

COMP4161: Advanced Topics in Software Verification

C

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Last Time



- → Deep and shallow embeddings
- → Isabelle records
- → Nondeterministic State Monad with Failure
- → Monadic Weakest Predondition Rules

Content



- → Intro & motivation, getting started
- → Foundations & Principles

 Lambda Calculus, natural deduction 	[1,2]
 Higher Order Logic 	[3 ^a]
 Term rewriting 	[4]

→ Proof & Specification Techniques

 Inductively defined sets, rule induction 	[5]
 Datatypes, recursion, induction 	[6, 7]
 Hoare logic, proofs about programs, C verification 	$[8^{b}, 9]$

• (mid-semester break)

• Writing Automated Proof Methods [10]

• Isar, codegen, typeclasses, locales [11^c,12]

^aa1 due; ^ba2 due; ^ca3 due

wp



apply (wp extra_wp_rules)

Tactic for automatic application of weakest precondition rules

- → Originally developed by Thomas Sewell, NICTA, for the seL4 proofs
- → Knows about a huge collection of existing wp rules for monads
- → Works best when precondition is a schematic variable
- → related tool: wpc for Hoare reasoning over case statements

When used with **AutoCorres**, allows automated reasoning about C programs.

Today we will learn about AutoCorres and C verification.



Demo

Introduction to AutoCorres and wp



A Brief Overview of C and Simpl

C



Main new problems in verifying C programs:

- → expressions with side effects
- → more control flow (do/while, for, break, continue, return)
- → local variables and blocks
- → functions & procedures
- → concrete C data types
- → C memory model and C pointers

C is not a nice language for reasoning.

Things are going to get ugly.

AutoCorres will help, later.

C Parser: translates C into Simpl



Simpl: deeply embedded imperative language in Isabelle.

- → generic imperative language by Norbert Schirmer, TU Munich
- → state space and basic expressions/statements can be instantiated
- → has operational semantics
- → has its own Hoare logic with soundness and completeness proof, plus automated vcg

C Parser: parses C, produces Simpl definitions in Isabelle

- → written by Michael Norrish, NICTA and ANU
- → Handles a non-trivial subset of C
- → Originally written to verify seL4's C implementation
- → AutoCorres is built on top of the C Parser

Commands in Simpl



's = state, 'p = procedure names, 'f = faults

Expressions with side effects

```
DATA x = f(h) +
```

```
a = a * b; x = f(h); i = ++i - i++; x = f(h)
```

- \rightarrow a = a * b Fine: easy to translate into Isabelle
- → x = f(h) Fine: may have side effects, but can be translated sanely.
- → i = ++i i++ Seriously? What does that even mean? Make this an error, force programmer to write instead:
 - i0 = i; i++; i = i i0; (or just i = 1)
- \Rightarrow x = f(h) + g(x) Ok if g and h do not have any side effects \implies Prove all functions in expressions are side-effect free

Alternative:

Explicitly model nondeterministic order of execution in expressions.

Control flow



```
do { c } while (condition);
```

Already can treat normal while-loops! Automatically translate into:

More control flow: break/continue



```
while (condition) {
   foo;
   if (Q) continue;
   bar;
   if (P) break;
}
```

Non-local control flow: **continue** goes to condition, **break** goes to end.

Can be modelled with exceptions:

- → throw exception 'continue', catch at end of body.
- → throw exception 'break', catch after loop.

Break/continue



Break/continue example becomes:

```
try {
    while (condition) {
        try {
            foo;
            if (Q) { exception = 'continue'; throw; }
            bar;
            if (P) { exception = 'break'; throw; }
        } catch { if (exception == 'continue') SKIP else throw; }
} catch { if (exception == 'break') SKIP else throw; }
```

This is not C any more. But it models C behaviour!

Need to be careful that only the translation has access to exception state.

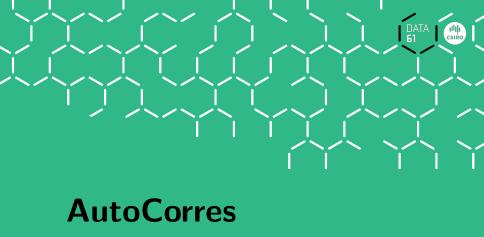
Return



```
if (P) return x;
foo;
return y;
```

Similar non-local control flow. **Similar solution:** use throw/try/catch

```
try {
    if (P) { return_val = x; exception = 'return'; throw; }
    foo;
    return_val = y; exception = 'return'; throw;
} catch {
    SKIP
}
```



AutoCorres

AutoCorres: reduces the pain in reasoning about C code



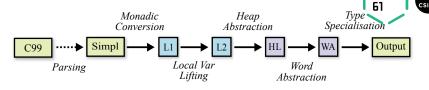
- → Written by David Greenaway, NICTA and UNSW
- → Converts C/Simpl into (monadic) shallow embedding in Isabelle
- → Shallow embedding easier to reason about than Simpl

Is self-certifying: produces Isabelle theorems proving its own correctness

For each Simpl definition C and its generated shallow embedding A:

- → AutoCorres proves an Isabelle theorem stating that *C* refines *A*
- → Every behaviour of C has a corresponding behaviour of A
- → Refinement guarantees that properties proved about A will also hold for C.
- → (Provided that A never fails. c.f. Total Correctness)

AutoCorres Process



L1: initial monadic shallow embedding

L2: local variables introduced by λ -bindings

HL: heap state abstracted into a set of **typed heaps**

WA: machine words abstracted to idealised integers or nats

Output: human-readable output with type strengthening, polish

On-the-fly proof:

Simpl refines L1 refines L2 refines HL refines WA refines Output

Example: C99

DATA | 1411 csiko

We will use the following example program to illustrate each of the phases.

```
unsigned some_func(unsigned *a, unsigned *b, unsigned
unsigned *p = NULL;

if (c > 10u){
   p = a;
} else {
   p = b;
}

return *p;
```

Example: Simpl



Example: L1 (monadic shallow embedding)



State type is the same as Simpl, namely a record with fields:

- → globals: heap and type information
- → a_', b_', c_', p_' (parameters and local variables)
- → ret_unsigned_', global_exn_var_' (return value, exception type)

Example: L2 (local variables lifted)



State is a record with just the **globals** field

- → function now takes its parameters as arguments
- \rightarrow local variable **p** now passed via λ -binding
- → L2_gets annotated with local variable names
- → This ensures preservation by later AutoCorres phases

Example: HL (heap abstracted into typed heaps)



State is a record with a set of **is_valid_** and **heap_** fields:

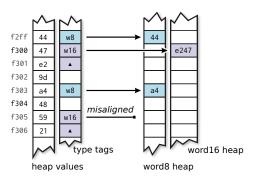
- → These store **pointer validity** and **heap contents** respectively, per type
- → above example has only 32-bit word pointers

Heap Abstraction

C Memory Model

AutoCorres Typed Heaps





C Memory Model: by Harvey Tuch

- → Heap is a mapping from 32-bit addresses to bytes: 32 word ⇒ 8 word
- → **Heap Type Description** stores type information for each heap location

Example: WA (words abstracted to ints and nats)



Word abstraction: C int \rightarrow Isabelle int, C unsigned \rightarrow Isabelle nat

- → Guards inserted to ensure absence of unsigned underflow and overflow
- → Signed under/overflow already has guards, because is undefined behaviour

In the example, the **unsigned** argument c is now of type nat

→ The function also returns a nat result

Example: Output (type strengthening and polish)



```
some_func' a b c \equiv DO p \leftarrow oreturn (if 10 < c then a else b); oguard (\lambdas. is_valid_w32 s p); ogets (\lambdas. unat (heap_w32 s p)) OD
```

Type Strengthening:

- → Tries to convert output to a more restricted monad
- → The above is in the **option** monad because it doesn't modify the state, but might fail
- → The **type** of the option monad implies it cannot modify state

Polish:

- → Simplify output as much as possible
- ightharpoonup The condition has been rewritten to a return because the condition 10 < c doesn't depend on the state

Type Strengthening





unsigned zero(void){ return Ou; }

Monad Type	Kind	Туре	Example
pure	Pure function	'a	0
gets	Read-only, non-failing	's ⇒ 'a	λ s. 0
option	Read-only function	$s \Rightarrow a \text{ option}$	oreturn 0

Effect information now encoded in function types

Later proofs get this information for free!

Can be controlled by the ts_force option of AutoCorres

Option Monad



Another standard monad, familiar from e.g. Haskell

Return:

oreturn
$$x \equiv \lambda s$$
. Some x

Bind:

obind $a \ b \equiv \lambda s$. case $a \ s$ of None \Rightarrow None | Some $r \Rightarrow b \ r \ s$

→ Infix notation: |>>>

→ **Do notation:** DO ... OD

Hoare Logic:

ovalid
$$P f Q \equiv \forall s r. P s \land f s = Some r \longrightarrow Q r s$$

Exception Monad

DATA | IIII csiro

Exceptions used to model early return, break and continue.

Exception Monad:
$$s \Rightarrow ((e + a) \times s) \text{ set } \times \text{ bool}$$

- → Instance of the nondeterministic state monad: return-value type is sum type 'e + 'a
- → Sum Type Constructors: InI :: $'e \Rightarrow 'e + 'a$ Inr :: $'a \Rightarrow 'e + 'a$
- → Convention: Inl used for exceptions, Inr used for ordinary return-values

Basic Monadic Operations

returnOk
$$x \equiv \text{return (Inr } x)$$
 throwError $e \equiv \text{return (Inl } e)$
lift $b \equiv (\lambda x. \text{ case } x \text{ of Inl } e \Rightarrow \text{throwError } e \mid \text{Inr } r \Rightarrow b r)$

bindE: $a \gg = E$ $b \equiv a \gg = (lift b)$ **Do notation:** doE ... odE

Hoare Rules for Exceptions

New kind of Hoare triples to model normal and exceptional cases:

Weakest Precondition Rules:

$$\overline{\{P x\}} \text{ returnOk } x \{P\}, \{E\}$$

$$\{E \in B \text{ throwError } e \{P\}, \{E\}\}$$

$$\frac{\bigwedge \times. \ \{\!\!\{R\ x\!\!\}\ b\ x\ \{\!\!\{Q\!\!\}, \{\!\!\{E\!\!\}\ \ \{\!\!\{P\!\!\}\ a\ \{\!\!\{R\!\!\}\}, \{\!\!\{E\!\!\}\ }\!\!\}}{\{\!\!\{P\!\!\}\ a\ \gg = \mathsf{E}\ b\ \{\!\!\{Q\!\!\}, \{\!\!\{E\!\!\}\ }\!\!\}}$$

(other rules analogous)

Today we have seen



- → The automated proof method wp
- → The C Parser and translating C into Simpl
- → AutoCorres and translating Simpl into monadic form
- → The option and exception monads