translating C into Simpl
- → AutoCorres and translating Simpl into monadic form
- → The option and exception monads

