COMP3161/9164 24T3 Assignment 2 Type Inference for Polymorphic MinHS

Version 1.4.2

Marks : 17.5% of the overall mark

Due date: Monday 18th November 2024, 12:00 PM Sydney time

Overview

In this assignment you will implement type inference for MinHS. The language used in this assignment differs from the language of Assignment 1 in two respects: it has a polymorphic type system, and it has aggregate data structures.

The assignment requires you to:

- (100% marks) Implement the type inference algorithm discussed in the lectures for polymorphic MinHS with sum and product data types;
- (5% bonus) adjust the type inference pass to include various simple syntax extensions from Assignment 1;
- (5% bonus) adjust the type inference pass to allow optional type annotations provided by the user;

Each of these parts is explained in detail below.

The MinHS parser and evaluator are provided for you. You do not have to change anything in any module other than TyInfer.hs (even for the bonus parts).

Your type inference pass should return the inferred type scheme of the top-level binding, main.

Your assignment will only be tested on correct programs, and will be judged correct if it produces a correct type for main up to α -renaming of type variables, and reordering of quantifiers.

Please use the Ed forum for questions about this assignment.

Submission

Submit your (modified) TyInfer.hs using the CSE give system, by typing the command

give cs3161 TyInfer TyInfer.hs

or by using the CSE give web interface.

1 Task 1

Task 1 is worth 100% of the marks of this assignment. You are to implement type inference for MinHS with aggregate data structures. The following cases must be handled:

- the MinHS language of the first task of assignment 1 (without *n*-ary functions, or lists);
- product types: the 0-tuple (aka the Unit type) and 2-tuples;

- sum types;
- polymorphic functions

These cases are explained in detail below. The abstract syntax defining these syntactic entities is in Syntax.hs. You should not need to modify the abstract syntax definition in any way.

Your implementation is to follow the definition of inference rules provided with this assignment. In particular, you must implement a *variables-in-contexts* version of Hindley-Milner type inference [1] by tracking *definitions* (in addition to declarations) for type variables in the context.

Additional material can be found in the lecture notes on polymorphism, and reference materials [2, 3]. The *variables-in-contexts* approach you will need to implement is outlined in this assignment specification, along with inference rules in Figures 1, 2 and 3.

2 Bonus Tasks

These tasks are all optional, and are worth a total of an additional 10%. Marks above 100% are converted to exam marks, at an exchange rate of 1 to 0.15—for example, a mark of 105% yields 0.75 bonus marks for the exam.

2.1 Bonus Task 1: Simple Syntax Extensions

This bonus task is worth an additional 5%. In this task, you should implement type inference for multiple bindings in the one let expression, with the same semantics as the extension task for Assignment 1.

You will need to develop the requisite extensions to the type inference algorithm yourself, but the extensions are very similar to the existing rules.

2.2 Bonus Task 2: User-provided type signatures

This bonus task is worth an additional 5%. In this task you are to extend the type inference pass to accept programs containing *some* type information. You need to combine this with the results of your type inference pass to produce the final type for each declaration. That is, you need to be able to infer correct types for programs like:

You must ensure that the type signatures provided are not overly general. For example, the following program should be a type error, as the user-provided signature is too general:

main :: (forall 'a. 'a) = 3;

You may assume for simplicity that the user-provided types have distinct type variable names for all bound / free type variables. Your solution should, for example, support programs such as:

main :: forall 'a. 'a -> 'a + Int = recfun m y =
 let g :: forall 'b. 'b -> 'a + 'b = recfun f x = Inl y;
 in g 1

where the type variable ' a is in scope for the expression bound to main and appears in the user-provided type annotating g. All occurrences of ' a within the bound expression reference the same type variable.

3 Algebraic Data Types

This section covers the extensions to the language of the first assignment. In all other respects (except lists) the language remains the same, so you can consult the reference material from the first assignment for further details on the language.

3.1 Product Types

We only have 2-tuples in MinHS, and the Unit type, which could be viewed as a 0-tuple.

Types
$$\tau$$
 ::= $\tau \star \tau$
 \mid 1
Expressions e ::= (e, e)
 \mid fst $e \mid$ snd e
 \mid ()

3.2 Sum Types

Sum types in MinHS follow the presentation in the lectures.

```
Types \tau ::= \cdots | \tau + \tau

Expressions e ::= \cdots

| Inl e

| Inr e

| case e of

Inl x \rightarrow e;

Inr y \rightarrow e;
```

3.3 Polymorphism

The extensions to allow polymorphism are relatively minor. Three new type forms have been introduced: the FlexVar t form, the RigidVar t form, and the Forall t e form. FlexVar t represents a unification variable introduced during type inference. RigidVar t represents a fixed type variable introduced by a forall-quantifier. Consult Section 4 for more details on the notational conventions used in this specification and how they relate to the Haskell code. We distinguish between type *schemes* and other types:¹

Type inference should return a correctly typed top-level binding for main. For example, consider the following code fragment before and after type inference:

```
main =
    let f = recfun g x = x;
    in if f True
        then f (Inl 1)
        else f (Inr ());
main :: (Int + 1) =
    let f = recfun g x = x;
    in if f True
        then f (Inl 1)
        else f (Inr ());
```

4 Notational Conventions

In this document, we will use a number of conventions and conveniences to streamline the presentation detailed in Table 1.

¹Here, and elsewhere in the spec we use $\overline{overlines}$ to mean "sequence of". So, e.g., $\overline{\sigma}$ is a sequence of type schemes.

| Concept | Specification Notation | Haskell Notation |
|-------------------------------------|--|---|
| Flexible Type Variable | $lpha^{	extsf{F}}, eta^{	extsf{F}}, ho^{	extsf{F}}, \ldots$ | FlexVar α |
| Rigid Type Variable | $lpha^{	extsf{r}},eta^{	extsf{r}}, ho^{	extsf{r}},\ldots$ | RigidVar $lpha$ |
| Flexible Type Variable Declaration | α | $\alpha := \text{HOLE}$ |
| Flexible Type Variable Definition | $\alpha := \tau$ | $\alpha:= \operatorname{Defn} \tau$ |
| Rigid Type Variable Substitution | $\tau[\alpha^{\mathbb{R}} := \tau']$ | substRigid ($lpha$ =: $	au'$) $	au$ |
| Flexible Type Variable Substitution | $\tau[\alpha^{\scriptscriptstyle \mathbb{F}}:=\tau']$ | substFlex ($lpha$ =: $	au'$) $	au$ |
| Term Variable Entry | $x:\sigma$ | $\operatorname{Term}\operatorname{Var} x\sigma$ |

Table 1: Notations and Conventions in this Specification vs. Haskell code for Assignment

Type variable *names* are ranged over by lowercase greek letters. We distinguish between flexible and rigid type variables by superscripting such names with F and R, respectively.

Declarations and definitions for flexible type variables appear in typing contexts, see Section 5.1 for the full grammar of contexts.

Substitution for type variables occurring in types is explained in Section 6. Since there are two kinds of type variables: flexible ones introduced during type inference, and rigid ones bound by \forall -quantifiers, we have two kinds of substitution operation depending on which type variables we wish to replace. These are called substFlex and substRigid in the Subst.hs Haskell module, substituting for flexible and rigid type variables, respectively.

5 Type Inference Rules

The type inference are rules presented in Figure 3 using the judgement form:

$$\Gamma_1 \vdash e \xrightarrow{\text{INF}} \tau \dashv \Gamma_2$$

where blue components on the left of $\stackrel{\text{INF}}{\Longrightarrow}$ can be viewed as *inputs* to the algorithm, while red components

on the right of $\xrightarrow{\text{INF}}$ can be viewed as outputs. The type inference rules directly encode an algorithm with explicit inputs and outputs. Inputs to the conclusion are inputs to the first premise (by convention the leftmost premise of a rule). The outputs of a premise can be used as inputs to subsequent premises. The left-hand typing environment and expression are inputs to any rule. The right-hand typing environment and the type are outputs. The judgement encodes a substitution from type variables in the input typing environment to types in the output typing environment.

Such an algorithm has type signature:

inferExp :: Gamma -> Exp -> TC (Type, Gamma)

The goal is to *infer* the type of the top-level binding by inferring the types for all its sub-expressions, and propagating this information upwards through the program source tree. You should replace the unannotated top-level binding (*i.e.* main) with an explicitly typed equivalent.

5.1 Contexts for Polymorphism, Contexts for Type Inference

To support polymorphism and enable type inference, the grammar for typing contexts Γ is extended to track *unification* or *flexible* type variables, and their *instantiation* with a concrete type, if any. They are "flexible" in the sense that they are introduced by the type inference algorithm in order to establish constraints between types.

A context tracks both *declarations* and *definitions* of flexible type variables. A declaration is denoted by α in this document, or $\alpha := \text{HOLE}$ in Haskell² and declares α to be the name of a flexible type variable which has not yet been instantiated with a concrete type. On the other hand, a definition is denoted by $\alpha := \tau$ for some type variable name α and type τ . The full grammar³ for contexts looks like this:

 $\Gamma \quad ::= \quad \epsilon \mid \Gamma \cdot x : \sigma \mid \Gamma \cdot \alpha \mid \Gamma \cdot \alpha := \tau \mid \Gamma \cdot \bullet$

²Again, Table 1 summarises these conventions.

³The • is explained later.

We distinguish a context from a *suffix* Δ which is a list containing only type variable declarations or definitions:

$$\Delta \quad ::= \quad [] \mid \alpha :: \Delta \mid \alpha := \tau :: \Delta$$

5.2 Generalisation

Generalisation is the process of introducing zero or more \forall quantified type variables on a type to form a *type scheme*. This process must be minimal in the sense that it generalises only those type variables relevant for the current type inference problem. The judgement form is:

| $\Gamma_1 \vdash e \xrightarrow{\text{GEN}} \sigma \dashv \Gamma_2$ |
|---|
|---|

where from input context Γ_1 and expression *e* the algorithm infers the *type scheme* σ and output context Γ_2 . There is only one rule for generalisation given by:

$$\frac{\frac{\text{GEN}}{\Gamma_{1} \cdot \bullet \vdash e \stackrel{\text{INF}}{\Longrightarrow} \tau \dashv \Gamma_{2} \cdot \bullet \cdot \Delta \quad \sigma = \text{gen}(\text{rev}(\Delta), \tau, [])}{\Gamma_{1} \vdash e \stackrel{\text{GEN}}{\Longrightarrow} \sigma \dashv \Gamma_{2}}$$

where rev(Δ) reverses the elements in the suffix Δ^4 .

The algorithm keeps track of relevant type variables by using *markers*, denoted by \bullet , which split the context up into localities. A type variable occurring to the right of a marker can be safely generalised in a type scheme because the surrounding context does not depend on it. In the GEN rule, we can generalise τ over Δ (which contains only type variable declarations and definitions) to form the type scheme σ :

Type variables can gain more global relevance by moving their declarations to the left of markers. Such a movement is irreversible, once a type variable has moved beyond a marker it can never be moved back "to the right".

To keep type inference tractable, generalisation is performed only on let-bindings and the top-level main binding. Recursive functions are not generalised. Pay close attention to the premises of the LET and PRO-GRAM typing rules in Figure 3 to see where generalisation should be used.

5.3 Unification

Solving type inference problems depends on solving *unification* problems between types. Just like the type inference rules, unification can be expressed algorithmically as a transformation on the typing context. Some of these rules were discussed in lectures and are repeated in Figure 1 (except a few structural and symmetric rules — fill in the details!) and take the following form:

$$\Gamma_1 \vdash \tau_1 \sim \tau_2 \overset{\text{UNI}}{\Longrightarrow} \Gamma_2$$

where, again, inputs are blue and outputs are red.

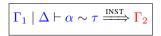
⁴Reversing Δ is required by our definition of gen(-, -, -) because we need to process more local type variables first in case they depend on later type variables appearing in Δ . You can avoid the reversal if you first build a simultaneous substitution (Section 6) out of Δ .

$$\Gamma_1 \vdash \tau_1 \sim \tau_2 \xrightarrow{\mathrm{UNI}} \Gamma_2$$

Figure 1: Unification Rules

5.4 Instantiation

The unification judgement depends on *instantiation*, that is, solving an equation involving a flexible type variable (unification variable) and any type which is not a flexible type variable. This judgement (Figure 2) takes the following form:



The algorithm simplifies the problem by moving through the context, similar to the strategy employed during unification for the case of unifying two flexible type variables. Some points worth noting:

- FTV (τ) computes the set of names of flexible type variables occurring in τ ;
- For DEFN, we must check that the no flexible type variables occurring in τ have the name α . This condition is known as the *occurs check* and prevents cyclic dependencies which are unsound;
- Instantiation accumulates a list Δ recording the type variable dependencies of τ which must be given more global relevance in order to solve for α;
- For DEFN, the dependencies of τ are placed to the right of the definition of α because by setting α:=τ, it also depends on type variables in Δ;

6 Substitution

Substitutions are implemented as an abstract data type, defined in Subst.hs. Subst is an instance of the Monoid type class, which is defined in the standard library as follows:

```
class Monoid a where
mappend :: a -> a -> a -- also written as the infix operator <>
mempty :: a
```

$$\Gamma_1 \mid \Delta \vdash \alpha \sim \tau \xrightarrow{\mathrm{INST}} \Gamma_2$$

| $\frac{\alpha \notin \text{FTV}(\tau)}{\Gamma_1 \cdot \alpha \mid \Delta \vdash \alpha \sim \tau \xrightarrow{\text{INST}} \Gamma_1 \cdot \Delta \cdot \alpha := \tau}$ | $\frac{\substack{\beta \neq \alpha \beta \in \texttt{FTV}(\tau) \Gamma_1 \mid \beta :: \Delta \vdash \alpha \sim \tau \stackrel{\texttt{INST}}{\Longrightarrow} \Gamma_2}{\Gamma_1 \cdot \beta \mid \Delta \vdash \alpha \sim \tau \stackrel{\texttt{INST}}{\Longrightarrow} \Gamma_2}$ |
|--|---|
| $\begin{split} & \frac{\mathrm{Subst}}{\Gamma_1 \cdot \Delta \vdash \alpha^{\mathrm{F}}[\beta^{\mathrm{F}} := \tau'] \sim \tau[\beta^{\mathrm{F}} := \tau'] \stackrel{\mathrm{UNI}}{\Longrightarrow} \Gamma_2}{\Gamma_1 \cdot \beta := \tau' \mid \Delta \vdash \alpha \sim \tau \stackrel{\mathrm{INST}}{\Longrightarrow} \Gamma_2 \cdot \beta := \tau'} \end{split}$ | $\frac{SKIP\text{-}Ty}{\beta \neq \alpha \beta \notin FTV\left(\tau\right) \Gamma_1 \mid \Delta \vdash \alpha \sim \tau \xrightarrow{INST} \Gamma_2}{\Gamma_1 \cdot \beta \mid \Delta \vdash \alpha \sim \tau \xrightarrow{INST} \Gamma_2 \cdot \beta}$ |
| $\begin{split} & \overset{\text{SKIP-TM}}{\Gamma_1 \mid \Delta \vdash \alpha \sim \tau \xrightarrow{\text{INST}} \Gamma_2} \\ & \overline{\Gamma_1 \cdot x : \sigma \mid \Delta \vdash \alpha \sim \tau \xrightarrow{\text{INST}} \Gamma_2 \cdot x :} \end{split}$ | $\sigma \qquad \qquad \begin{array}{c} SKIP\text{-}MARK \\ \Gamma_1 \mid \Delta \vdash \alpha \sim \tau \xrightarrow{INST} \Gamma_2 \\ \hline \\ \overline{\Gamma_1 \cdot \bullet \mid \Delta \vdash \alpha \sim \tau \xrightarrow{INST} \Gamma_2 \cdot \bullet} \end{array}$ |

Figure 2: Algorithmic instantiation rules

For the Subst instance, mempty corresponds to the empty substitution, and mappend is *substitution composition*. That is, applying the substitution a <> b is the same as applying a and b simultaneously. It should be reasonably clear that this instance obeys the *monoid laws*:

| mempty <> x == x | left identity |
|--|--------------------|
| x <> mempty == x | right identity |
| $x \iff (y \iff z) == (x \iff y) \iff z$ | associativity |

It is also *commutative* ($x \ll y = y \ll x$) assuming that the substitutions are *disjoint* (i.e that $dom(x) \cap dom(y) = \emptyset$). In the type inference algorithm, your substitutions are all applied in order and thus should be disjoint, therefore this property should hold.

You can use this <> operator to combine multiple substitutions into a single substitution; however, there should be little need to use anything more complicated than single substitutions for this algorithm.

You can construct a singleton substitution, which replaces one variable, with the =: operator, so the substitution ("a" =: FlexVar "b") <> ("b" =: FlexVar "c") using substFlex is a substitution which renames all flexible type variables with name a or b with the name c.

The Subst module also includes a variety of functions for running substitutions on types and expressions for both rigid and flexible type variable replacement. In particular, the module provides two functions for expressions and types respectively, for substitution of type variables:

```
-- | Perform substitution on rigid type variables.
substRigid :: Subst -> Type -> Type
-- | Perform substitution on flexible type variables.
substFlex :: Subst -> Type -> Type
```

and similar for Exp. You can use these functions for implementing some of the algorithmic rules.

7 Errors and Fresh Names

Thus far, the following type signature would be sufficient for implementing our type inference function:

inferExp :: Gamma -> Exp -> (Type, Gamma)

Unification is a partial function, however, so we want a principled way to handle the error cases, rather than just bail out with error calls.

To achieve this, we'll adjust the basic, pure signature for type inference to include the possibility of a TypeError:

$$\Gamma_1 \vdash e \xrightarrow{\mathrm{INF}} \tau \dashv \Gamma_2$$

$$\begin{array}{l} \operatorname{Var} & \operatorname{Int} \\ \frac{x: \forall \, \overline{\alpha_i}. \, \tau \in \Gamma}{\Gamma \vdash x \xrightarrow{\operatorname{InF}} \tau[\, \overline{\alpha^{\operatorname{R}}{}_i := \beta^{\operatorname{F}}{}_i \,]} \dashv \Gamma \cdot \overline{\beta_i}} \, \beta_i \, fresh & \begin{array}{l} \operatorname{Int} \\ n \, \text{an integer} \\ \overline{\Gamma \vdash n \xrightarrow{\operatorname{InF}} \operatorname{Int}} \dashv \Gamma \end{array} \end{array}$$

.

С

$$\frac{\operatorname{App}}{\Gamma_{1} \vdash e_{1} \xrightarrow{\operatorname{INF}} \tau_{1} \dashv \Gamma_{2} \quad \Gamma_{2} \vdash e_{2} \xrightarrow{\operatorname{INF}} \tau_{2} \dashv \Gamma_{3} \quad \Gamma_{3} \cdot \alpha \vdash \tau_{1} \sim \tau_{2} \to \alpha^{\operatorname{F}} \xrightarrow{\operatorname{UNI}} \Gamma_{4}}{\Gamma_{1} \vdash \operatorname{Apply} e_{1} e_{2} \xrightarrow{\operatorname{INF}} \alpha^{\operatorname{F}} \dashv \Gamma_{4}} \alpha \text{ fresh}$$

$$\begin{array}{c} \text{IF-THEN-ELSE} \\ \Gamma_1 \vdash e \xrightarrow{\text{INF}} \tau \dashv \Gamma_2 \quad \Gamma_2 \vdash \tau \sim \text{Bool} \xrightarrow{\text{UNI}} \Gamma_3 \\ \hline \Gamma_3 \vdash e_t \xrightarrow{\text{INF}} \tau_t \dashv \Gamma_4 \quad \Gamma_4 \vdash e_f \xrightarrow{\text{INF}} \tau_f \dashv \Gamma_5 \quad \Gamma_5 \vdash \tau_t \sim \tau_f \xrightarrow{\text{UNI}} \Gamma_6 \\ \hline \hline \Gamma_1 \vdash \text{If } e \; e_t \; e_f \xrightarrow{\text{INF}} \tau_t \dashv \Gamma_6 \end{array}$$

CASE

$$\begin{split} & \Gamma_{1} \vdash e \xrightarrow{\mathrm{INF}} \tau \dashv \Gamma_{2} \quad \Gamma_{2} \cdot \alpha \cdot \beta \vdash \tau \sim \alpha^{\mathrm{F}} + \beta^{\mathrm{F}} \xrightarrow{\mathrm{UNI}} \Gamma_{3} \\ & \Gamma_{3} \cdot x : \alpha^{\mathrm{F}} \vdash e_{1} \xrightarrow{\mathrm{INF}} \tau_{1} \dashv \Gamma_{4} \cdot x : \alpha^{\mathrm{F}} \cdot \Delta \quad \Gamma_{4} \cdot \Delta \cdot y : \beta^{\mathrm{F}} \vdash e_{2} \xrightarrow{\mathrm{INF}} \tau_{2} \dashv \Gamma_{5} \cdot y : \beta^{\mathrm{F}} \cdot \Delta' \\ & \Gamma_{5} \cdot \Delta' \vdash \tau_{1} \sim \tau_{2} \xrightarrow{\mathrm{UNI}} \Gamma_{6} \\ & \Gamma_{1} \vdash \mathrm{Case} \ e \ x.e_{1} \ y.e_{2} \xrightarrow{\mathrm{INF}} \tau_{1} \dashv \Gamma_{6} \\ \end{split}$$

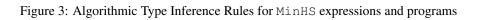
RECFUN

$$\begin{array}{c} \overbrace{\Gamma_{1} \cdot \alpha \cdot \beta \cdot x : \alpha^{\mathrm{F}} \cdot f : \beta^{\mathrm{F}} \vdash e \stackrel{\mathrm{INF}}{\Longrightarrow} \tau \dashv \Gamma_{2} \cdot x : \alpha^{\mathrm{F}} \cdot f : \beta^{\mathrm{F}} \cdot \Delta \quad \Gamma_{2} \cdot \Delta \vdash \beta^{\mathrm{F}} \sim \alpha^{\mathrm{F}} \rightarrow \tau \stackrel{\mathrm{UNI}}{\Longrightarrow} \Gamma_{3}}{\Gamma_{1} \vdash \operatorname{Recfun} f.x.e \stackrel{\mathrm{INF}}{\Longrightarrow} \beta^{\mathrm{F}} \dashv \Gamma_{3}} \\ \\ \begin{array}{c} \underset{\Gamma_{1} \vdash e_{1} \stackrel{\mathrm{GEN}}{\Longrightarrow} \sigma \dashv \Gamma_{2} \quad \Gamma_{2} \cdot x : \sigma \vdash e_{2} \stackrel{\mathrm{INF}}{\Longrightarrow} \tau \dashv \Gamma_{3} \cdot x : \sigma \cdot \Delta}{\Gamma_{1} \vdash \operatorname{Let} e_{1} \ x.e_{2} \stackrel{\mathrm{INF}}{\Longrightarrow} \tau \dashv \Gamma_{3} \cdot \Delta} \end{array} \end{array}$$

 $\Gamma_1 \vdash p \xrightarrow{\text{INF_PROG}} \sigma \dashv \Gamma_2$

 $\begin{array}{c} \operatorname{Program} \\ \Gamma_1 \vdash e \xrightarrow{\operatorname{gen}} \sigma \dashv \Gamma_2 \end{array}$

$$\Gamma_1 \vdash \operatorname{Program} e \xrightarrow{\operatorname{INF}\operatorname{PROG}} \sigma \dashv \Gamma_2$$



inferExp :: Gamma -> Exp -> Either TypeError (Type, Gamma)

Even this, though, is not sufficient, as we cannot generate fresh, unique type variable names for use as flexible/unification variables:

freshId :: Id -- it is impossible for fresh to return a different
freshId = ? -- value each time!

To solve this problem, we could pass an (infinite) list of unique names around our program, and fresh could simply take a name from the top of the list, and return a new list with the name removed:

fresh :: [Id] -> ([Id],Id)
fresh (x:xs) = (xs,x)

This is quite awkward though, as now we have to manually thread our list of identifiers throughout the entire inference algorithm:

```
inferExp :: Gamma -> Exp -> [Id] -> Either TypeError ([Id], (Type, Gamma))
```

To resolve this, we bundle both the [Id] state transformer and the Either TypeError x error handling into one abstract type, called TC (defined in TCMonad.hs)

newtype TC a = TC ([Id] -> Either TypeError ([Id], a))

One can think of TC a abstractly as referring to a *stateful action* that will, if executed, return a value of type a, or throw an exception.

As the name of the module implies, TC is a *Monad*, meaning that it exposes two functions (return and >>=) as part of its interface.

```
return :: a -> TC a
return = ...
(>>) :: TC a -> TC b -> TC b
a >> b = a >>= const b
(>>=) :: TC a -> (a -> TC b) -> TC b
a >>= b = ...
```

The function return is, despite its name, just an ordinary function which *lifts* pure values into a TC action that returns that value. The function (>>) (read *then*), is a kind of composition operator, which produces a TC action which runs two TC actions in sequence, one after the other, returning the value of the last one to be executed. Lastly, the function (>>=), more general than (>>), allows the second executed action to be determined by the return value of the first.

The TCMonad.hs module also includes a few built-in actions:

typeError :: TypeError -> TC a -- throw an error freshId :: TC Id -- return a fresh type variable name

Haskell includes special syntactic sugar for monads, which allow for programming in a somewhat imperative style. Called do notation, it is simple sugar for (>>) and (>>=).

| do e | е |
|-----------------|-----------------------|
| do e; v | e >> do v |
| do p <- e; v | e >>= \p -> do v |
| do let x = y; v | let x = y in do v |

This lets us write unification and type inference quite naturally. A simple example of the use of the TC monad is already provided to you, the specialise function, which takes a type with some number of quantifiers, and replaces all quantifiers with fresh variables (very useful in the type inference cases for variables, constructors, and primops):

```
specialise :: Scheme -> TC (Type, Suffix)
specialise (Forall xs t) =
    do ids <- freshForall xs
        return (S.substRigid (S.fromList (map (second FlexVar) ids)) t
        , map (flip (,) HOLE . snd) ids)</pre>
```

To run a TC action in your top level infer function, the runTC function can be used:

```
runTC :: TC a -> Either TypeError a
```

Please note: This function runs the TC action with the same source of fresh names each time! Using it more than once in your program is not likely to give correct results.

8 Program structure

A program in MinHS may evaluate to any non-function type, including an aggregate type. This is a valid MinHS program:

```
main = (1, (InL True, False));
```

which can be elaborated to the following type:

8.1 Type information

The most significant change to the language of assignment 1 is that the parser now accepts programs without any type information. Type declarations are not compulsory! Unless you are attempting the bonus parts of the assignment, you can assume that *no* type information will be provided in the program.

You can view the type information after your pass using --dump type-infer.

9 Implementing Type Inference

You are required to implement the function infer. Some stub code has been provided for you, along with some type declarations, and the type signatures of useful functions you may wish to implement. You may change any part of TyInfer.hs you wish, as long as it still provides the function infer, of the correct type. The stub code is provided only as a hint, you are free to ignore it.

10 Testing

Your assignments will be autotested rigorously. You are encouraged to autotest yourself. MinHS comes with a tester script, and you can add your own tests to this. Your assignment will be tested by comparing the output Program of your infer function (*not* the output of tyinf --dump type-infer) against the expected output Program. Your solution must be α -equivalent to the expected solution.

Much like the previous assignment, you are given a suite of tests for Task 1. Unlike the previous assignment, the tests do not specify the expected results—note the lack of .out files. Beware: unless you add .out specifying the expected result yourself, the tests will report success no matter what you return.

It is up to you to write your own tests for the extension tasks. Any .out files and additional tests you write are for your own benefit – you will not submit them for marking.

In this assignment we make no use of the later phases of the compiler.

11 Building MinHS

Building MinHS is exactly the same as in Assignment 1.

To run the type inference pass and inspect its results, for cabal users type:

\$ cabal run tyinf -- --dump type-infer foo.mhs

Users of stack should type:

\$ stack exec tyinf -- --dump type-infer foo.mhs

You may wish to experiment with some of the debugging options to see, for example, how your program is parsed, and what abstract syntax is generated. Many --dump flags are provided, which let you see the abstract syntax at various stages in the compiler.

12 Late Penalty

You may submit up to five days (120 hours) late. Each day of lateness corresponds to a 5% reduction of your total mark. For example, if your assignment is worth 88% and you submit it two days late, you get 78%. If you submit it more than five days late, you get 0%.

Course staff cannot grant assignment extensions—if you need an extension, you have to apply for special consideration through the standard procedure. More information here: https://www.student.unsw.edu.au/special-consideration

13 Plagiarism

Many students do not appear to understand what is regarded as plagiarism. This is no defense. Before submitting any work you should read and understand the UNSW plagiarism policy https://student.unsw.edu.au/plagiarism.

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References

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