

COMP2521 24T3

Graphs (II)

Graph Traversal

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bfs and dfs
path checking
path finding

Common problems on graphs:

- Is there a path between two vertices?
- What is the shortest path between two vertices?
- Is the graph connected?
- If we remove an edge, is the graph still connected?
- Which vertices are reachable from a particular vertex?
- Is there a cycle that passes through all vertices?

All of the above problems can be solved by a **systematic exploration** of a graph via its **edges**.

This systematic exploration is called **traversal** or **search**.

- Visiting a vertex: going to a vertex
- Exploration of the vertex: exploration means if I am on a particular vertex, then visiting its all adjacent vertices

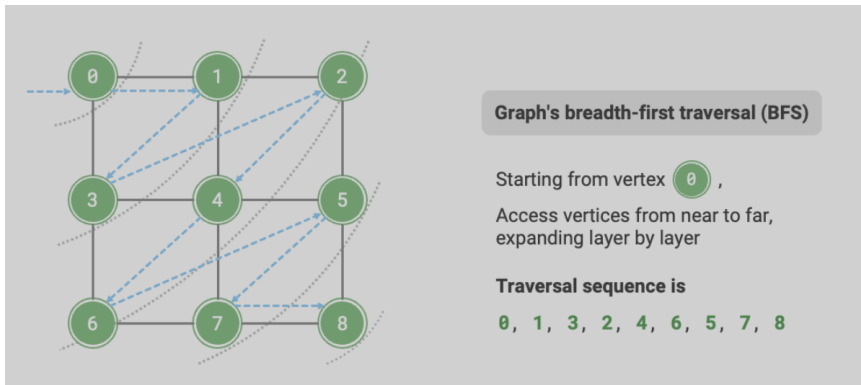
Two primary methods for graph traversal/search:

Breadth-first search (BFS)

- Prioritises visiting all neighbours over path-following
 - “Go wide”
- Implemented iteratively (using a queue)

Depth-first search (DFS)

- Prioritises path-following over visiting all neighbours
 - “Go deep”
- Implemented recursively or iteratively (using a stack)



Graph's depth-first traversal (DFS)

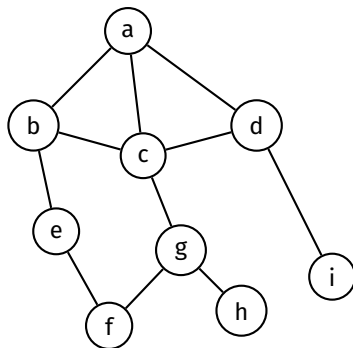
Starting from vertex **0**

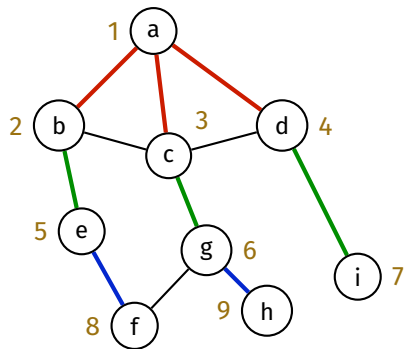
Search to the end before returning, then continue to search before returning

Continue like this until the traversal is completed

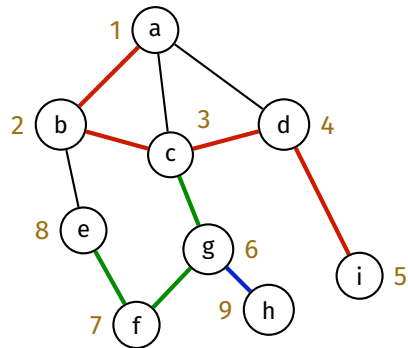
Traversal sequence is
0, 1, 2, 5, 4, 6, 3

In what order would BFS and DFS visit the vertices of this graph?





Breadth-first search



Depth-first search

Breadth-first search visits vertices
in order of distance from the starting vertex.

It visits the starting vertex,
then the neighbours of the starting vertex,
then the neighbours of those neighbours,
etc.

BFS is implemented iteratively using a queue.

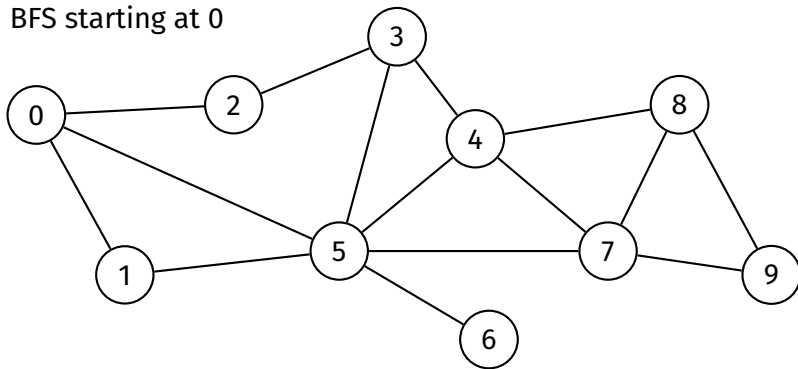
Data structures used in BFS:

- Visited array
 - To keep track of which vertices have been visited
- Predecessor array
 - To keep track of the predecessor of each vertex
 - The predecessor of v is the vertex from which we reached v
 - i.e., the vertex before v on the path to v
- Queue
 - First-in-first-out data structure
 - Stores unvisited vertices in the order that they should be visited

Algorithm:

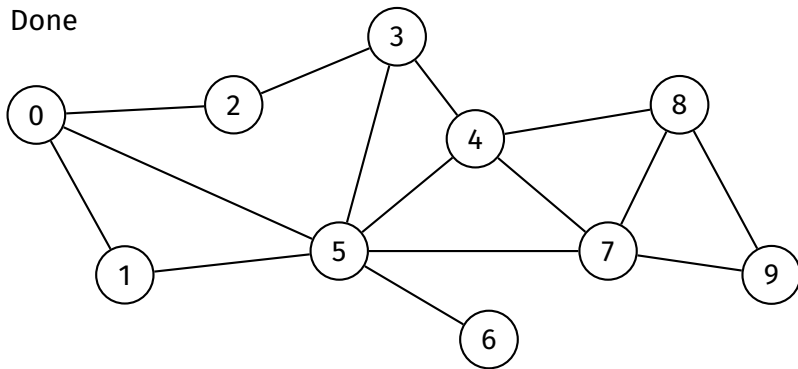
- 1 Create/initialise data structures:
 - Create visited array, initialised to false
 - Create predecessor array, initialised to -1
 - Create empty queue
- 2 Mark starting vertex as visited and enqueue it
- 3 While the queue is not empty:
 - 1 Dequeue a vertex
 - Let this vertex be v
 - 2 **Explore** v - that is, for each of v 's unvisited neighbours:
 - 1 Mark it as visited
 - 2 Set its predecessor to v
 - 3 Enqueue it

BFS starting at 0



	[0]	[1]	[2]	[3]	[4]	[5]	[6]	[7]	[8]	[9]
visited	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>
pred	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>
queue	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>

Done



	[0]	[1]	[2]	[3]	[4]	[5]	[6]	[7]	[8]	[9]
visited	1	1	1	1	1	1	1	1	1	1
pred	-1	0	0	2	5	0	5	5	4	7
queue	0	1	2	5	3	4	6	7	8	9

```
bfs( $G$ ,  $src$ ):
```

```
  Input: graph  $G$ , starting vertex  $src$ 
```

```
  create visited array, initialised to false  
  create predecessor array, initialised to -1  
  create queue  $Q$ 
```

```
  visited[ $src$ ] = true  
  enqueue  $src$  into  $Q$ 
```

```
  while  $Q$  is not empty:
```

```
     $v$  = dequeue from  $Q$ 
```

```
    for each neighbour  $w$  of  $v$  in  $G$  where visited[ $w$ ] = false:
```

```
      visited[ $w$ ] = true
```

```
      predecessor[ $w$ ] =  $v$ 
```

```
      enqueue  $w$  into  $Q$ 
```

Graph
Traversal

BFS

Example

Pseudocode

Analysis

Path Finding

DFS

Ideas/Issues

When using a predecessor array in BFS,
the predecessor array can double as a visited array

$\text{predecessor}[v] = -1$ means v is not visited

```
dfs( $G, src$ ):
```

```
  Input: graph  $G$ , starting vertex  $src$ 
```

```
  create predecessor array, initialised to -1
```

```
  create queue  $Q$ 
```

```
  predecessor[ $src$ ] =  $src$  //  $\leftarrow$  mark  $src$  as visited
```

```
  enqueue  $src$  into  $Q$ 
```

```
  while  $Q$  is not empty:
```

```
     $v$  = dequeue from  $Q$ 
```

```
    for each neighbour  $w$  of  $v$  in  $G$  where predecessor[ $w$ ] = -1:
```

```
      predecessor[ $w$ ] =  $v$ 
```

```
      enqueue  $w$  into  $Q$ 
```


BFS is $O(V + E)$ when using the adjacency list representation:

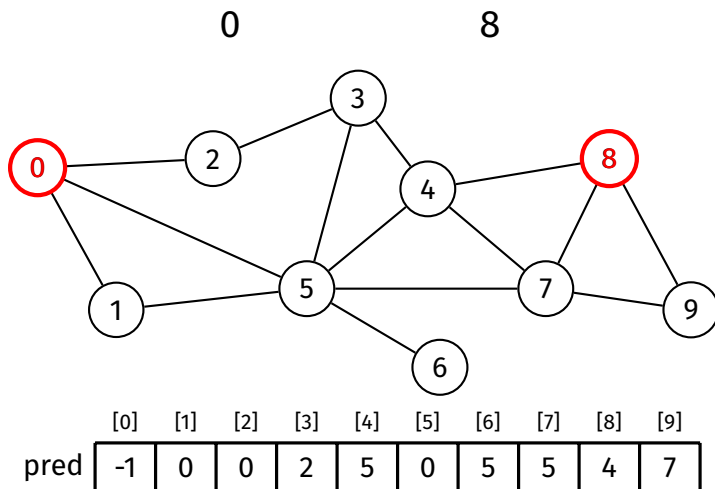
- Typical queue implementation has $O(1)$ enqueue and dequeue
- Each vertex is visited at most once $\Rightarrow O(V)$
- For each vertex, all of its edges are considered $\Rightarrow O(E)$

A BFS finds the shortest path between the starting vertex and all other vertices.

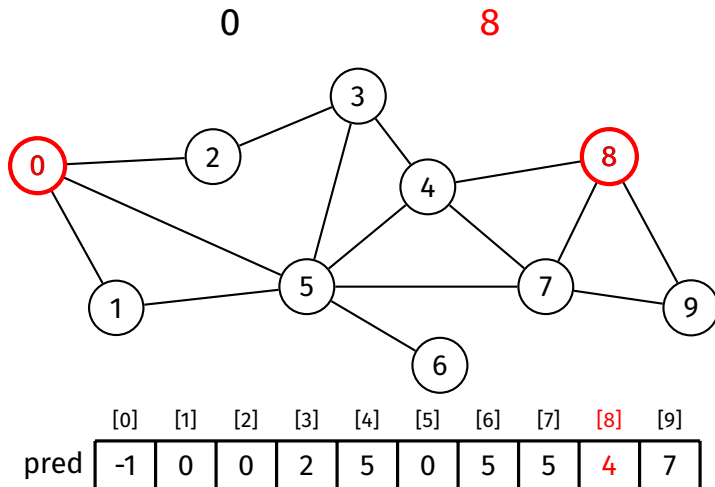
- Shortest path in terms of the number of edges

The shortest path between *src* and *dest* can be found by tracing backwards through the predecessor array (from *dest* to *src*).

Example: Shortest path from 0 to 8



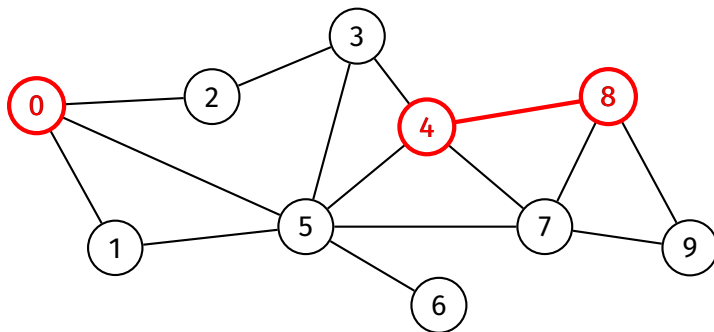
Example: Shortest path from 0 to 8



Example: Shortest path from 0 to 8

0

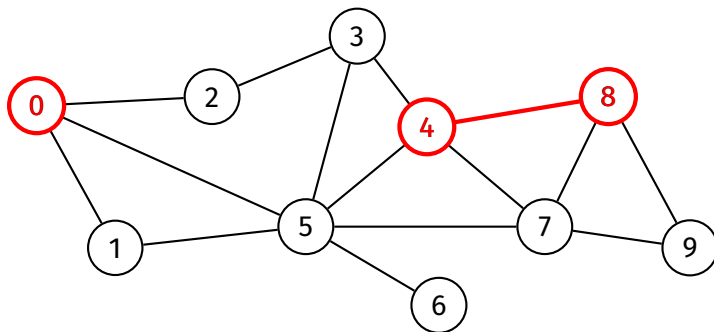
4 → 8



	[0]	[1]	[2]	[3]	[4]	[5]	[6]	[7]	[8]	[9]
pred	-1	0	0	2	5	0	5	5	4	7

Example: Shortest path from 0 to 8

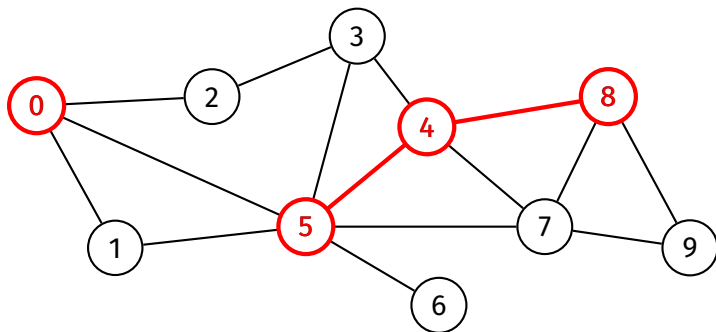
0 4 → 8



	[0]	[1]	[2]	[3]	[4]	[5]	[6]	[7]	[8]	[9]
pred	-1	0	0	2	5	0	5	5	4	7

Example: Shortest path from 0 to 8

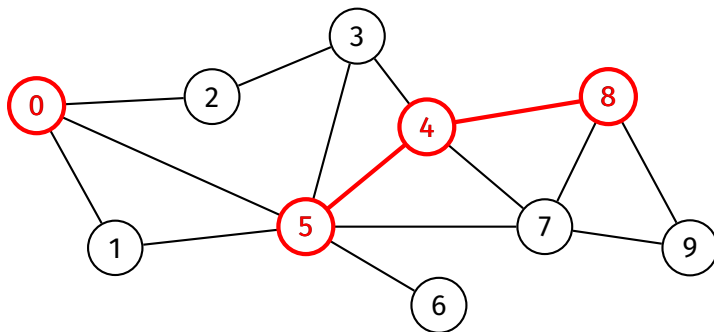
0 5 → 4 → 8



	[0]	[1]	[2]	[3]	[4]	[5]	[6]	[7]	[8]	[9]
pred	-1	0	0	2	5	0	5	5	4	7

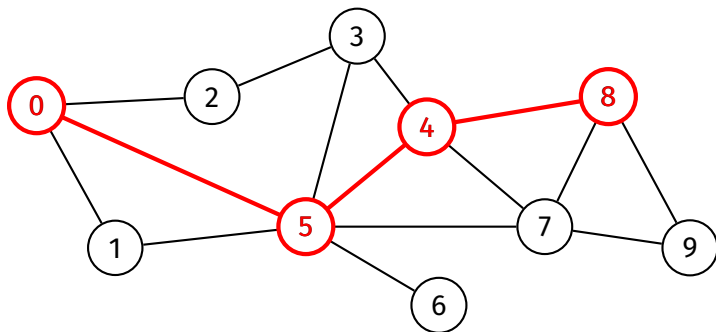
Example: Shortest path from 0 to 8

0 5 → 4 → 8



	[0]	[1]	[2]	[3]	[4]	[5]	[6]	[7]	[8]	[9]
pred	-1	0	0	2	5	0	5	5	4	7

Example: Shortest path from 0 to 8

 $0 \rightarrow 5 \rightarrow 4 \rightarrow 8$ 

	[0]	[1]	[2]	[3]	[4]	[5]	[6]	[7]	[8]	[9]
pred	-1	0	0	2	5	0	5	5	4	7

```
bfsFindPath( $G$ ,  $src$ ,  $dest$ ):  
    Input: graph  $G$ , vertices  $src$  and  $dest$   
  
    ... BFS starting from  $src$  ...  
  
    if predecessor[ $dest$ ]  $\neq$  -1:  
         $v = dest$   
        while  $v \neq src$ :  
            print  $v$ , "<-"  
             $v = predecessor[v]$   
  
    print  $src$ 
```

Depth-first search goes as far down one path as possible until it reaches a dead end, then backtracks until it finds a new path to take, then repeats

DFS can be implemented recursively or iteratively.

Depth-first search is described recursively as:

- 1 Mark current vertex as visited
 - The first time, this is the starting vertex
- 2 For each neighbour of the current vertex:
 - If it has not been visited:
 - Recursively traverse starting from that vertex

The recursion naturally induces backtracking.

```
dfs( $G$ ,  $src$ ):
```

```
    Input: graph  $G$ , starting vertex  $src$ 
```

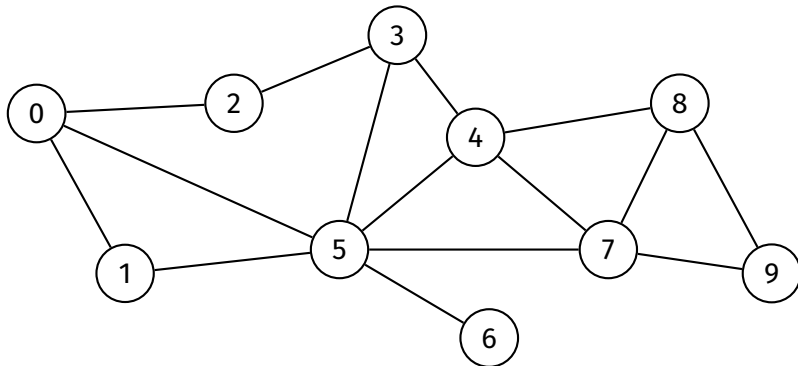
```
    create visited array, initialised to false  
    dfsRec( $G$ ,  $src$ , visited)
```

```
dfsRec( $G$ ,  $v$ , visited):
```

```
    Input: graph  $G$ , vertex  $v$ , visited array
```

```
    visited[ $v$ ] = true // "visit"  $v$   
    for each neighbour  $w$  of  $v$  in  $G$ :  
        if visited[ $w$ ] = false:  
            dfsRec( $G$ ,  $w$ , visited)
```

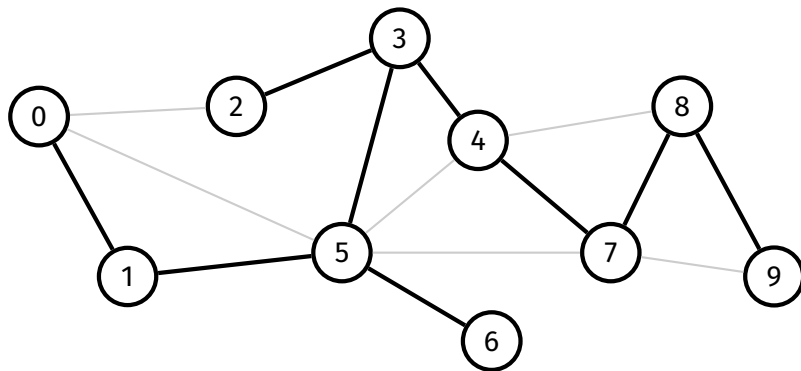
DFS starting at 0



	[0]	[1]	[2]	[3]	[4]	[5]	[6]	[7]	[8]	[9]
visited	0	0	0	0	0	0	0	0	0	0

visit order

Done



	[0]	[1]	[2]	[3]	[4]	[5]	[6]	[7]	[8]	[9]
visited	1	1	1	1	1	1	1	1	1	1

visit order 0 1 5 3 2 4 7 8 9 6

Graph
Traversal

BFS

DFS

Recursive

Pseudocode

Example

Analysis

Path checking

Path finding

Iterative

Ideas/Issues

Recursive DFS is $O(V + E)$ when using the adjacency list representation:

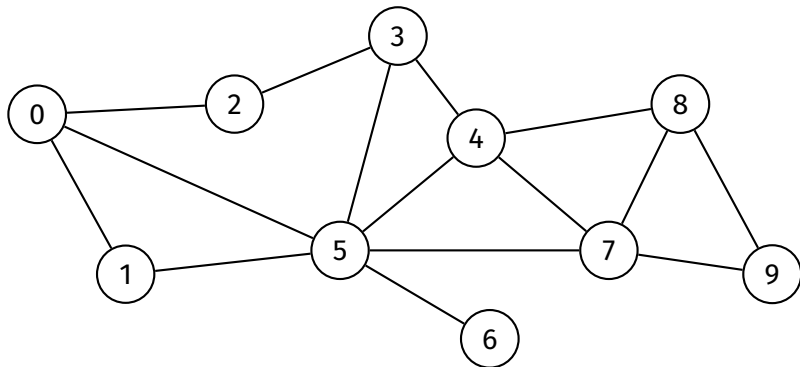
- Each vertex is visited at most once $\Rightarrow O(V)$
 - Function is called on each vertex at most once
- For each vertex, all of its edges are considered once $\Rightarrow O(E)$

Recursive DFS can be adapted to check if a path exists between two vertices.

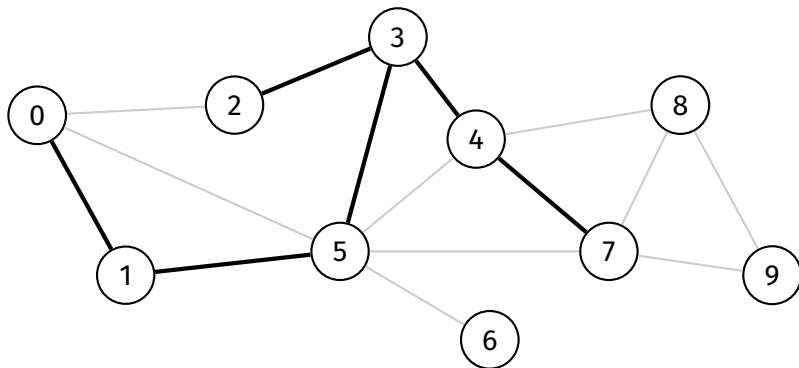
Idea:

- To check if a path exists between src and $dest$:
 - If $src = dest$, then there is a path (the empty path)
 - Otherwise, for each neighbour of src , recursively check if there is a path from that neighbour to $dest$

Does there exist a path between 0 and 7 in this graph?



Answer: Yes



```
dfsHasPath( $G$ ,  $src$ ,  $dest$ ):
```

```
    Input: graph  $G$ , vertices  $src$  and  $dest$ 
```

```
    Output: true if there is a path from  $src$  to  $dest$   
             false otherwise
```

```
    create visited array, initialised to false
```

```
    return dfsHasPathRec( $G$ ,  $src$ ,  $dest$ , visited)
```

```
dfsHasPathRec( $G$ ,  $v$ ,  $dest$ , visited):
```

```
    Input: graph  $G$ , vertices  $v$  and  $dest$ , visited array
```

```
    visited[ $v$ ] = true
```

```
    if  $v = dest$ :
```

```
        return true
```

```
    for each neighbour  $w$  of  $v$  in  $G$ :
```

```
        if visited[ $w$ ] = false:
```

```
            if dfsHasPathRec( $G$ ,  $w$ ,  $dest$ , visited):
```

```
                return true
```

```
    return false
```

Graph
Traversal

BFS

DFS

Recursive

Pseudocode

Example

Analysis

Path checking

Path finding

Iterative

Ideas/Issues

$O(V + E)$ when using the adjacency list representation:

- Algorithm is just a modified recursive DFS with return statements

Graph
Traversal

BFS

DFS

Recursive

Pseudocode

Example

Analysis

Path checking

Path finding

Iterative

Ideas/Issues

Knowing whether a path exists can be useful.

Knowing what the path is can be even more useful.

Idea:

- Record the predecessor of each vertex during the DFS
- Trace backwards through the path after the DFS

```
dfsFindPath( $G$ ,  $src$ ,  $dest$ ):
```

```
    Input: graph  $G$ , vertices  $src$  and  $dest$ 
```

```
    create predecessor array, initialised to -1
```

```
    predecessor[ $src$ ] =  $src$ 
```

```
    if dfsFindPathRec( $G$ ,  $src$ ,  $dest$ , predecessor):
```

```
         $v$  =  $dest$ 
```

```
        while  $v \neq src$ :
```

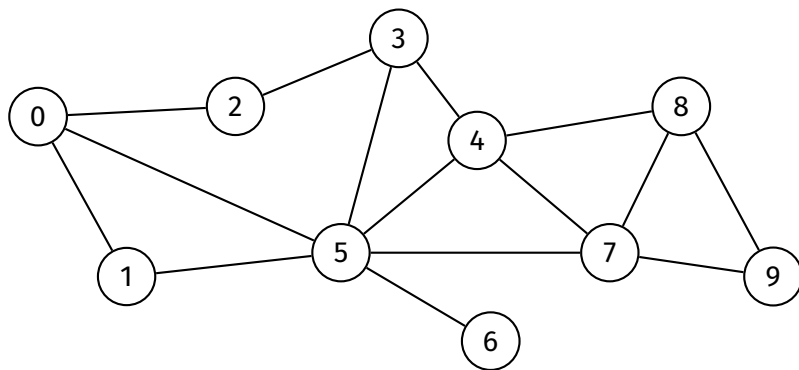
```
            print  $v$ , "<-"
```

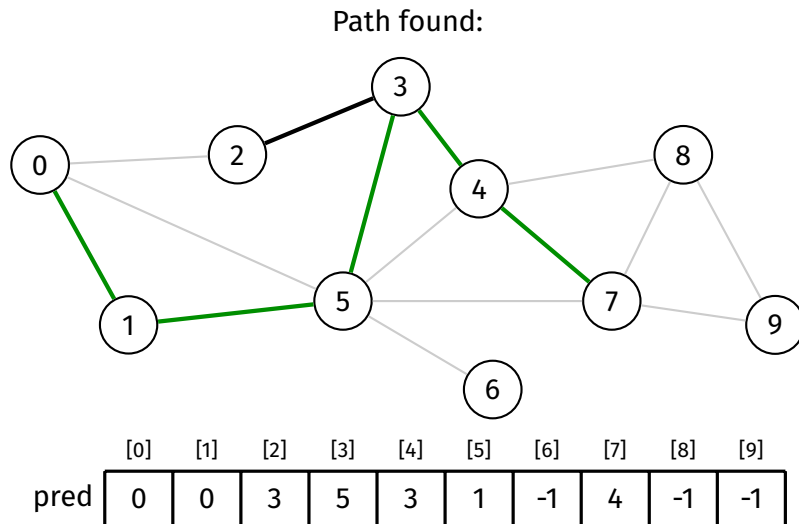
```
             $v$  = predecessor[ $v$ ]
```

```
    print  $src$ 
```

```
dfsFindPathRec( $G$ ,  $v$ ,  $dest$ , predecessor):  
    if  $v = dest$ :  
        return true  
  
    for each neighbour  $w$  of  $v$  in  $G$ :  
        if predecessor[ $w$ ] = -1:  
            predecessor[ $w$ ] =  $v$   
            if dfsFindPathRec( $G$ ,  $w$ ,  $dest$ , predecessor):  
                return true  
  
    return false
```


Find a path from 0 to 7





Clearly, DFS is not guaranteed to find the shortest path.

DFS can be implemented iteratively.

Iterative DFS is similar to BFS, but there are a few crucial differences:

- DFS uses a stack instead of a queue
- DFS marks a vertex as visited after removing it from the stack, not when adding it (which is what BFS does, but with a queue)

```
dfs( $G$ ,  $src$ ):
```

```
    Input: graph  $G$ , vertex  $src$ 
```

```
    create visited array, initialised to false
```

```
    create predecessor array, initialised to -1
```

```
    create stack  $S$ 
```

```
    push  $src$  onto  $S$ 
```

```
    while  $S$  is not empty:
```

```
         $v$  = pop from  $S$ 
```

```
        if visited[ $v$ ] = true:
```

```
            continue // i.e., return to start of loop
```

```
        visited[ $v$ ] = true
```

```
        for each neighbour  $w$  of  $v$  in  $G$  where visited[ $w$ ] = false:
```

```
            predecessor[ $w$ ] =  $v$ 
```

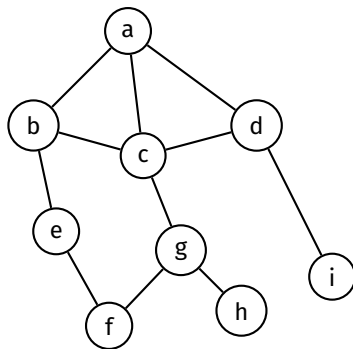
```
            push  $w$  onto  $S$ 
```

Iterative DFS is $O(V + E)$ when using the adjacency list representation.

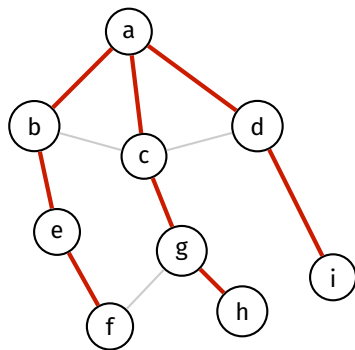
- Typical stack implementation has $O(1)$ push and pop
- Each vertex visited at most once $\Rightarrow O(V)$
- For each vertex, all of its edges are considered $\Rightarrow O(E)$

The edges traversed in a graph traversal form a **spanning tree**.

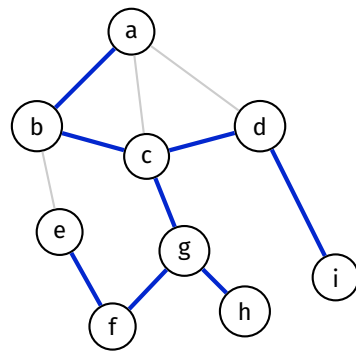
Consider the following graph:



A traversal starting at vertex 'a' forms the following spanning trees:

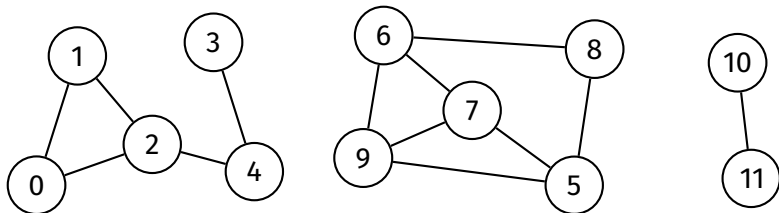


Breadth-first search



Depth-first search

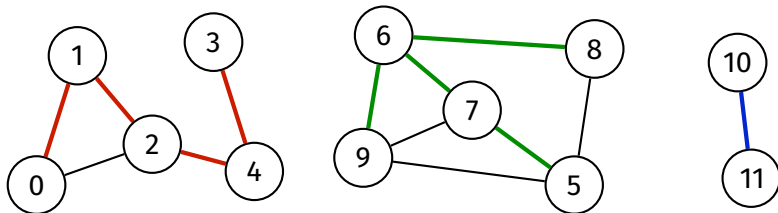
If a graph is not connected,
a graph traversal starting from a given vertex
will not traverse the entire graph



Solution

After initial traversal is complete,
perform traversal again on an unvisited vertex,
repeat until all vertices are visited

This produces a **spanning forest**



```
dfs( $G$ ):
```

```
    Input: graph  $G$ 
```

```
    create predecessor array, initialised to -1
```

```
    for each vertex  $v$  in  $G$ :
```

```
        if predecessor[ $v$ ] = -1:
```

```
            dfsRec( $G$ ,  $v$ , predecessor)
```

```
    ...
```

Graph
Traversal

BFS
DFS

Ideas/Issues
Spanning Trees
Disconnected
Graphs

<https://forms.office.com/r/zEqxUXvmLR>



Appendix

BFS Example
DFS Example
Path-Checking
Example

Appendix

Appendix

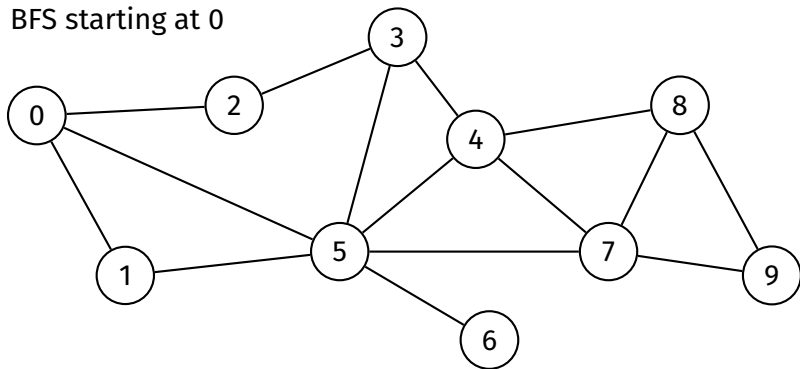
BFS Example

DFS Example

Path-Checking

Example

BFS starting at 0



	[0]	[1]	[2]	[3]	[4]	[5]	[6]	[7]	[8]	[9]
visited	0	0	0	0	0	0	0	0	0	0
pred	-1	-1	-1	-1	-1	-1	-1	-1	-1	-1

queue

Appendix

BFS Example

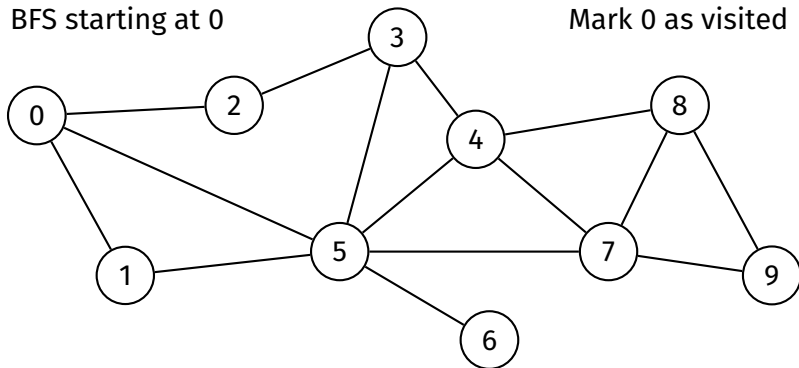
DFS Example

Path-Checking

Example

BFS starting at 0

Mark 0 as visited



	[0]	[1]	[2]	[3]	[4]	[5]	[6]	[7]	[8]	[9]
visited	1	0	0	0	0	0	0	0	0	0
pred	-1	-1	-1	-1	-1	-1	-1	-1	-1	-1

queue 0

Appendix

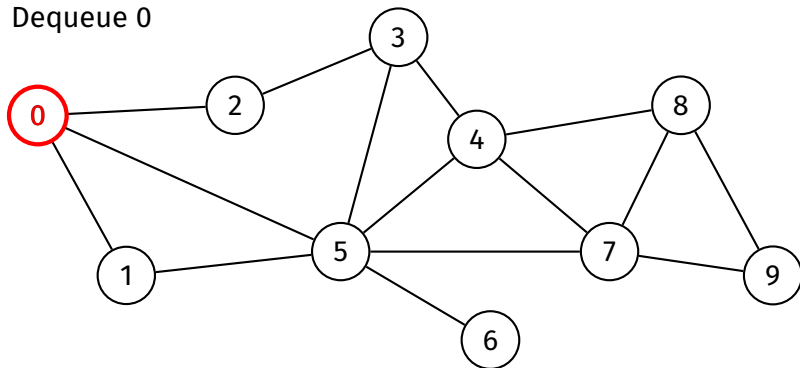
BFS Example

DFS Example

Path-Checking

Example

Dequeue 0



	[0]	[1]	[2]	[3]	[4]	[5]	[6]	[7]	[8]	[9]
visited	1	0	0	0	0	0	0	0	0	0
pred	-1	-1	-1	-1	-1	-1	-1	-1	-1	-1

queue 0

Appendix

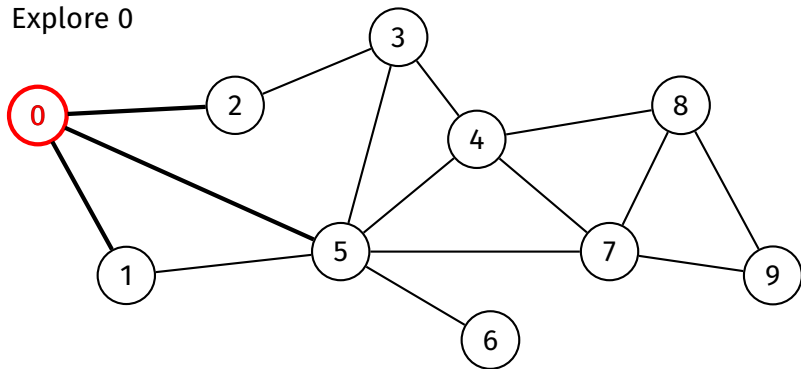
BFS Example

DFS Example

Path-Checking

Example

Explore 0



	[0]	[1]	[2]	[3]	[4]	[5]	[6]	[7]	[8]	[9]
visited	1	0	0	0	0	0	0	0	0	0
pred	-1	-1	-1	-1	-1	-1	-1	-1	-1	-1

queue 0

Appendix

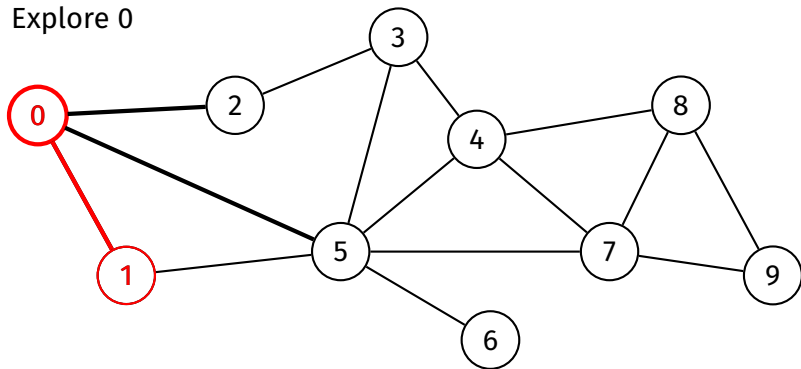
BFS Example

DFS Example

Path-Checking

Example

Explore 0



	[0]	[1]	[2]	[3]	[4]	[5]	[6]	[7]	[8]	[9]
visited	1	0	0	0	0	0	0	0	0	0
pred	-1	-1	-1	-1	-1	-1	-1	-1	-1	-1

queue 0

Appendix

BFS Example

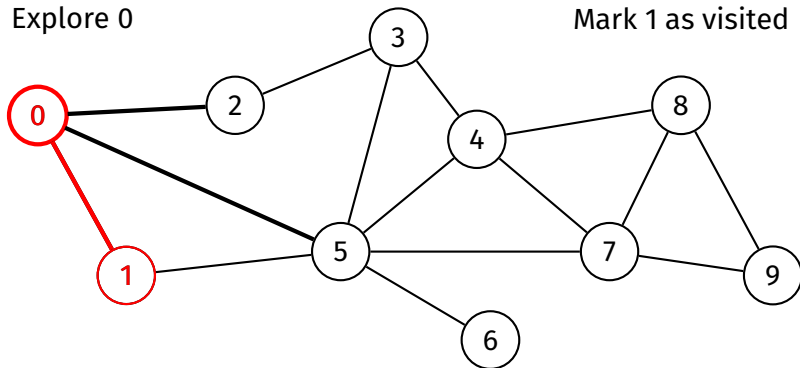
DFS Example

Path-Checking

Example

Explore 0

Mark 1 as visited



	[0]	[1]	[2]	[3]	[4]	[5]	[6]	[7]	[8]	[9]
visited	1	1	0	0	0	0	0	0	0	0
pred	-1	0	-1	-1	-1	-1	-1	-1	-1	-1

queue 0 1

Appendix

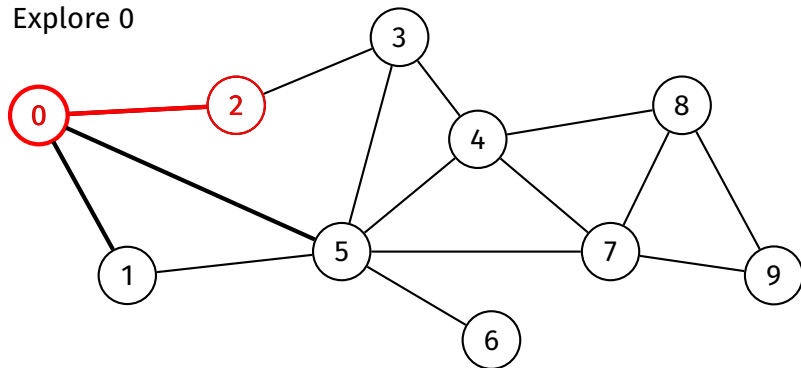
BFS Example

DFS Example

Path-Checking

Example

Explore 0



	[0]	[1]	[2]	[3]	[4]	[5]	[6]	[7]	[8]	[9]
visited	1	1	0	0	0	0	0	0	0	0
pred	-1	0	-1	-1	-1	-1	-1	-1	-1	-1

queue 0 1

Appendix

BFS Example

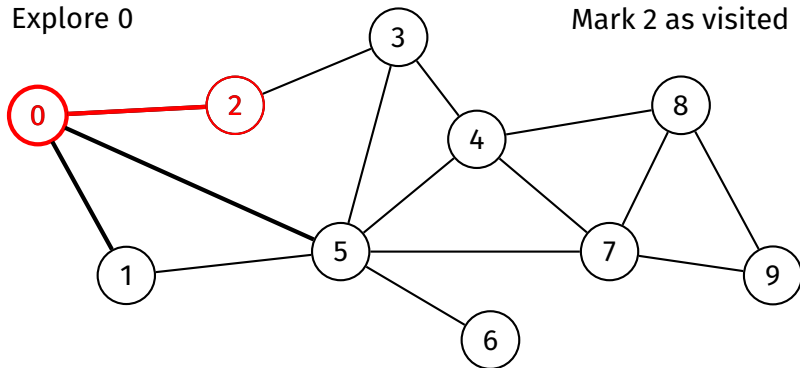
DFS Example

Path-Checking

Example

Explore 0

Mark 2 as visited



	[0]	[1]	[2]	[3]	[4]	[5]	[6]	[7]	[8]	[9]
visited	1	1	1	0	0	0	0	0	0	0
pred	-1	0	0	-1	-1	-1	-1	-1	-1	-1

queue 0 1 2

Appendix

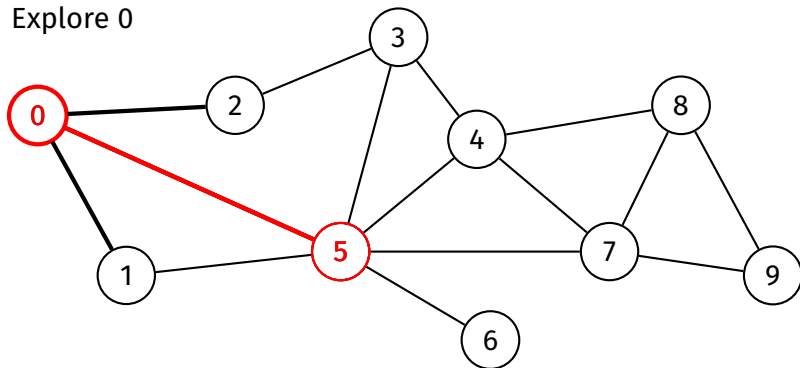
BFS Example

DFS Example

Path-Checking

Example

Explore 0

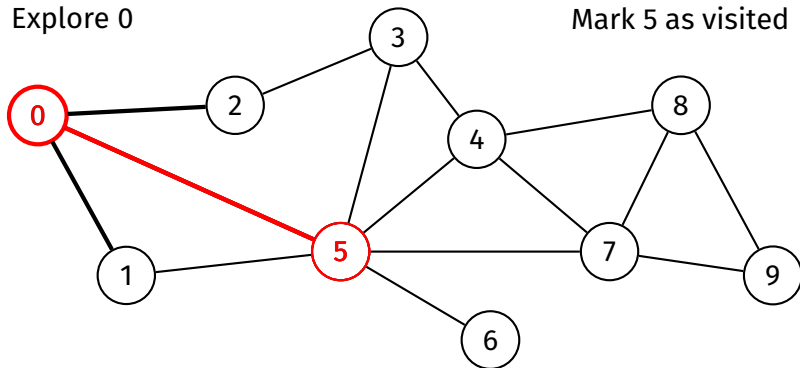


	[0]	[1]	[2]	[3]	[4]	[5]	[6]	[7]	[8]	[9]
visited	1	1	1	0	0	0	0	0	0	0
pred	-1	0	0	-1	-1	-1	-1	-1	-1	-1

queue 0 1 2

Explore 0

Mark 5 as visited



	[0]	[1]	[2]	[3]	[4]	[5]	[6]	[7]	[8]	[9]
visited	1	1	1	0	0	1	0	0	0	0
pred	-1	0	0	-1	-1	0	-1	-1	-1	-1

queue 0 1 2 5

Appendix

BFS Example

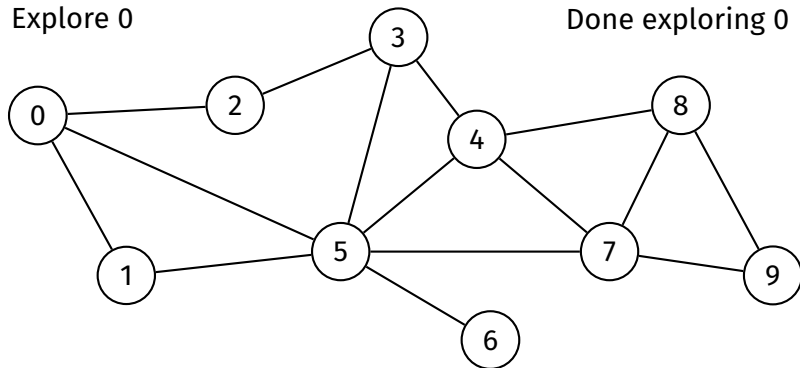
DFS Example

Path-Checking

Example

Explore 0

Done exploring 0



	[0]	[1]	[2]	[3]	[4]	[5]	[6]	[7]	[8]	[9]
visited	1	1	1	0	0	1	0	0	0	0
pred	-1	0	0	-1	-1	0	-1	-1	-1	-1

queue 0 1 2 5

Appendix

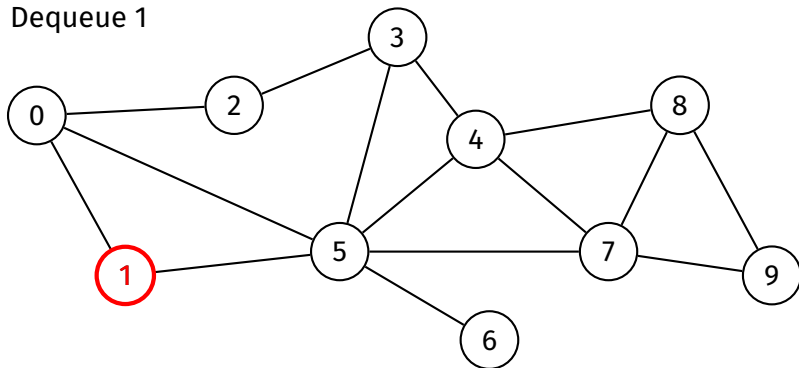
BFS Example

DFS Example

Path-Checking

Example

Dequeue 1



	[0]	[1]	[2]	[3]	[4]	[5]	[6]	[7]	[8]	[9]
visited	1	1	1	0	0	1	0	0	0	0
pred	-1	0	0	-1	-1	0	-1	-1	-1	-1

queue 0 1 2 5

Appendix

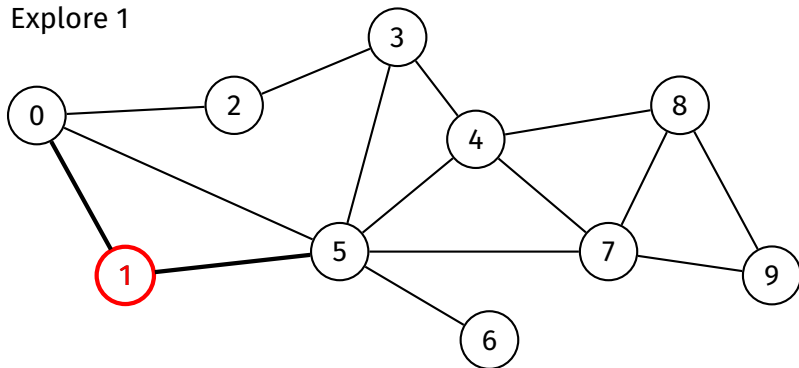
BFS Example

DFS Example

Path-Checking

Example

Explore 1



	[0]	[1]	[2]	[3]	[4]	[5]	[6]	[7]	[8]	[9]
visited	1	1	1	0	0	1	0	0	0	0
pred	-1	0	0	-1	-1	0	-1	-1	-1	-1

queue 0 1 2 5

Appendix

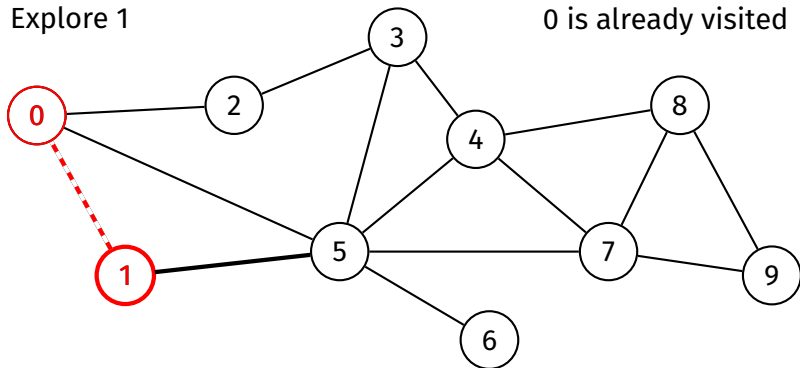
BFS Example

DFS Example

Path-Checking

Example

Explore 1



	[0]	[1]	[2]	[3]	[4]	[5]	[6]	[7]	[8]	[9]
visited	1	1	1	0	0	1	0	0	0	0
pred	-1	0	0	-1	-1	0	-1	-1	-1	-1

queue 0 1 2 5

Appendix

BFS Example

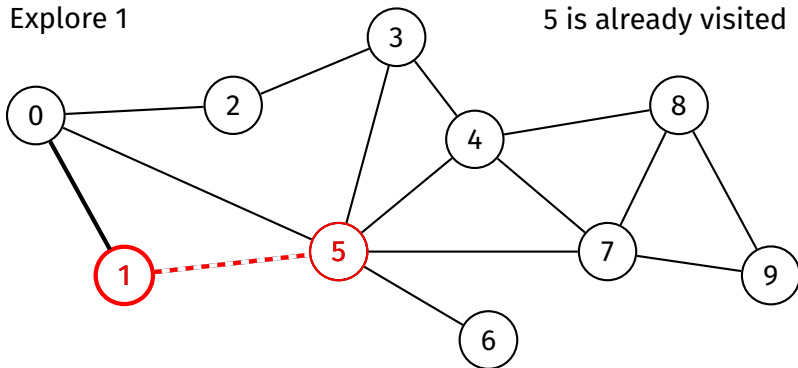
DFS Example

Path-Checking

Example

Explore 1

5 is already visited



	[0]	[1]	[2]	[3]	[4]	[5]	[6]	[7]	[8]	[9]
visited	1	1	1	0	0	1	0	0	0	0
pred	-1	0	0	-1	-1	0	-1	-1	-1	-1

queue 0 1 2 5

Appendix

BFS Example

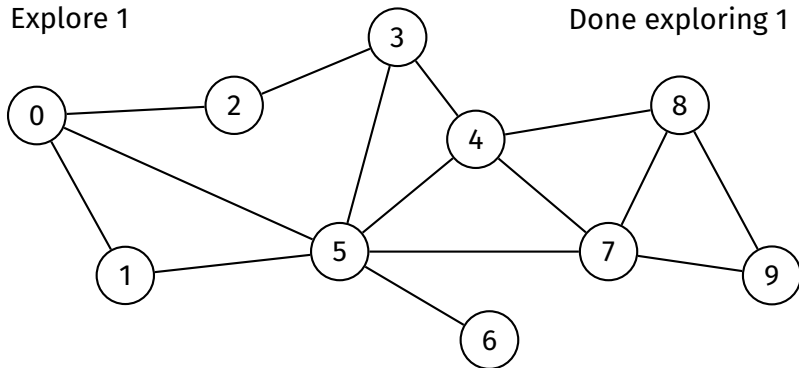
DFS Example

Path-Checking

Example

Explore 1

Done exploring 1



	[0]	[1]	[2]	[3]	[4]	[5]	[6]	[7]	[8]	[9]
visited	1	1	1	0	0	1	0	0	0	0
pred	-1	0	0	-1	-1	0	-1	-1	-1	-1

queue 0 1 2 5

Appendix

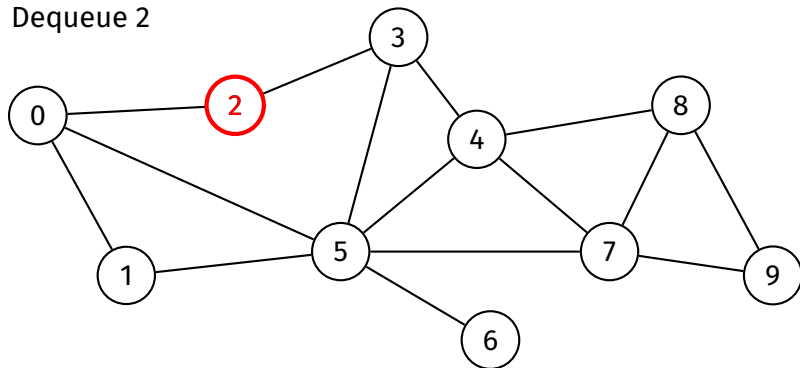
BFS Example

DFS Example

Path-Checking

Example

Dequeue 2



	[0]	[1]	[2]	[3]	[4]	[5]	[6]	[7]	[8]	[9]
visited	1	1	1	0	0	1	0	0	0	0
pred	-1	0	0	-1	-1	0	-1	-1	-1	-1

queue 0 1 2 5

Appendix

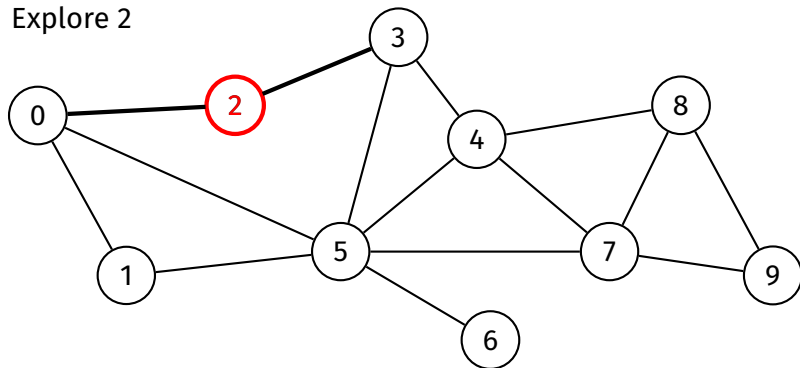
BFS Example

DFS Example

Path-Checking

Example

Explore 2

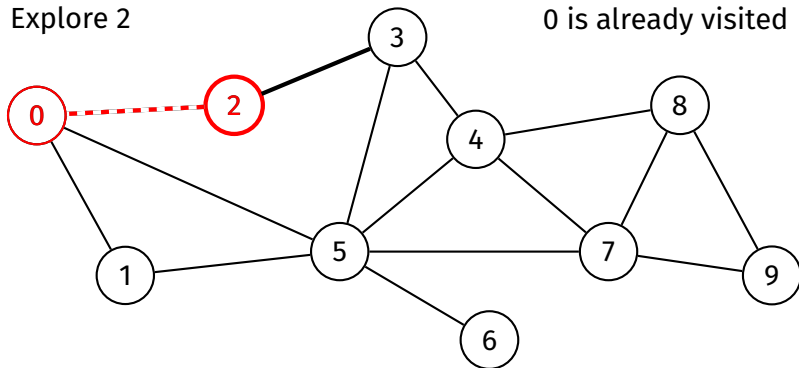


	[0]	[1]	[2]	[3]	[4]	[5]	[6]	[7]	[8]	[9]
visited	1	1	1	0	0	1	0	0	0	0
pred	-1	0	0	-1	-1	0	-1	-1	-1	-1

queue 0 1 2 5

Explore 2

0 is already visited



	[0]	[1]	[2]	[3]	[4]	[5]	[6]	[7]	[8]	[9]
visited	1	1	1	0	0	1	0	0	0	0
pred	-1	0	0	-1	-1	0	-1	-1	-1	-1

queue 0 1 2 5

Appendix

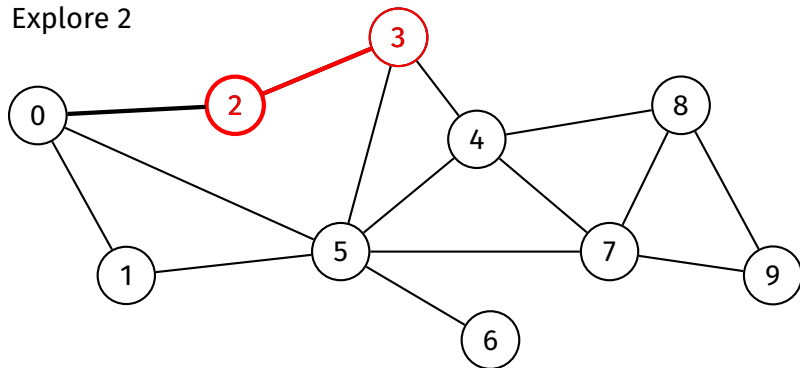
BFS Example

DFS Example

Path-Checking

Example

Explore 2



	[0]	[1]	[2]	[3]	[4]	[5]	[6]	[7]	[8]	[9]
visited	1	1	1	0	0	1	0	0	0	0
pred	-1	0	0	-1	-1	0	-1	-1	-1	-1

queue 0 1 2 5

Appendix

BFS Example

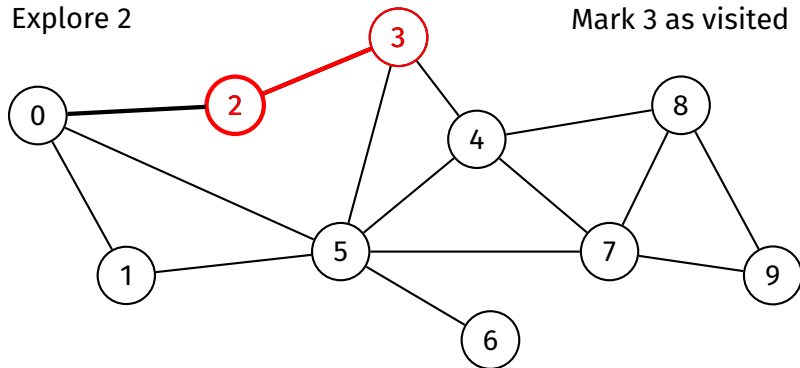
DFS Example

Path-Checking

Example

Explore 2

Mark 3 as visited



	[0]	[1]	[2]	[3]	[4]	[5]	[6]	[7]	[8]	[9]
visited	1	1	1	1	0	1	0	0	0	0
pred	-1	0	0	2	-1	0	-1	-1	-1	-1

queue 0 1 2 5 3

Appendix

BFS Example

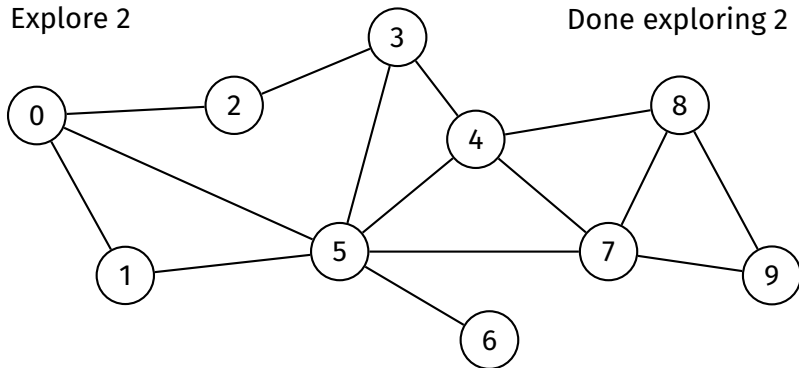
DFS Example

Path-Checking

Example

Explore 2

Done exploring 2



	[0]	[1]	[2]	[3]	[4]	[5]	[6]	[7]	[8]	[9]
visited	1	1	1	1	0	1	0	0	0	0
pred	-1	0	0	2	-1	0	-1	-1	-1	-1

queue 0 1 2 5 3

Appendix

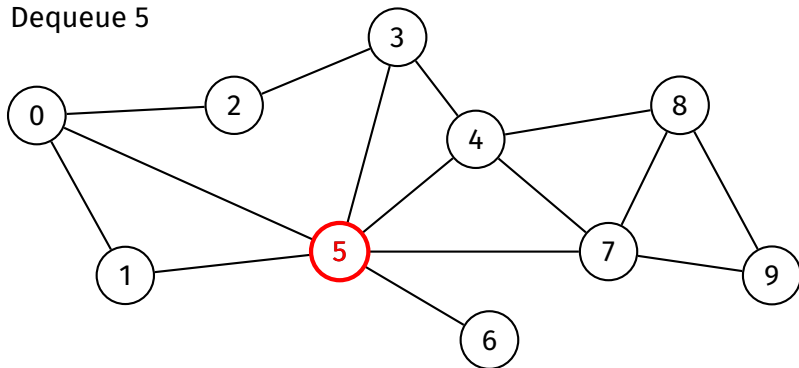
BFS Example

DFS Example

Path-Checking

Example

Dequeue 5



	[0]	[1]	[2]	[3]	[4]	[5]	[6]	[7]	[8]	[9]
visited	1	1	1	1	0	1	0	0	0	0
pred	-1	0	0	2	-1	0	-1	-1	-1	-1

queue 0 1 2 5 3

Appendix

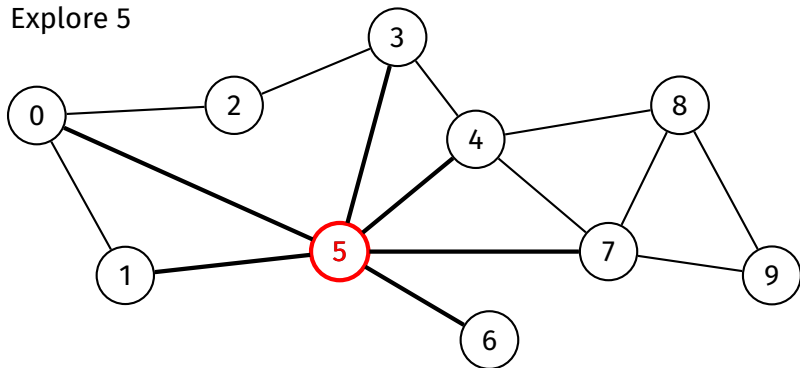
BFS Example

DFS Example

Path-Checking

Example

Explore 5



	[0]	[1]	[2]	[3]	[4]	[5]	[6]	[7]	[8]	[9]
visited	1	1	1	1	0	1	0	0	0	0
pred	-1	0	0	2	-1	0	-1	-1	-1	-1

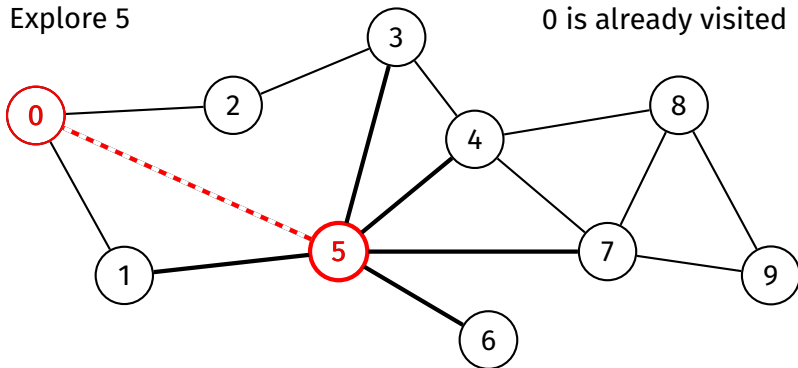
queue 0 1 2 5 3

Appendix

BFS Example
DFS Example
Path-Checking
Example

Explore 5

0 is already visited



	[0]	[1]	[2]	[3]	[4]	[5]	[6]	[7]	[8]	[9]
visited	1	1	1	1	0	1	0	0	0	0
pred	-1	0	0	2	-1	0	-1	-1	-1	-1

queue 0 1 2 5 3

Appendix

BFS Example

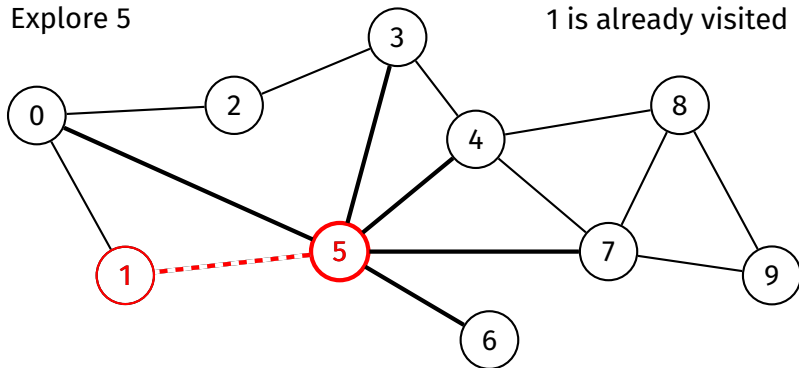
DFS Example

Path-Checking

Example

Explore 5

1 is already visited

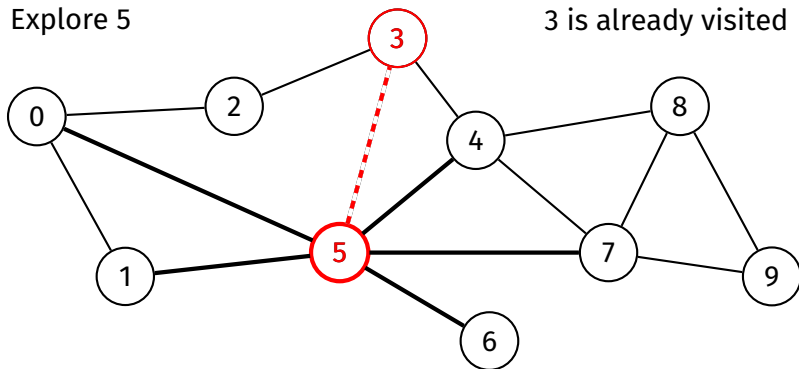


	[0]	[1]	[2]	[3]	[4]	[5]	[6]	[7]	[8]	[9]
visited	1	1	1	1	0	1	0	0	0	0
pred	-1	0	0	2	-1	0	-1	-1	-1	-1

queue 0 1 2 5 3

Explore 5

3 is already visited



	[0]	[1]	[2]	[3]	[4]	[5]	[6]	[7]	[8]	[9]
visited	1	1	1	1	0	1	0	0	0	0
pred	-1	0	0	2	-1	0	-1	-1	-1	-1

queue 0 1 2 5 3

Appendix

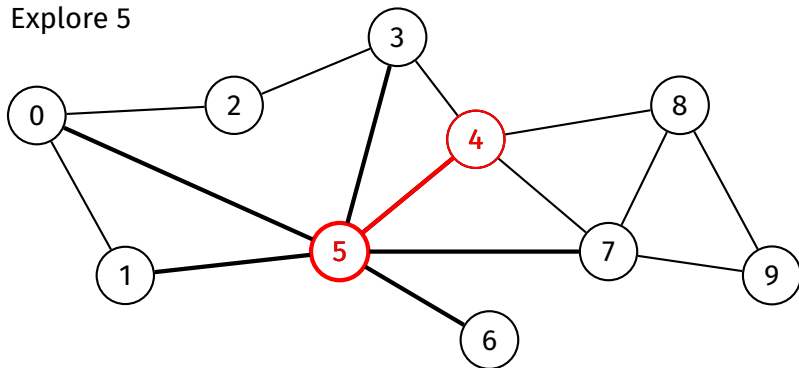
BFS Example

DFS Example

Path-Checking

Example

Explore 5



	[0]	[1]	[2]	[3]	[4]	[5]	[6]	[7]	[8]	[9]
visited	1	1	1	1	0	1	0	0	0	0
pred	-1	0	0	2	-1	0	-1	-1	-1	-1

queue 0 1 2 5 3

Appendix

BFS Example

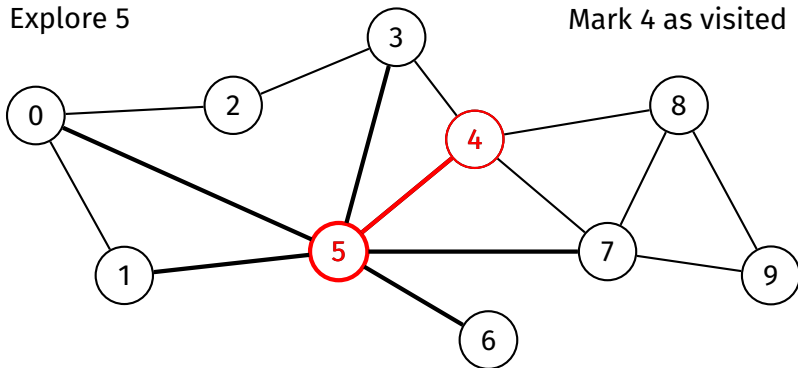
DFS Example

Path-Checking

Example

Explore 5

Mark 4 as visited



	[0]	[1]	[2]	[3]	[4]	[5]	[6]	[7]	[8]	[9]
visited	1	1	1	1	1	1	0	0	0	0
pred	-1	0	0	2	5	0	-1	-1	-1	-1

queue 0 1 2 5 3 4

Appendix

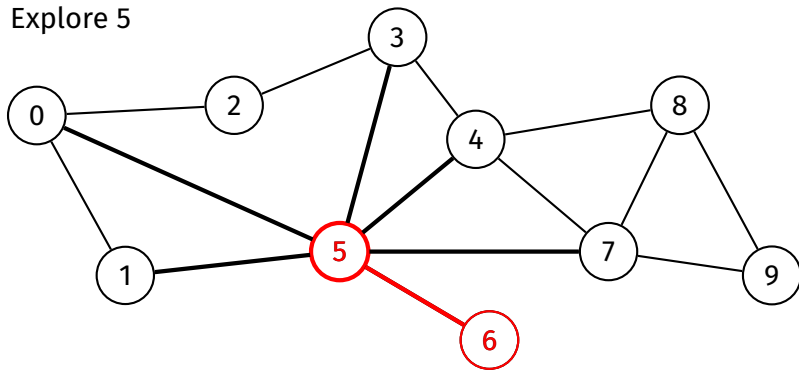
BFS Example

DFS Example

Path-Checking

Example

Explore 5



	[0]	[1]	[2]	[3]	[4]	[5]	[6]	[7]	[8]	[9]
visited	1	1	1	1	1	1	0	0	0	0
pred	-1	0	0	2	5	0	-1	-1	-1	-1

queue 0 1 2 5 3 4

Appendix

BFS Example

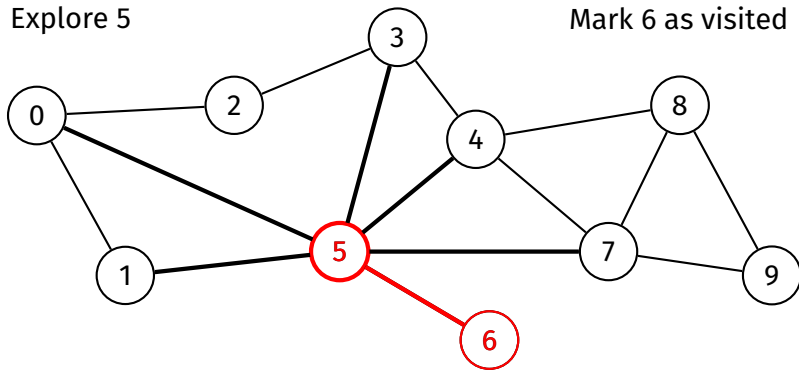
DFS Example

Path-Checking

Example

Explore 5

Mark 6 as visited



	[0]	[1]	[2]	[3]	[4]	[5]	[6]	[7]	[8]	[9]
visited	1	1	1	1	1	1	1	0	0	0
pred	-1	0	0	2	5	0	5	-1	-1	-1

queue 0 1 2 5 3 4 6

Appendix

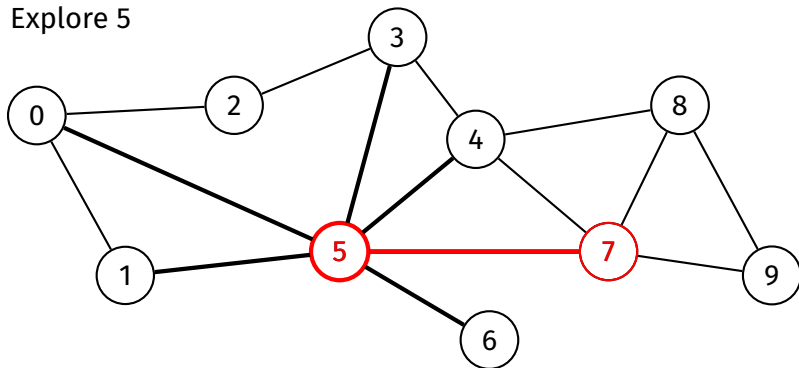
BFS Example

DFS Example

Path-Checking

Example

Explore 5



	[0]	[1]	[2]	[3]	[4]	[5]	[6]	[7]	[8]	[9]
visited	1	1	1	1	1	1	1	0	0	0
pred	-1	0	0	2	5	0	5	-1	-1	-1

queue 0 1 2 5 3 4 6

Appendix

BFS Example

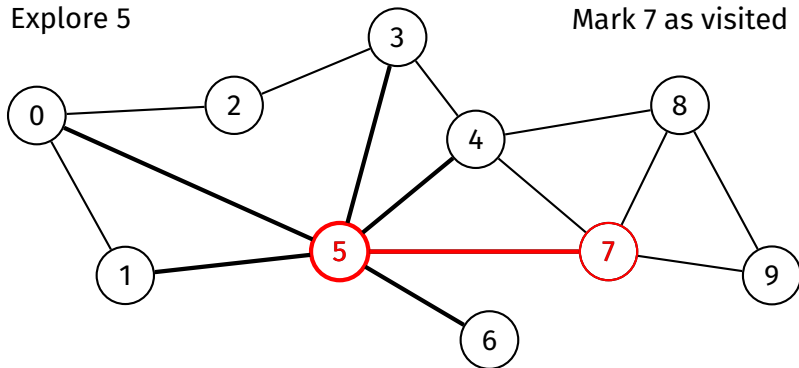
DFS Example

Path-Checking

Example

Explore 5

Mark 7 as visited



	[0]	[1]	[2]	[3]	[4]	[5]	[6]	[7]	[8]	[9]
visited	1	1	1	1	1	1	1	1	0	0
pred	-1	0	0	2	5	0	5	5	-1	-1

queue 0 1 2 5 3 4 6 7

Appendix

BFS Example

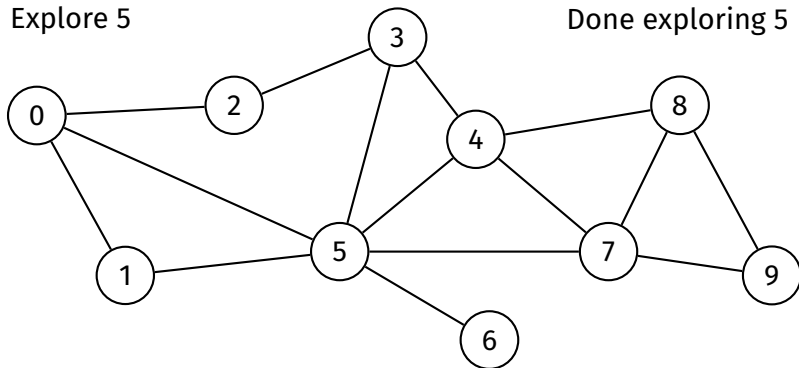
DFS Example

Path-Checking

Example

Explore 5

Done exploring 5



	[0]	[1]	[2]	[3]	[4]	[5]	[6]	[7]	[8]	[9]
visited	1	1	1	1	1	1	1	1	0	0
pred	-1	0	0	2	5	0	5	5	-1	-1

queue 0 1 2 5 3 4 6 7

Appendix

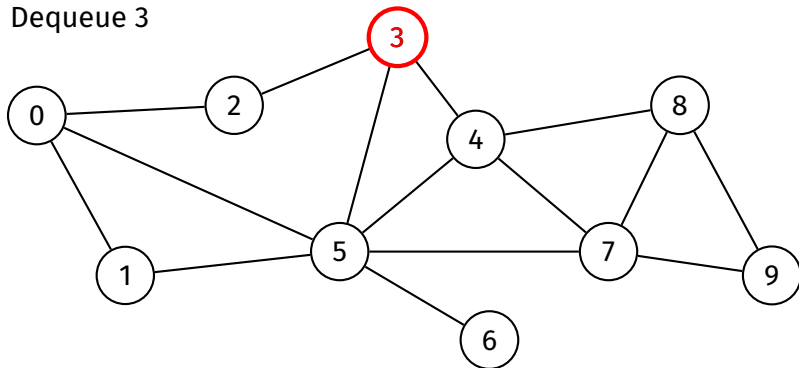
BFS Example

DFS Example

Path-Checking

Example

Dequeue 3



	[0]	[1]	[2]	[3]	[4]	[5]	[6]	[7]	[8]	[9]
visited	1	1	1	1	1	1	1	1	0	0
pred	-1	0	0	2	5	0	5	5	-1	-1

queue 0 1 2 5 3 4 6 7

Appendix

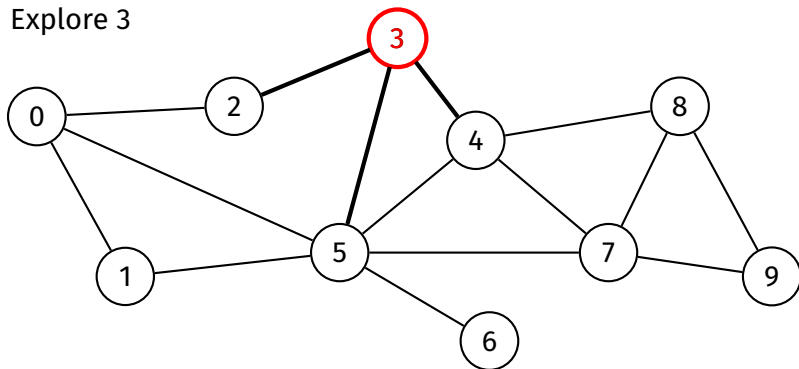
BFS Example

DFS Example

Path-Checking

Example

Explore 3



	[0]	[1]	[2]	[3]	[4]	[5]	[6]	[7]	[8]	[9]
visited	1	1	1	1	1	1	1	1	0	0
pred	-1	0	0	2	5	0	5	5	-1	-1

queue 0 1 2 5 3 4 6 7

Appendix

BFS Example

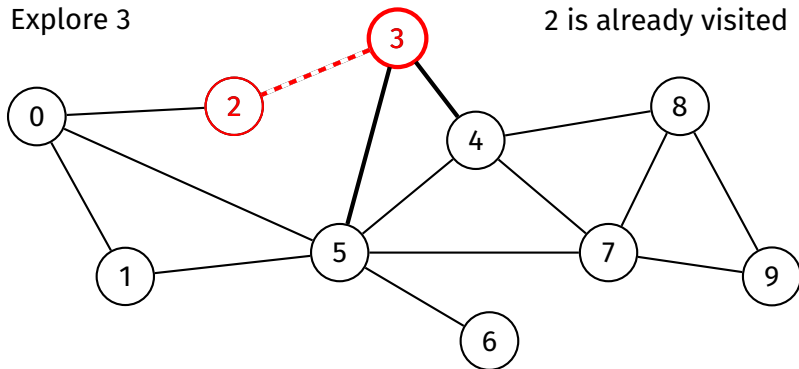
DFS Example

Path-Checking

Example

Explore 3

2 is already visited



	[0]	[1]	[2]	[3]	[4]	[5]	[6]	[7]	[8]	[9]
visited	1	1	1	1	1	1	1	1	0	0
pred	-1	0	0	2	5	0	5	5	-1	-1

queue 0 1 2 5 3 4 6 7

Appendix

BFS Example

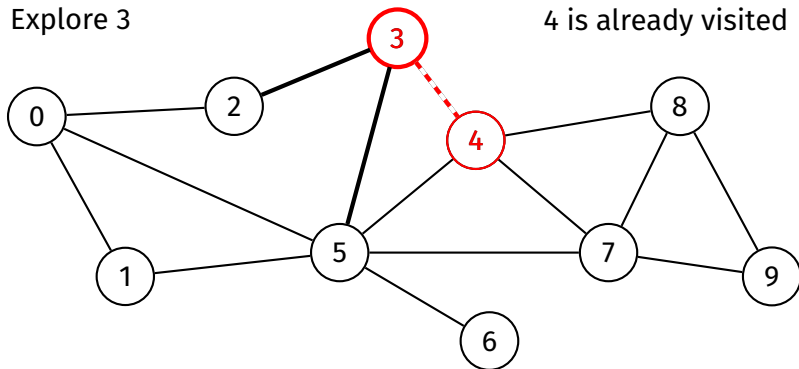
DFS Example

Path-Checking

Example

Explore 3

4 is already visited



	[0]	[1]	[2]	[3]	[4]	[5]	[6]	[7]	[8]	[9]
visited	1	1	1	1	1	1	1	1	0	0
pred	-1	0	0	2	5	0	5	5	-1	-1

queue 0 1 2 5 3 4 6 7

Appendix

BFS Example

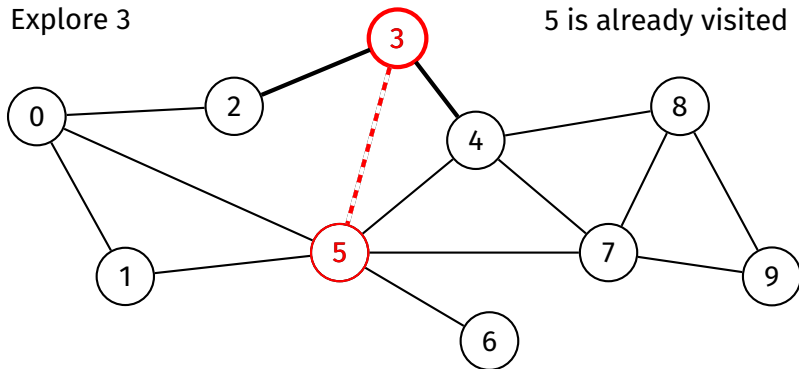
DFS Example

Path-Checking

Example

Explore 3

5 is already visited



	[0]	[1]	[2]	[3]	[4]	[5]	[6]	[7]	[8]	[9]
visited	1	1	1	1	1	1	1	1	0	0
pred	-1	0	0	2	5	0	5	5	-1	-1

queue 0 1 2 5 3 4 6 7

Appendix

BFS Example

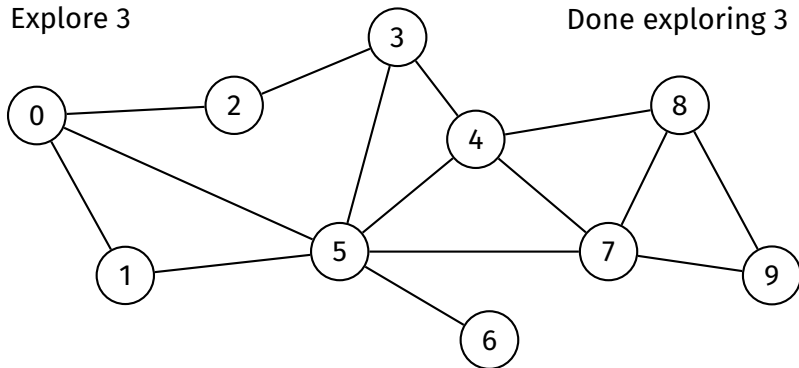
DFS Example

Path-Checking

Example

Explore 3

Done exploring 3



	[0]	[1]	[2]	[3]	[4]	[5]	[6]	[7]	[8]	[9]
visited	1	1	1	1	1	1	1	1	0	0
pred	-1	0	0	2	5	0	5	5	-1	-1

queue 0 1 2 5 3 4 6 7

Appendix

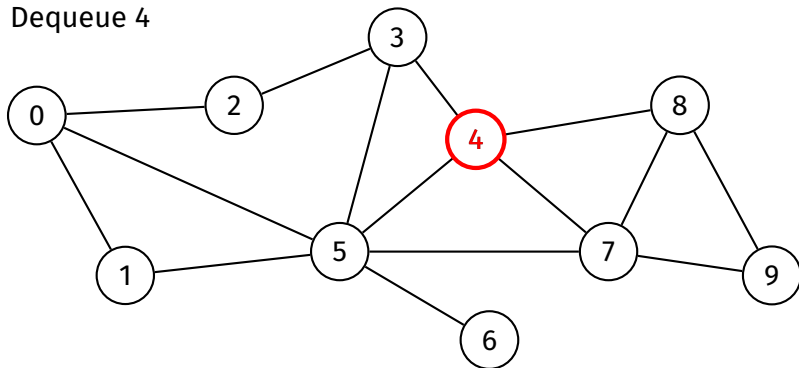
BFS Example

DFS Example

Path-Checking

Example

Dequeue 4



	[0]	[1]	[2]	[3]	[4]	[5]	[6]	[7]	[8]	[9]
visited	1	1	1	1	1	1	1	1	0	0
pred	-1	0	0	2	5	0	5	5	-1	-1

queue 0 1 2 5 3 4 6 7

Appendix

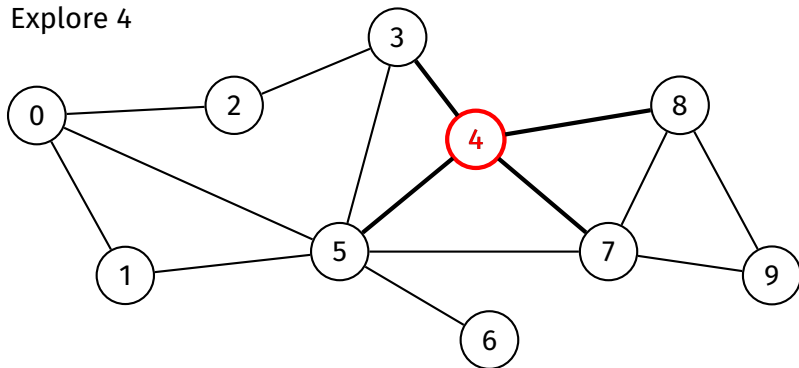
BFS Example

DFS Example

Path-Checking

Example

Explore 4



	[0]	[1]	[2]	[3]	[4]	[5]	[6]	[7]	[8]	[9]
visited	1	1	1	1	1	1	1	1	0	0
pred	-1	0	0	2	5	0	5	5	-1	-1

queue 0 1 2 5 3 4 6 7

Appendix

BFS Example

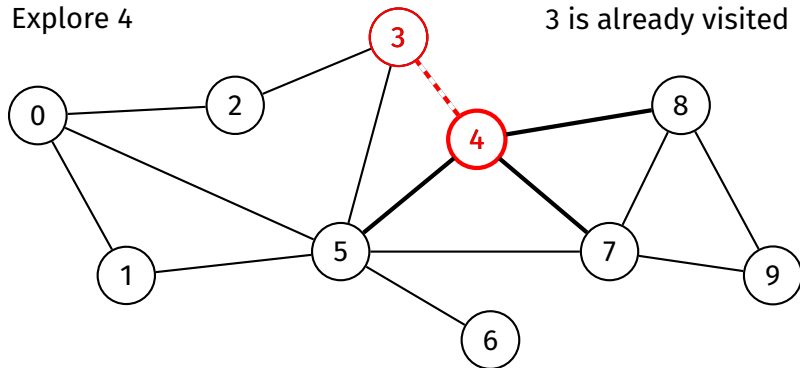
DFS Example

Path-Checking

Example

Explore 4

3 is already visited



	[0]	[1]	[2]	[3]	[4]	[5]	[6]	[7]	[8]	[9]
visited	1	1	1	1	1	1	1	1	0	0
pred	-1	0	0	2	5	0	5	5	-1	-1

queue 0 1 2 5 3 4 6 7

Appendix

BFS Example

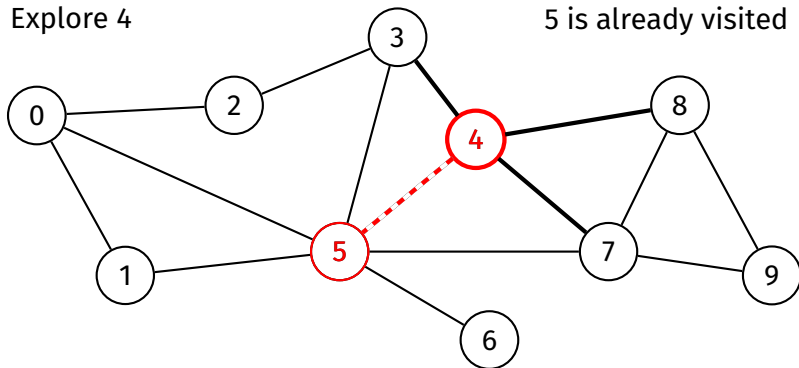
DFS Example

Path-Checking

Example

Explore 4

5 is already visited



	[0]	[1]	[2]	[3]	[4]	[5]	[6]	[7]	[8]	[9]
visited	1	1	1	1	1	1	1	1	0	0
pred	-1	0	0	2	5	0	5	5	-1	-1

queue 0 1 2 5 3 4 6 7

Appendix

BFS Example

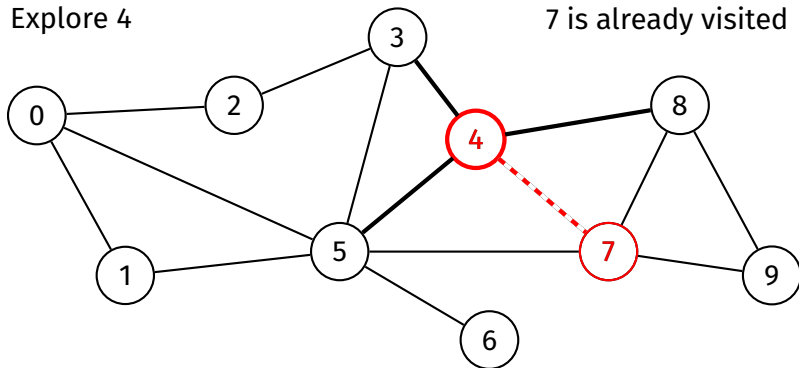
DFS Example

Path-Checking

Example

Explore 4

7 is already visited



	[0]	[1]	[2]	[3]	[4]	[5]	[6]	[7]	[8]	[9]
visited	1	1	1	1	1	1	1	1	0	0
pred	-1	0	0	2	5	0	5	5	-1	-1

queue 0 1 2 5 3 4 6 7

Appendix

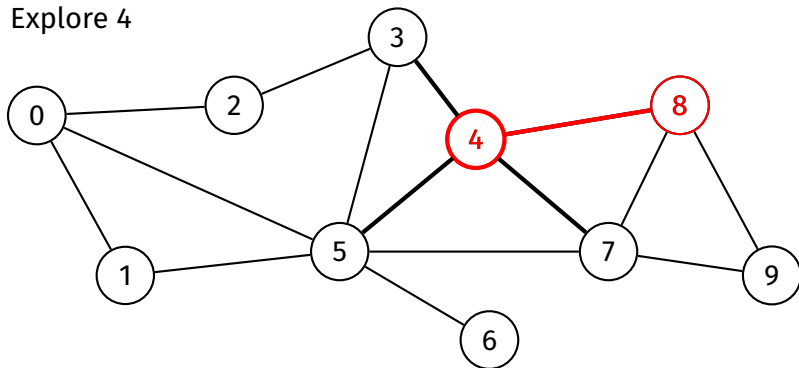
BFS Example

DFS Example

Path-Checking

Example

Explore 4



	[0]	[1]	[2]	[3]	[4]	[5]	[6]	[7]	[8]	[9]
visited	1	1	1	1	1	1	1	1	0	0
pred	-1	0	0	2	5	0	5	5	-1	-1

queue 0 1 2 5 3 4 6 7

Appendix

BFS Example

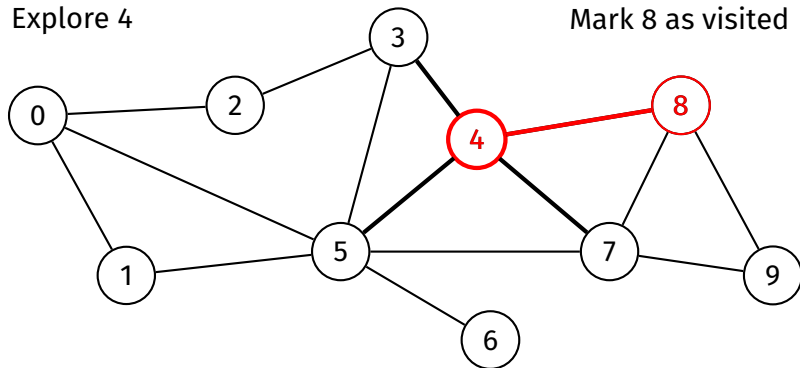
DFS Example

Path-Checking

Example

Explore 4

Mark 8 as visited



	[0]	[1]	[2]	[3]	[4]	[5]	[6]	[7]	[8]	[9]
visited	1	1	1	1	1	1	1	1	1	0
pred	-1	0	0	2	5	0	5	5	4	-1

queue 0 1 2 5 3 4 6 7 8

Appendix

BFS Example

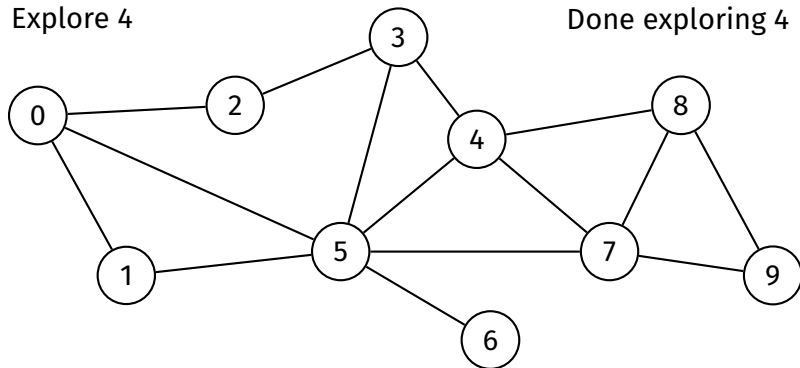
DFS Example

Path-Checking

Example

Explore 4

Done exploring 4



	[0]	[1]	[2]	[3]	[4]	[5]	[6]	[7]	[8]	[9]
visited	1	1	1	1	1	1	1	1	1	0
pred	-1	0	0	2	5	0	5	5	4	-1

queue 0 1 2 5 3 4 6 7 8

Appendix

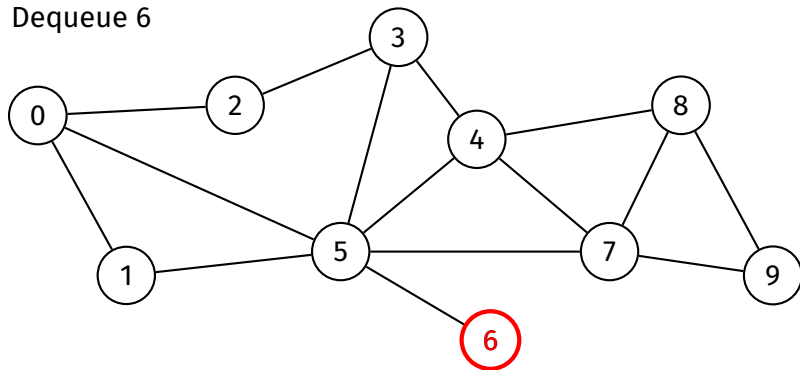
BFS Example

DFS Example

Path-Checking

Example

Dequeue 6



	[0]	[1]	[2]	[3]	[4]	[5]	[6]	[7]	[8]	[9]
visited	1	1	1	1	1	1	1	1	1	0
pred	-1	0	0	2	5	0	5	5	4	-1

queue 0 1 2 5 3 4 6 7 8

Appendix

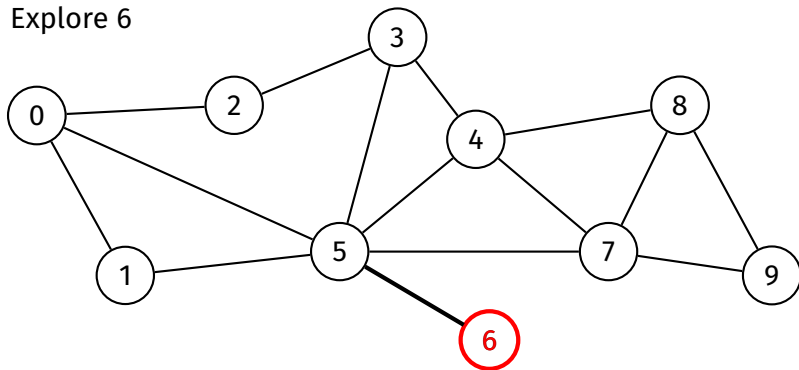
BFS Example

DFS Example

Path-Checking

Example

Explore 6



	[0]	[1]	[2]	[3]	[4]	[5]	[6]	[7]	[8]	[9]
visited	1	1	1	1	1	1	1	1	1	0
pred	-1	0	0	2	5	0	5	5	4	-1

queue 0 1 2 5 3 4 6 7 8

Appendix

BFS Example

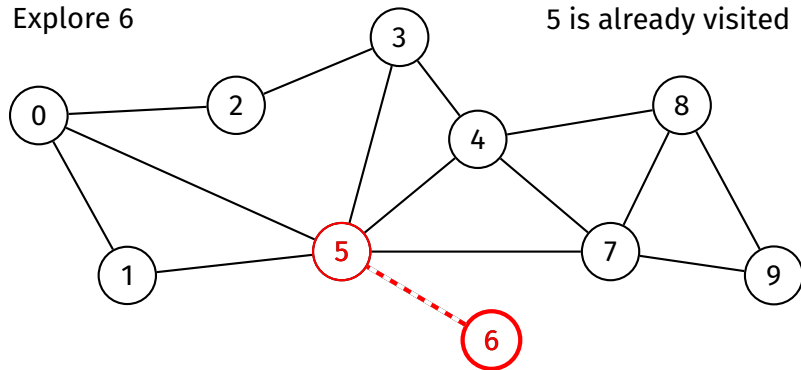
DFS Example

Path-Checking

Example

Explore 6

5 is already visited



	[0]	[1]	[2]	[3]	[4]	[5]	[6]	[7]	[8]	[9]
visited	1	1	1	1	1	1	1	1	1	0
pred	-1	0	0	2	5	0	5	5	4	-1

queue 0 1 2 5 3 4 6 7 8

Appendix

BFS Example

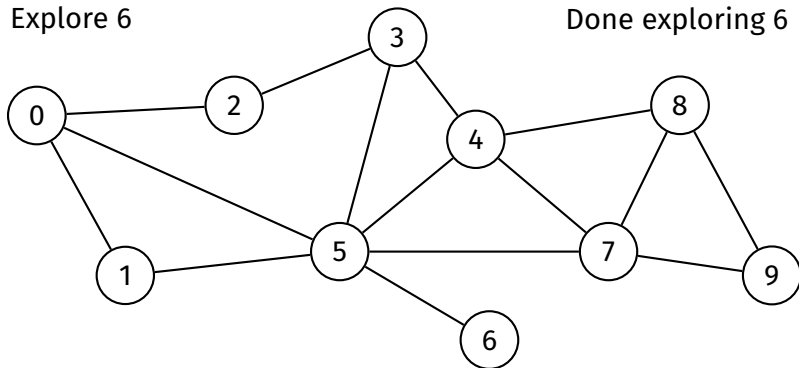
DFS Example

Path-Checking

Example

Explore 6

Done exploring 6



	[0]	[1]	[2]	[3]	[4]	[5]	[6]	[7]	[8]	[9]
visited	1	1	1	1	1	1	1	1	1	0
pred	-1	0	0	2	5	0	5	5	4	-1

queue 0 1 2 5 3 4 6 7 8

Appendix

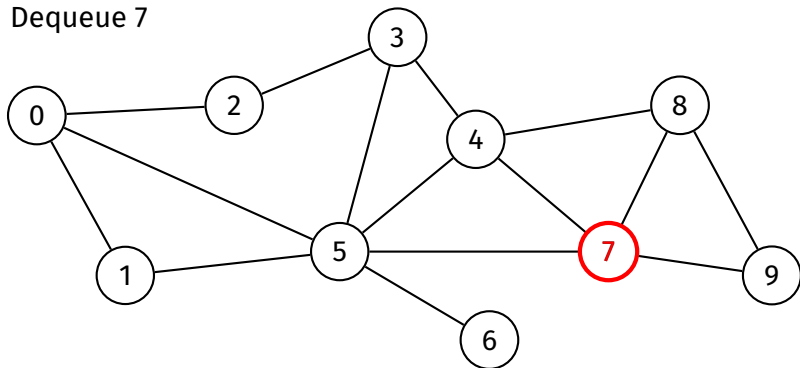
BFS Example

DFS Example

Path-Checking

Example

Dequeue 7



	[0]	[1]	[2]	[3]	[4]	[5]	[6]	[7]	[8]	[9]
visited	1	1	1	1	1	1	1	1	1	0
pred	-1	0	0	2	5	0	5	5	4	-1

queue 0 1 2 5 3 4 6 7 8

Appendix

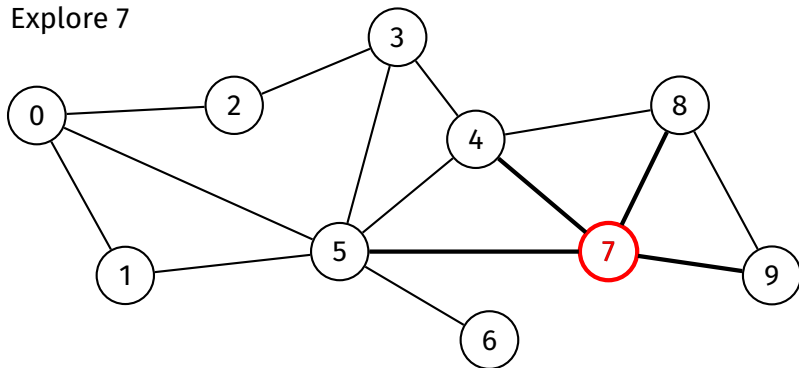
BFS Example

DFS Example

Path-Checking

Example

Explore 7



	[0]	[1]	[2]	[3]	[4]	[5]	[6]	[7]	[8]	[9]
visited	1	1	1	1	1	1	1	1	1	0
pred	-1	0	0	2	5	0	5	5	4	-1

queue 0 1 2 5 3 4 6 7 8

Appendix

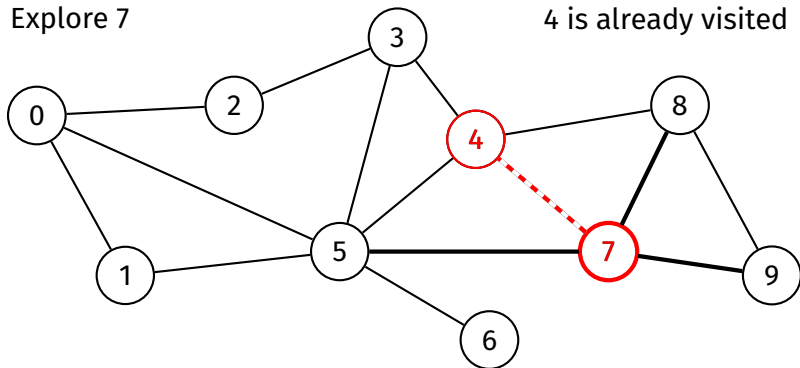
BFS Example

DFS Example

Path-Checking

Example

Explore 7



	[0]	[1]	[2]	[3]	[4]	[5]	[6]	[7]	[8]	[9]
visited	1	1	1	1	1	1	1	1	1	0
pred	-1	0	0	2	5	0	5	5	4	-1

queue 0 1 2 5 3 4 6 7 8

Appendix

BFS Example

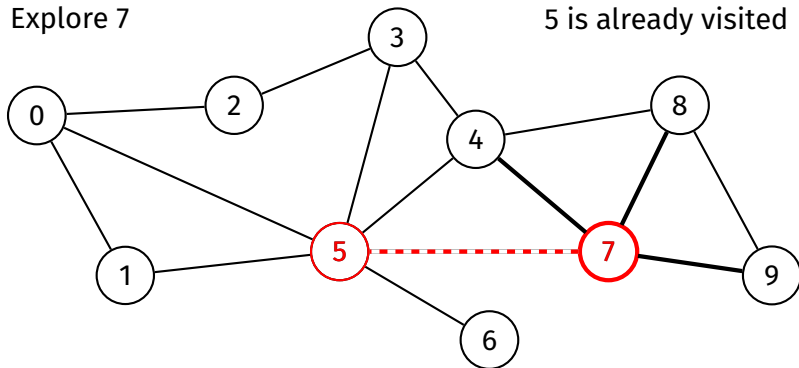
DFS Example

Path-Checking

Example

Explore 7

5 is already visited



	[0]	[1]	[2]	[3]	[4]	[5]	[6]	[7]	[8]	[9]
visited	1	1	1	1	1	1	1	1	1	0
pred	-1	0	0	2	5	0	5	5	4	-1

queue 0 1 2 5 3 4 6 7 8

Appendix

BFS Example

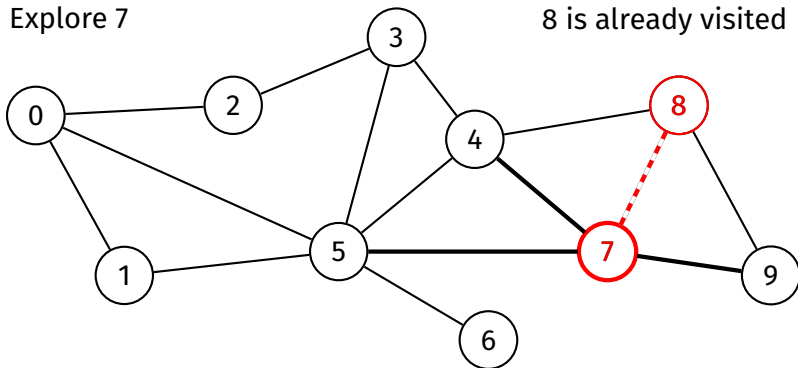
DFS Example

Path-Checking

Example

Explore 7

8 is already visited



	[0]	[1]	[2]	[3]	[4]	[5]	[6]	[7]	[8]	[9]
visited	1	1	1	1	1	1	1	1	1	0
pred	-1	0	0	2	5	0	5	5	4	-1

queue 0 1 2 5 3 4 6 7 8

Appendix

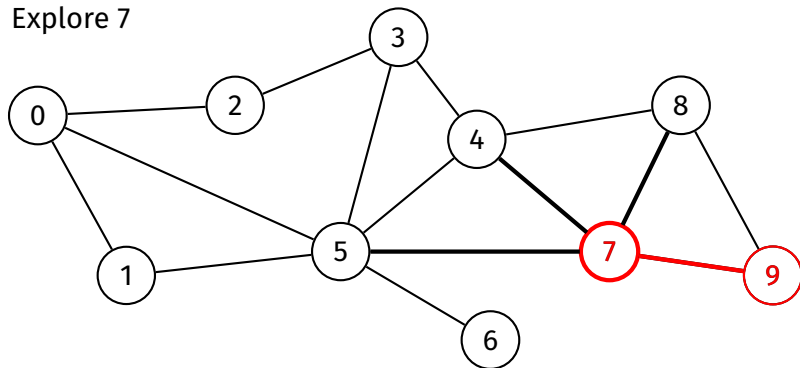
BFS Example

DFS Example

Path-Checking

Example

Explore 7



	[0]	[1]	[2]	[3]	[4]	[5]	[6]	[7]	[8]	[9]
visited	1	1	1	1	1	1	1	1	1	0
pred	-1	0	0	2	5	0	5	5	4	-1

queue 0 1 2 5 3 4 6 7 8

Appendix

BFS Example

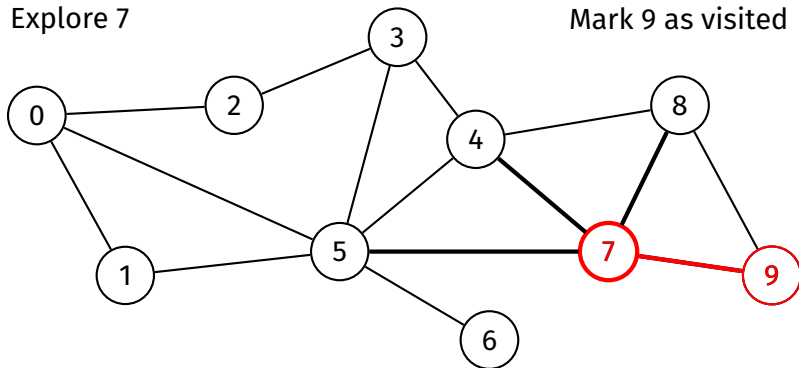
DFS Example

Path-Checking

Example

Explore 7

Mark 9 as visited



	[0]	[1]	[2]	[3]	[4]	[5]	[6]	[7]	[8]	[9]
visited	1	1	1	1	1	1	1	1	1	1
pred	-1	0	0	2	5	0	5	5	4	7

queue 0 1 2 5 3 4 6 7 8 9

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BFS Example

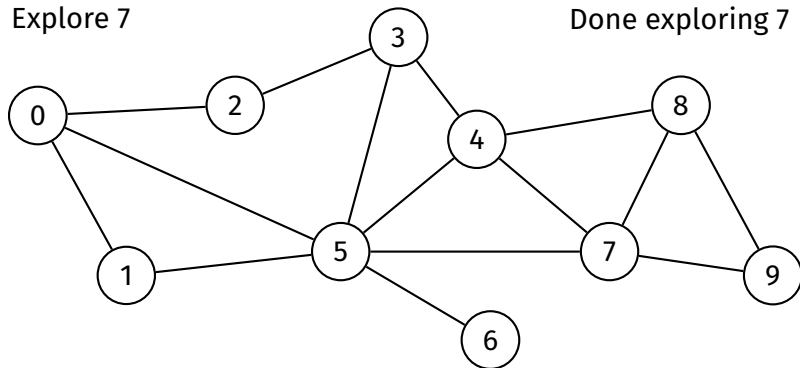
DFS Example

Path-Checking

Example

Explore 7

Done exploring 7



	[0]	[1]	[2]	[3]	[4]	[5]	[6]	[7]	[8]	[9]
visited	1	1	1	1	1	1	1	1	1	1
pred	-1	0	0	2	5	0	5	5	4	7

queue 0 1 2 5 3 4 6 7 8 9

Appendix

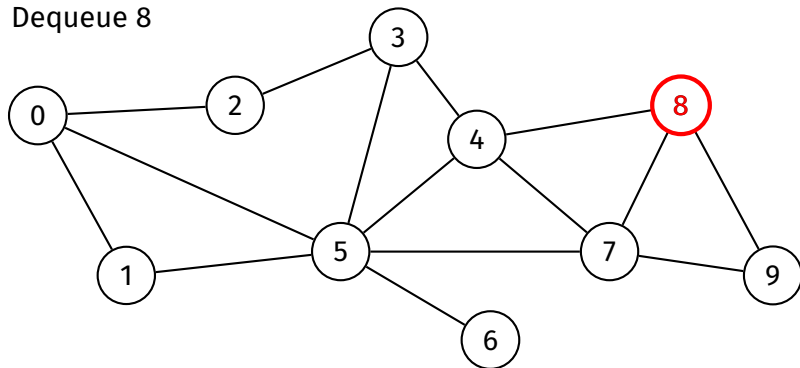
BFS Example

DFS Example

Path-Checking

Example

Dequeue 8



	[0]	[1]	[2]	[3]	[4]	[5]	[6]	[7]	[8]	[9]
visited	1	1	1	1	1	1	1	1	1	1
pred	-1	0	0	2	5	0	5	5	4	7

queue 0 1 2 5 3 4 6 7 8 9

Appendix

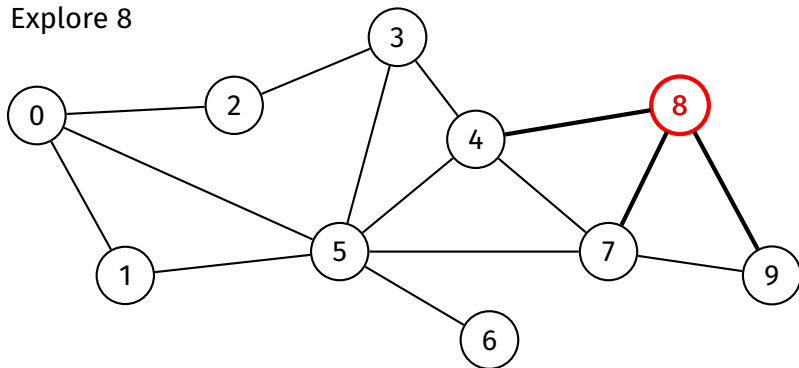
BFS Example

DFS Example

Path-Checking

Example

Explore 8



	[0]	[1]	[2]	[3]	[4]	[5]	[6]	[7]	[8]	[9]
visited	1	1	1	1	1	1	1	1	1	1
pred	-1	0	0	2	5	0	5	5	4	7

queue 0 1 2 5 3 4 6 7 8 9

Appendix

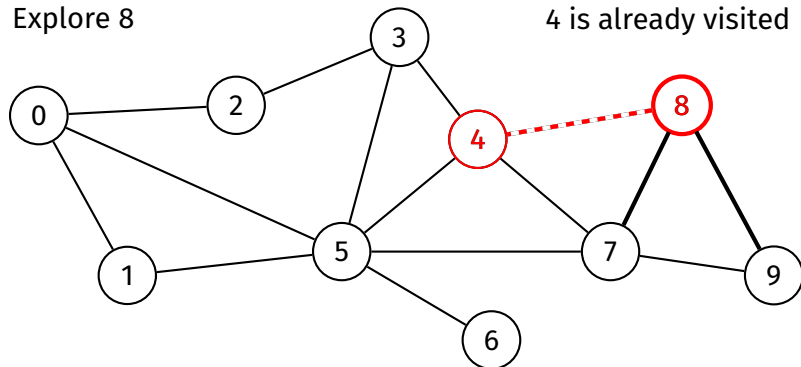
BFS Example

DFS Example

Path-Checking

Example

Explore 8



	[0]	[1]	[2]	[3]	[4]	[5]	[6]	[7]	[8]	[9]
visited	1	1	1	1	1	1	1	1	1	1
pred	-1	0	0	2	5	0	5	5	4	7

queue 0 1 2 5 3 4 6 7 8 9

Appendix

BFS Example

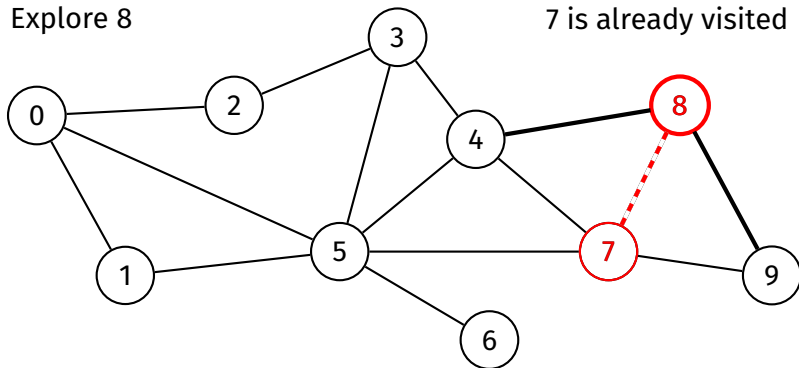
DFS Example

Path-Checking

Example

Explore 8

7 is already visited



	[0]	[1]	[2]	[3]	[4]	[5]	[6]	[7]	[8]	[9]
visited	1	1	1	1	1	1	1	1	1	1
pred	-1	0	0	2	5	0	5	5	4	7

queue 0 1 2 5 3 4 6 7 8 9

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BFS Example

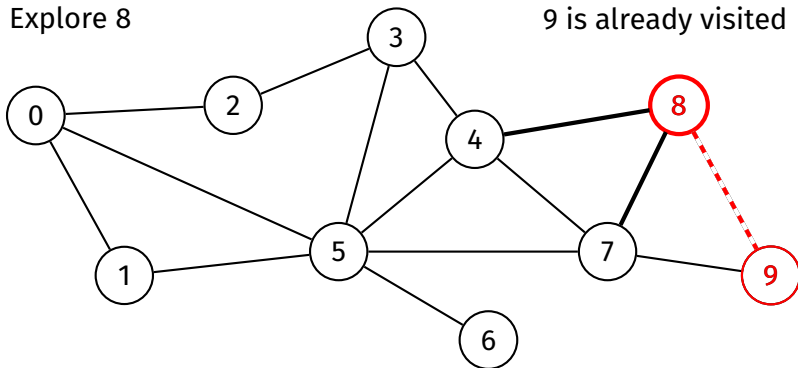
DFS Example

Path-Checking

Example

Explore 8

9 is already visited



	[0]	[1]	[2]	[3]	[4]	[5]	[6]	[7]	[8]	[9]
visited	1	1	1	1	1	1	1	1	1	1
pred	-1	0	0	2	5	0	5	5	4	7

queue 0 1 2 5 3 4 6 7 8 9

Appendix

BFS Example

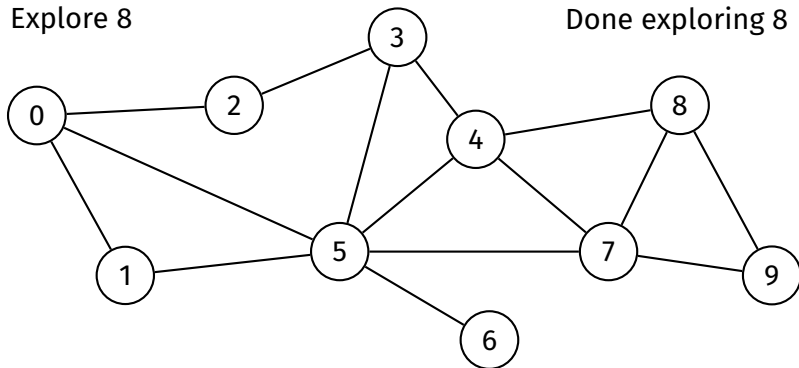
DFS Example

Path-Checking

Example

Explore 8

Done exploring 8



	[0]	[1]	[2]	[3]	[4]	[5]	[6]	[7]	[8]	[9]
visited	1	1	1	1	1	1	1	1	1	1
pred	-1	0	0	2	5	0	5	5	4	7

queue 0 1 2 5 3 4 6 7 8 9

Appendix

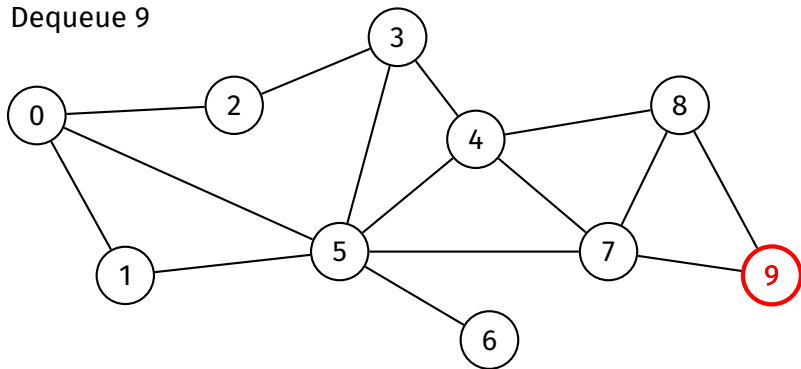
BFS Example

DFS Example

Path-Checking

Example

Dequeue 9



	[0]	[1]	[2]	[3]	[4]	[5]	[6]	[7]	[8]	[9]
visited	1	1	1	1	1	1	1	1	1	1
pred	-1	0	0	2	5	0	5	5	4	7

queue 0 1 2 5 3 4 6 7 8 9

Appendix

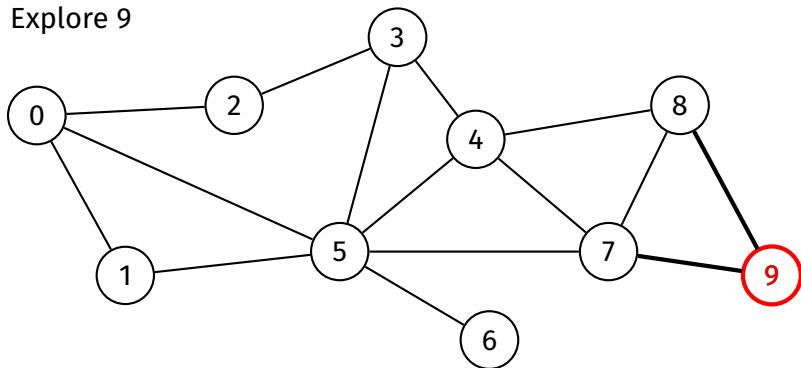
BFS Example

DFS Example

Path-Checking

Example

Explore 9



	[0]	[1]	[2]	[3]	[4]	[5]	[6]	[7]	[8]	[9]
visited	1	1	1	1	1	1	1	1	1	1
pred	-1	0	0	2	5	0	5	5	4	7

queue 0 1 2 5 3 4 6 7 8 9

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BFS Example

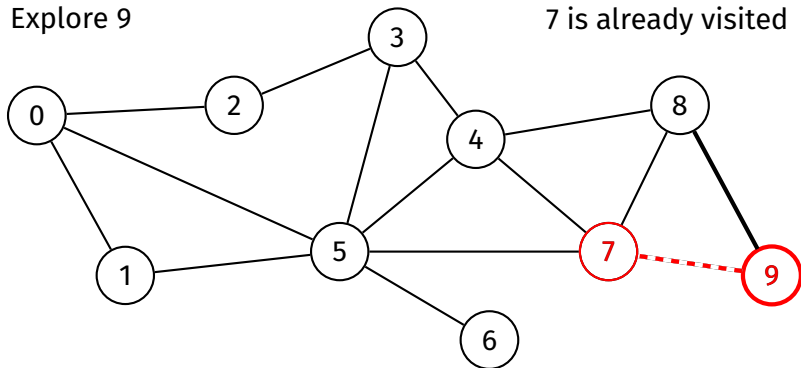
DFS Example

Path-Checking

Example

Explore 9

7 is already visited



	[0]	[1]	[2]	[3]	[4]	[5]	[6]	[7]	[8]	[9]
visited	1	1	1	1	1	1	1	1	1	1
pred	-1	0	0	2	5	0	5	5	4	7

queue 0 1 2 5 3 4 6 7 8 9

Appendix

BFS Example

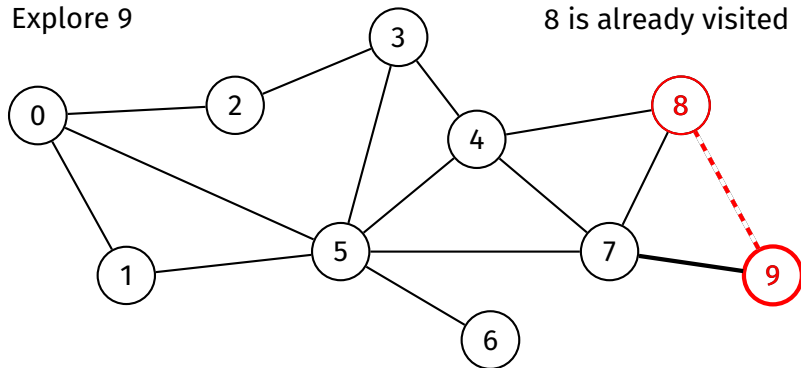
DFS Example

Path-Checking

Example

Explore 9

8 is already visited



	[0]	[1]	[2]	[3]	[4]	[5]	[6]	[7]	[8]	[9]
visited	1	1	1	1	1	1	1	1	1	1
pred	-1	0	0	2	5	0	5	5	4	7

queue 0 1 2 5 3 4 6 7 8 9

Appendix

BFS Example

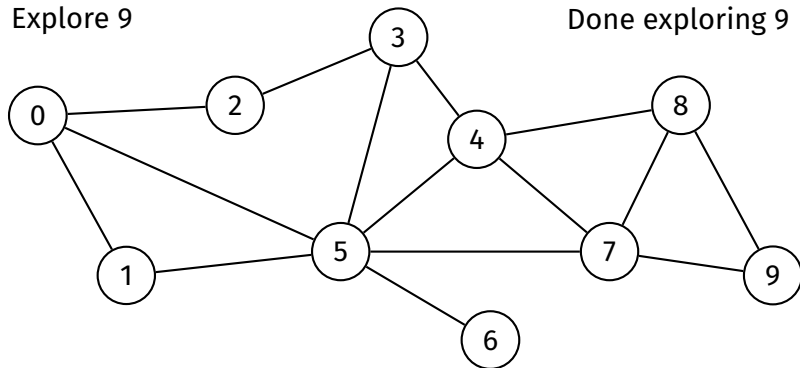
DFS Example

Path-Checking

Example

Explore 9

Done exploring 9



	[0]	[1]	[2]	[3]	[4]	[5]	[6]	[7]	[8]	[9]
visited	1	1	1	1	1	1	1	1	1	1
pred	-1	0	0	2	5	0	5	5	4	7

queue 0 1 2 5 3 4 6 7 8 9

Appendix

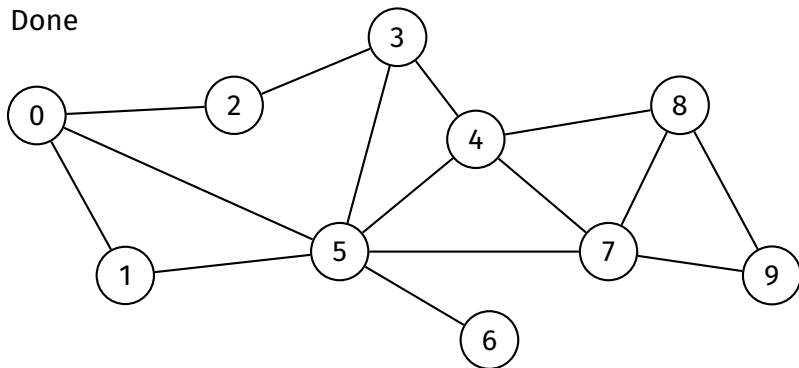
BFS Example

DFS Example

Path-Checking

Example

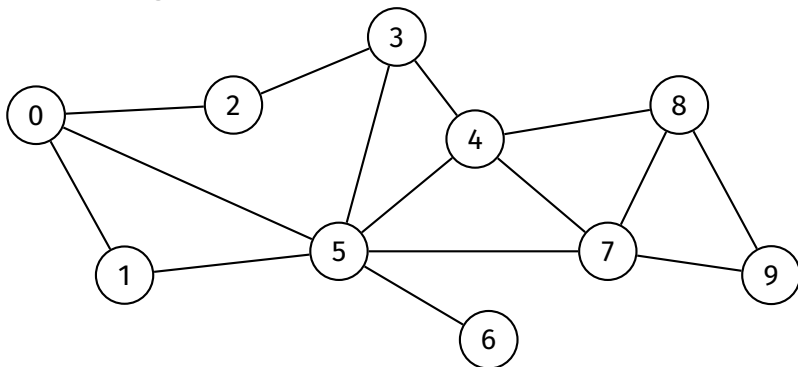
Done



	[0]	[1]	[2]	[3]	[4]	[5]	[6]	[7]	[8]	[9]
visited	1	1	1	1	1	1	1	1	1	1
pred	-1	0	0	2	5	0	5	5	4	7

queue 0 1 2 5 3 4 6 7 8 9

DFS starting at 0



	[0]	[1]	[2]	[3]	[4]	[5]	[6]	[7]	[8]	[9]
visited	0	0	0	0	0	0	0	0	0	0

call stack

visit order

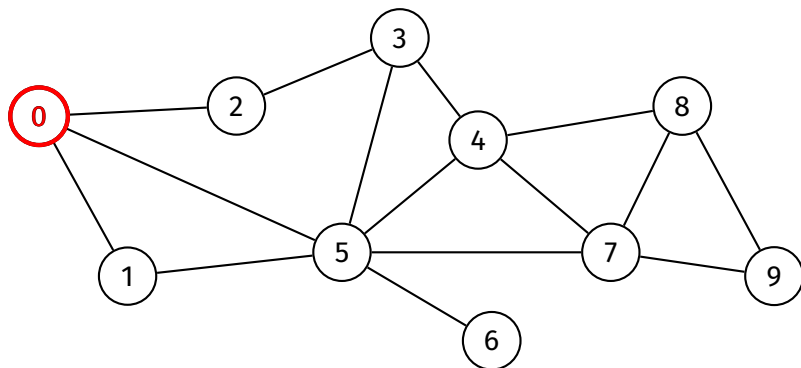
Appendix

BFS Example

DFS Example

Path-Checking

Example



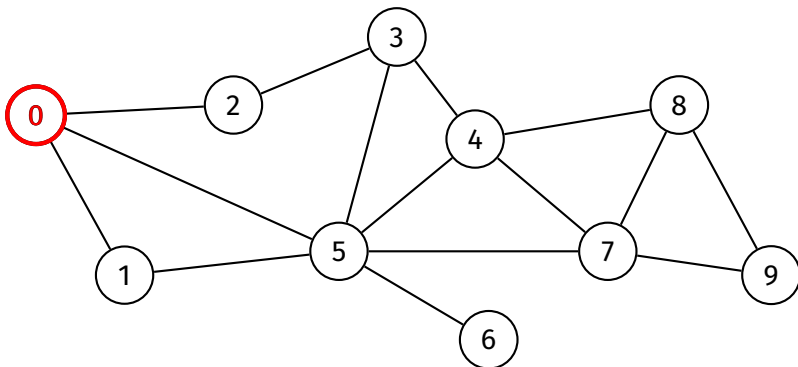
	[0]	[1]	[2]	[3]	[4]	[5]	[6]	[7]	[8]	[9]
visited	0	0	0	0	0	0	0	0	0	0

visit order

dfs(0)

call stack

Mark 0 as visited



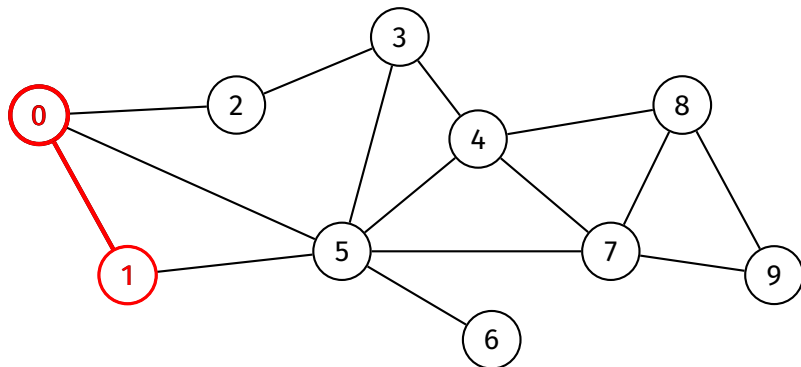
	[0]	[1]	[2]	[3]	[4]	[5]	[6]	[7]	[8]	[9]
visited	1	0	0	0	0	0	0	0	0	0

visit order 0

dfs(0)

call stack

1 has not been visited



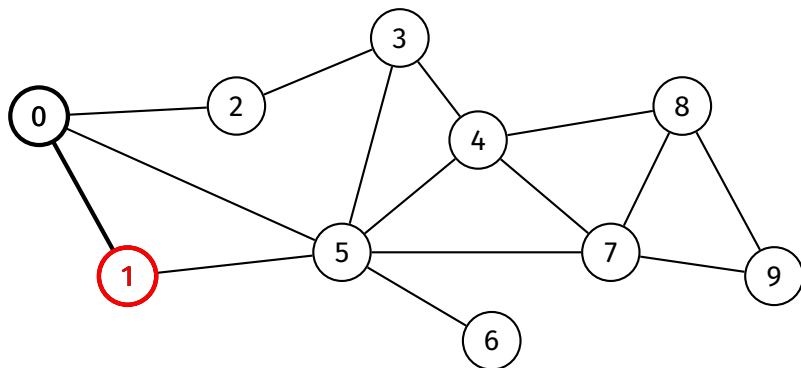
	[0]	[1]	[2]	[3]	[4]	[5]	[6]	[7]	[8]	[9]
visited	1	0	0	0	0	0	0	0	0	0

visit order 0

dfs(0)

call stack

Recurse into 1



	[0]	[1]	[2]	[3]	[4]	[5]	[6]	[7]	[8]	[9]
visited	1	0	0	0	0	0	0	0	0	0

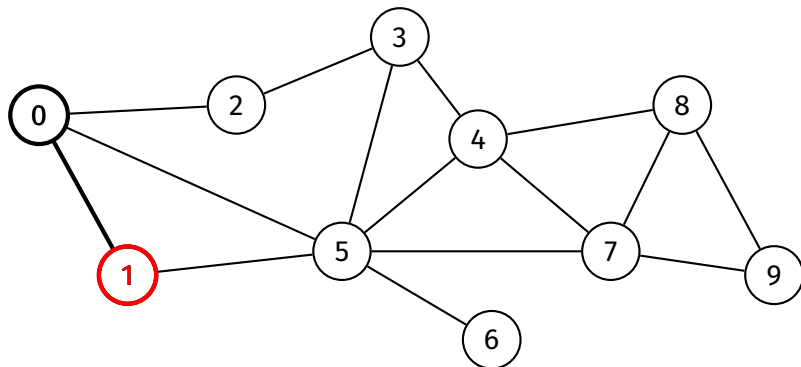
visit order 0

dfs(1)

dfs(0)

call stack

Mark 1 as visited



	[0]	[1]	[2]	[3]	[4]	[5]	[6]	[7]	[8]	[9]
visited	1	1	0	0	0	0	0	0	0	0

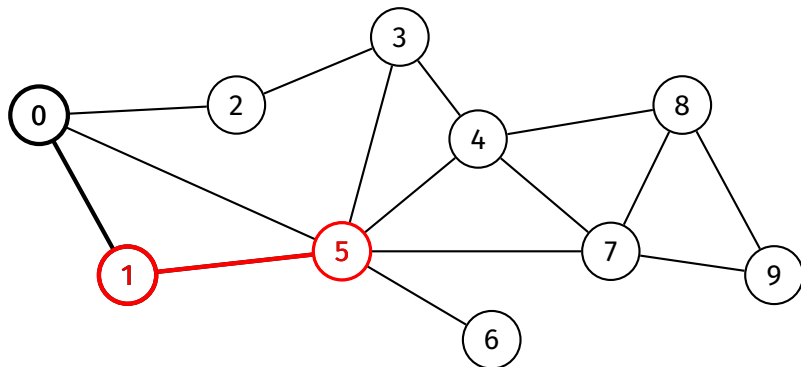
visit order 0 1

dfs(1)

dfs(0)

call stack

5 has not been visited



	[0]	[1]	[2]	[3]	[4]	[5]	[6]	[7]	[8]	[9]
visited	1	1	0	0	0	0	0	0	0	0

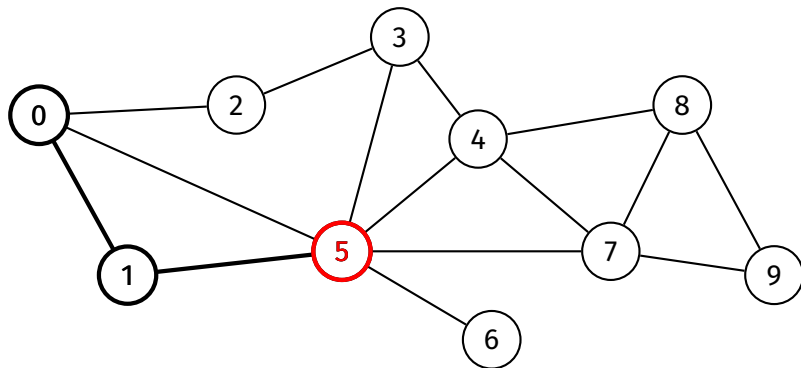
visit order 0 1

dfs(1)

dfs(0)

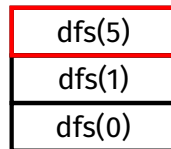
call stack

Recurse into 5



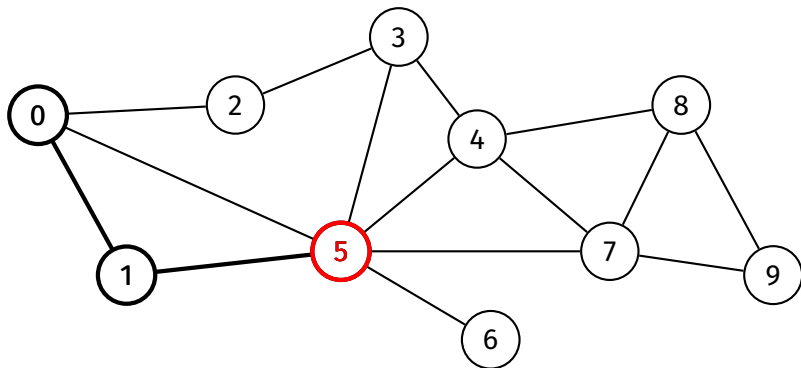
	[0]	[1]	[2]	[3]	[4]	[5]	[6]	[7]	[8]	[9]
visited	1	1	0	0	0	0	0	0	0	0

visit order 0 1



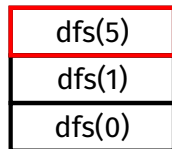
call stack

Mark 5 as visited



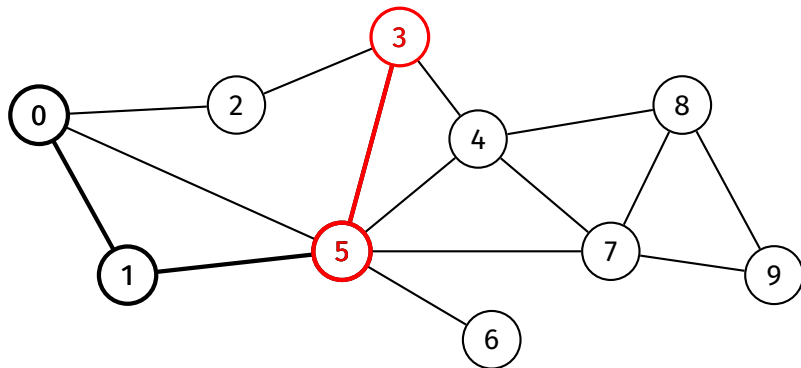
	[0]	[1]	[2]	[3]	[4]	[5]	[6]	[7]	[8]	[9]
visited	1	1	0	0	0	1	0	0	0	0

visit order 0 1 5



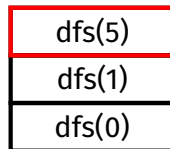
call stack

3 has not been visited



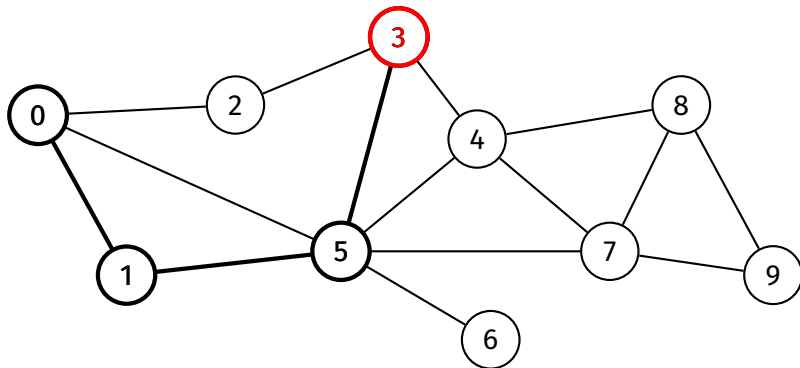
	[0]	[1]	[2]	[3]	[4]	[5]	[6]	[7]	[8]	[9]
visited	1	1	0	0	0	1	0	0	0	0

visit order 0 1 5



call stack

Recurse into 3



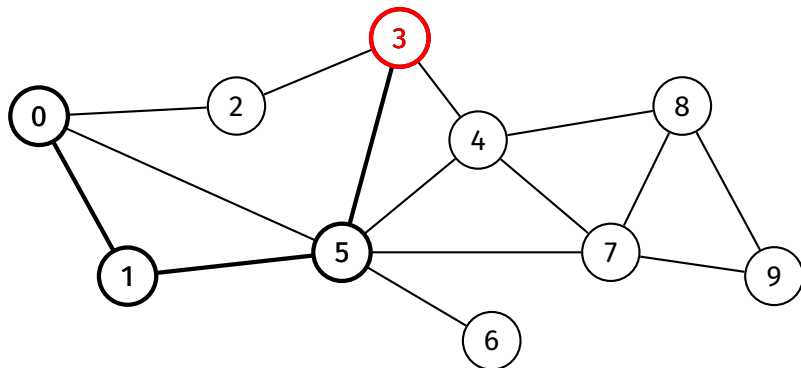
	[0]	[1]	[2]	[3]	[4]	[5]	[6]	[7]	[8]	[9]
visited	1	1	0	0	0	1	0	0	0	0

visit order 0 1 5

dfs(3)
dfs(5)
dfs(1)
dfs(0)

call stack

Mark 3 as visited



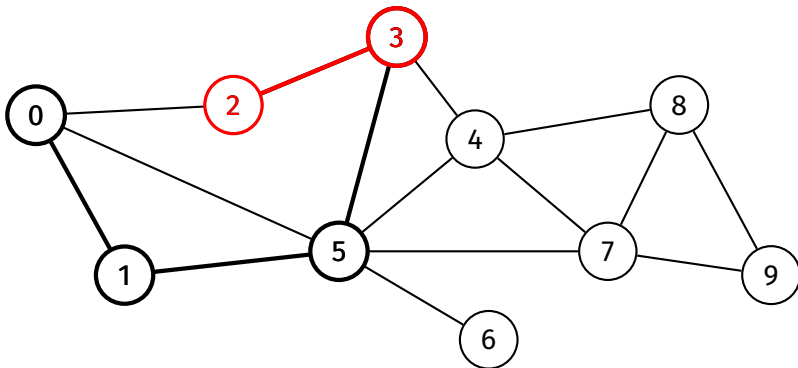
	[0]	[1]	[2]	[3]	[4]	[5]	[6]	[7]	[8]	[9]
visited	1	1	0	1	0	1	0	0	0	0

visit order 0 1 5 3

dfs(3)
dfs(5)
dfs(1)
dfs(0)

call stack

2 has not been visited



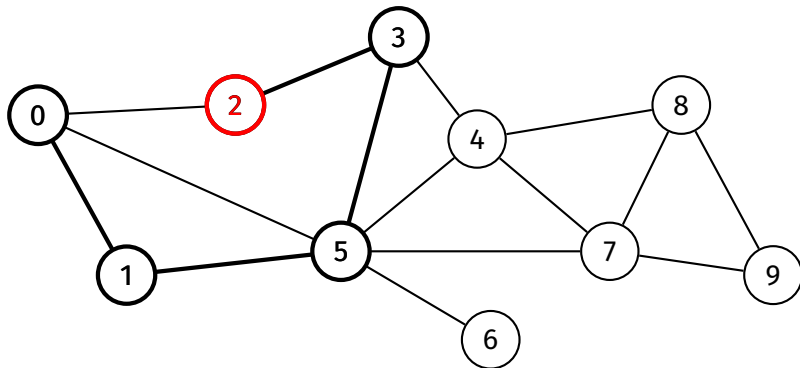
	[0]	[1]	[2]	[3]	[4]	[5]	[6]	[7]	[8]	[9]
visited	1	1	0	1	0	1	0	0	0	0

visit order 0 1 5 3

dfs(3)
dfs(5)
dfs(1)
dfs(0)

call stack

Recurse into 2



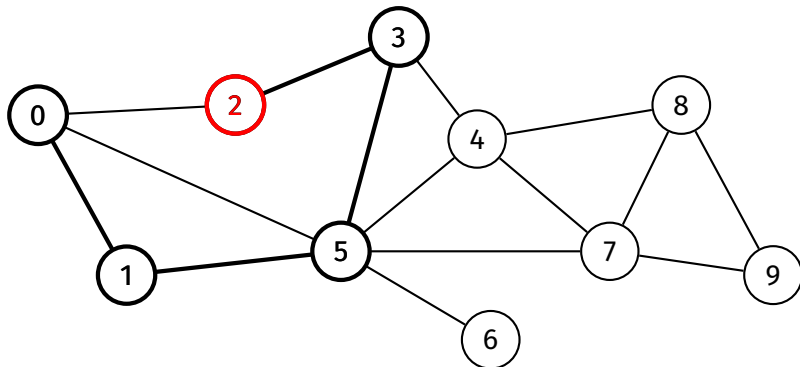
	[0]	[1]	[2]	[3]	[4]	[5]	[6]	[7]	[8]	[9]
visited	1	1	0	1	0	1	0	0	0	0

visit order 0 1 5 3

dfs(2)
dfs(3)
dfs(5)
dfs(1)
dfs(0)

call stack

Mark 2 as visited



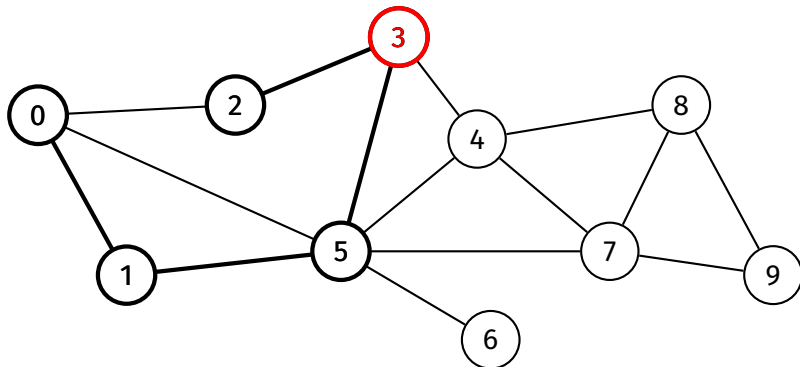
	[0]	[1]	[2]	[3]	[4]	[5]	[6]	[7]	[8]	[9]
visited	1	1	1	1	0	1	0	0	0	0

visit order 0 1 5 3 2

dfs(2)
dfs(3)
dfs(5)
dfs(1)
dfs(0)

call stack

Return



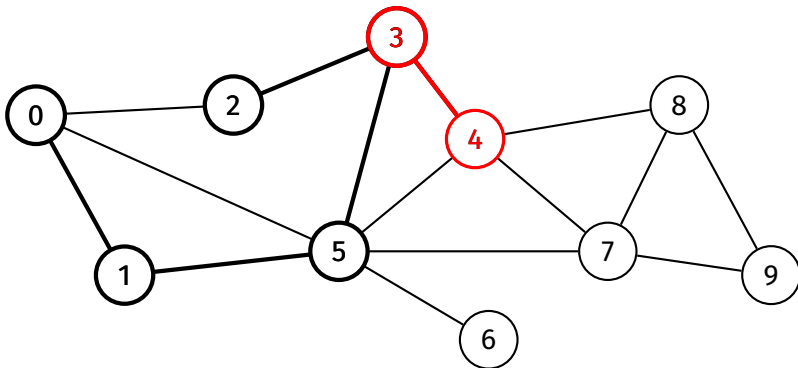
	[0]	[1]	[2]	[3]	[4]	[5]	[6]	[7]	[8]	[9]
visited	1	1	1	1	0	1	0	0	0	0

visit order 0 1 5 3 2

dfs(3)
dfs(5)
dfs(1)
dfs(0)

call stack

4 has not been visited



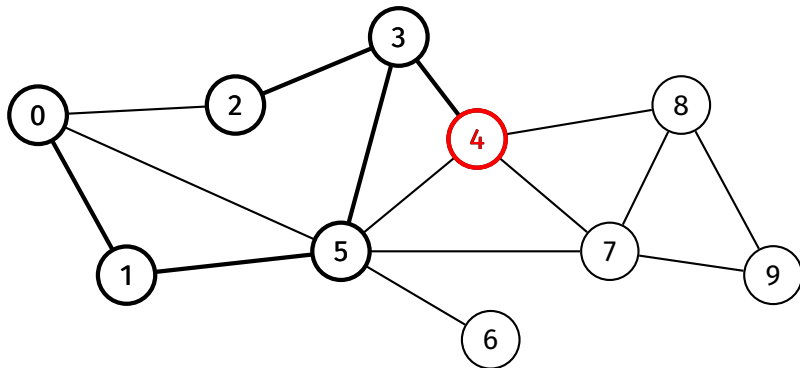
	[0]	[1]	[2]	[3]	[4]	[5]	[6]	[7]	[8]	[9]
visited	1	1	1	1	0	1	0	0	0	0

visit order 0 1 5 3 2

dfs(3)
dfs(5)
dfs(1)
dfs(0)

call stack

Recurse into 4



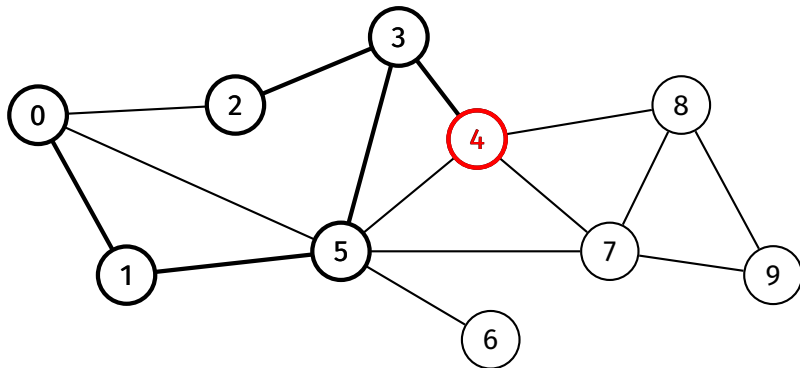
	[0]	[1]	[2]	[3]	[4]	[5]	[6]	[7]	[8]	[9]
visited	1	1	1	1	0	1	0	0	0	0

visit order 0 1 5 3 2

dfs(4)
dfs(3)
dfs(5)
dfs(1)
dfs(0)

call stack

Mark 4 as visited



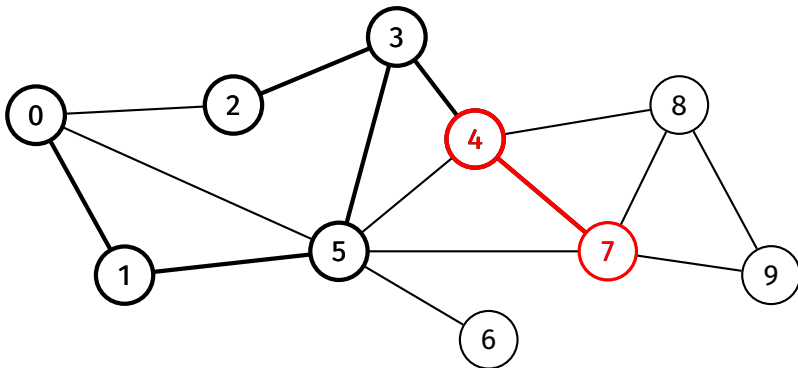
	[0]	[1]	[2]	[3]	[4]	[5]	[6]	[7]	[8]	[9]
visited	1	1	1	1	1	1	0	0	0	0

visit order 0 1 5 3 2 4

dfs(4)
dfs(3)
dfs(5)
dfs(1)
dfs(0)

call stack

7 has not been visited



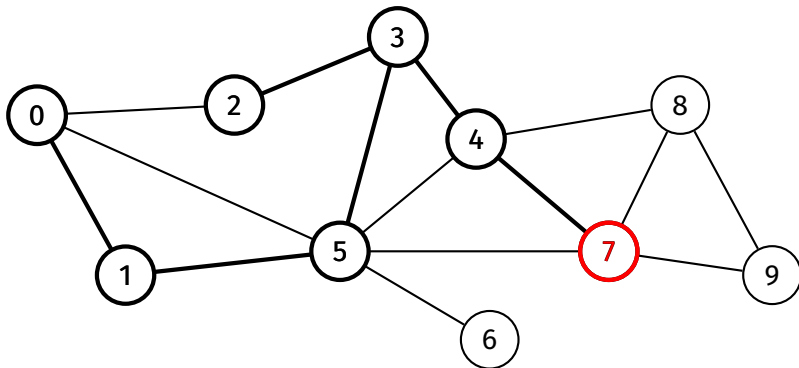
	[0]	[1]	[2]	[3]	[4]	[5]	[6]	[7]	[8]	[9]
visited	1	1	1	1	1	1	0	0	0	0

visit order 0 1 5 3 2 4

dfs(4)
dfs(3)
dfs(5)
dfs(1)
dfs(0)

call stack

Recurse into 7



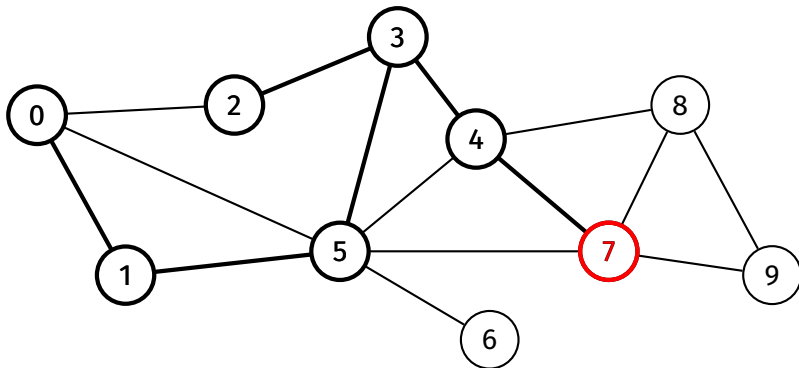
	[0]	[1]	[2]	[3]	[4]	[5]	[6]	[7]	[8]	[9]
visited	1	1	1	1	1	1	0	0	0	0

visit order 0 1 5 3 2 4

dfs(7)
dfs(4)
dfs(3)
dfs(5)
dfs(1)
dfs(0)

call stack

Mark 7 as visited



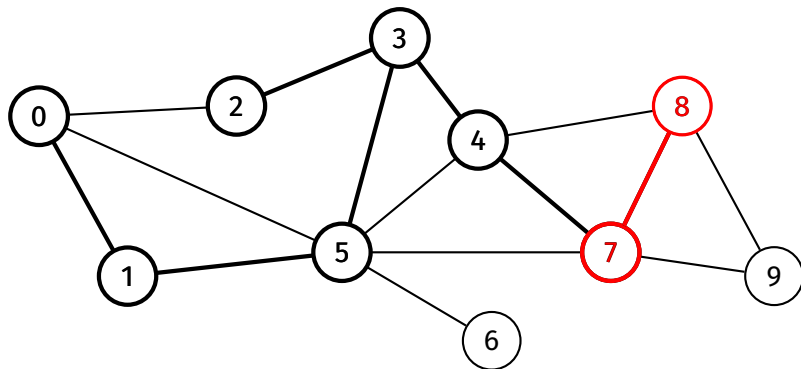
	[0]	[1]	[2]	[3]	[4]	[5]	[6]	[7]	[8]	[9]
visited	1	1	1	1	1	1	0	1	0	0

visit order 0 1 5 3 2 4 7

dfs(7)
dfs(4)
dfs(3)
dfs(5)
dfs(1)
dfs(0)

call stack

8 has not been visited



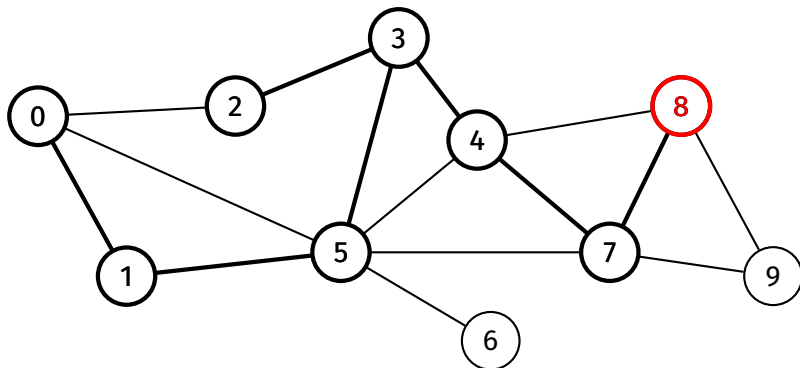
	[0]	[1]	[2]	[3]	[4]	[5]	[6]	[7]	[8]	[9]
visited	1	1	1	1	1	1	0	1	0	0

visit order 0 1 5 3 2 4 7

dfs(7)
dfs(4)
dfs(3)
dfs(5)
dfs(1)
dfs(0)

call stack

Recurse into 8



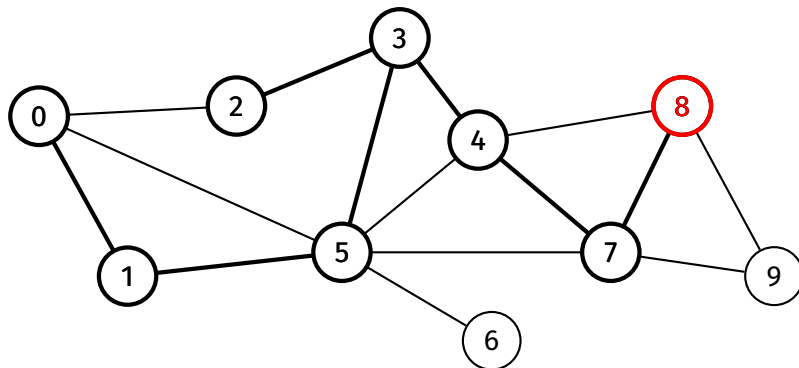
	[0]	[1]	[2]	[3]	[4]	[5]	[6]	[7]	[8]	[9]
visited	1	1	1	1	1	1	0	1	0	0

visit order 0 1 5 3 2 4 7

dfs(8)
dfs(7)
dfs(4)
dfs(3)
dfs(5)
dfs(1)
dfs(0)

call stack

Mark 8 as visited



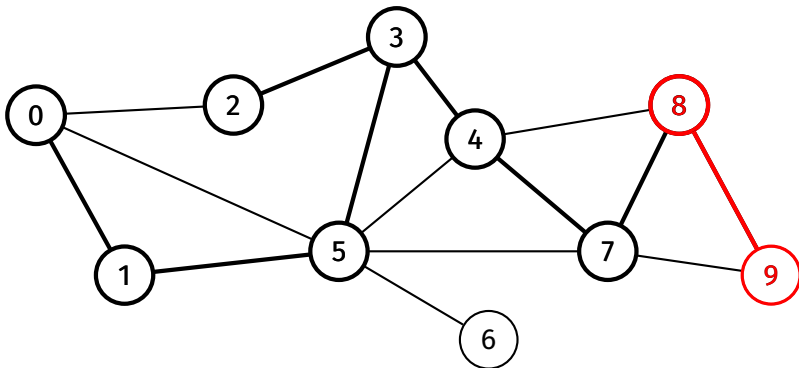
	[0]	[1]	[2]	[3]	[4]	[5]	[6]	[7]	[8]	[9]
visited	1	1	1	1	1	1	0	1	1	0

visit order 0 1 5 3 2 4 7 8

dfs(8)
dfs(7)
dfs(4)
dfs(3)
dfs(5)
dfs(1)
dfs(0)

call stack

9 has not been visited



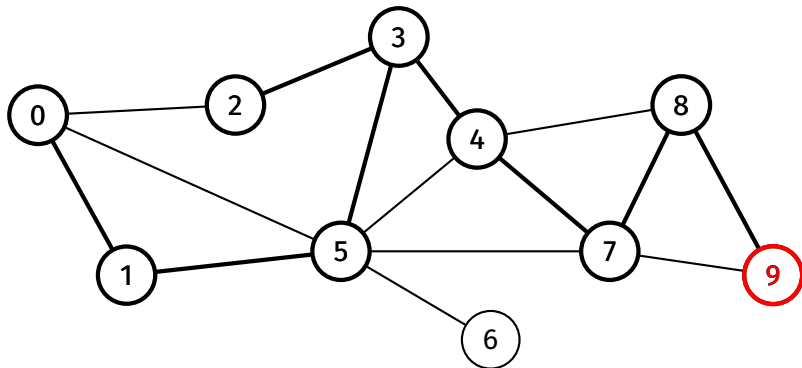
	[0]	[1]	[2]	[3]	[4]	[5]	[6]	[7]	[8]	[9]
visited	1	1	1	1	1	1	0	1	1	0

visit order 0 1 5 3 2 4 7 8

dfs(8)
dfs(7)
dfs(4)
dfs(3)
dfs(5)
dfs(1)
dfs(0)

call stack

Recurse into 9



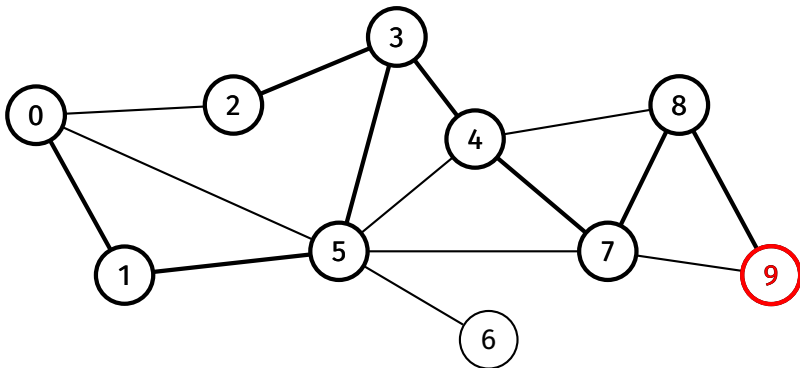
	[0]	[1]	[2]	[3]	[4]	[5]	[6]	[7]	[8]	[9]
visited	1	1	1	1	1	1	0	1	1	0

visit order 0 1 5 3 2 4 7 8

dfs(9)
dfs(8)
dfs(7)
dfs(4)
dfs(3)
dfs(5)
dfs(1)
dfs(0)

call stack

Mark 9 as visited



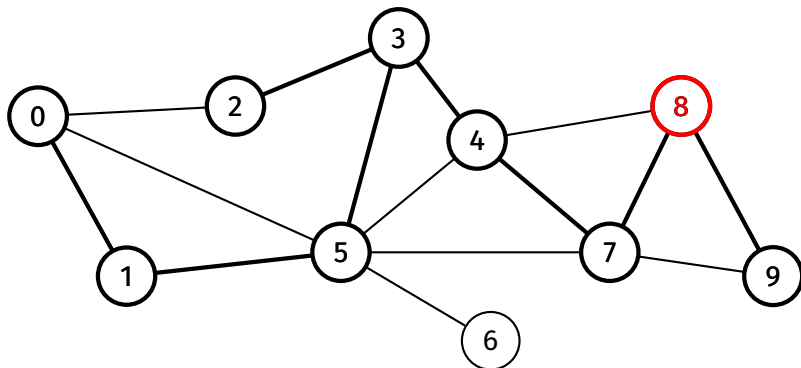
	[0]	[1]	[2]	[3]	[4]	[5]	[6]	[7]	[8]	[9]
visited	1	1	1	1	1	1	0	1	1	1

visit order 0 1 5 3 2 4 7 8 9

dfs(9)
dfs(8)
dfs(7)
dfs(4)
dfs(3)
dfs(5)
dfs(1)
dfs(0)

call stack

Return



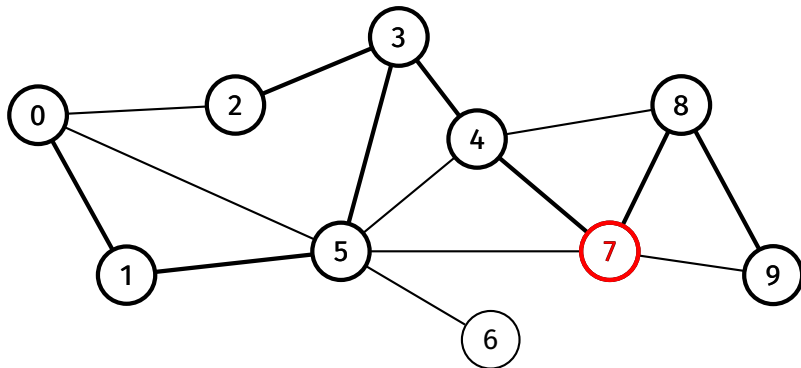
	[0]	[1]	[2]	[3]	[4]	[5]	[6]	[7]	[8]	[9]
visited	1	1	1	1	1	1	0	1	1	1

visit order 0 1 5 3 2 4 7 8 9

dfs(8)
dfs(7)
dfs(4)
dfs(3)
dfs(5)
dfs(1)
dfs(0)

call stack

Return



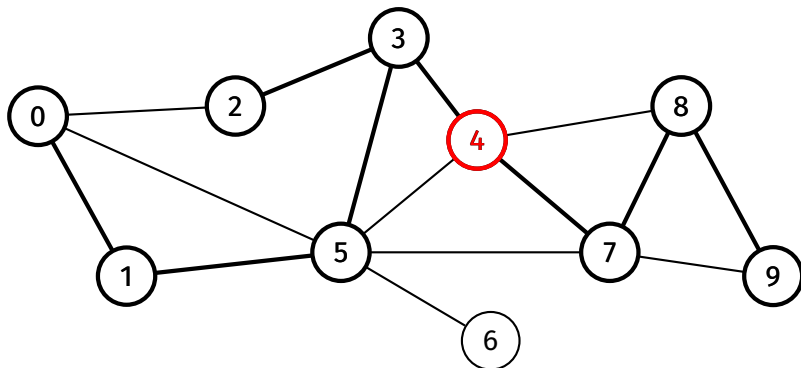
dfs(7)
dfs(4)
dfs(3)
dfs(5)
dfs(1)
dfs(0)

call stack

	[0]	[1]	[2]	[3]	[4]	[5]	[6]	[7]	[8]	[9]
visited	1	1	1	1	1	1	0	1	1	1

visit order 0 1 5 3 2 4 7 8 9

Return



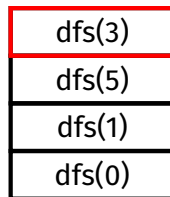
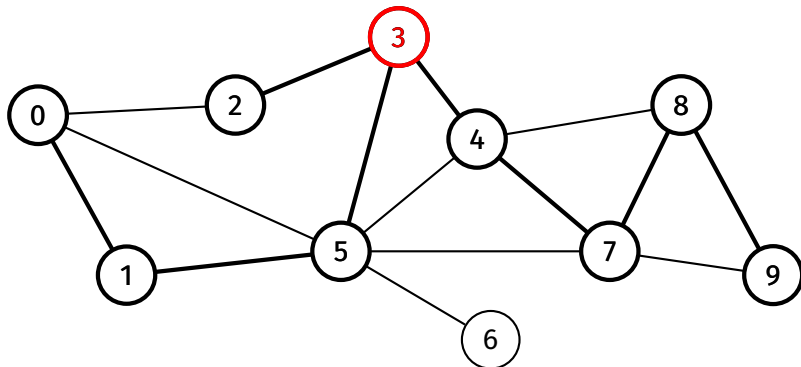
dfs(4)
dfs(3)
dfs(5)
dfs(1)
dfs(0)

call stack

	[0]	[1]	[2]	[3]	[4]	[5]	[6]	[7]	[8]	[9]
visited	1	1	1	1	1	1	0	1	1	1

visit order 0 1 5 3 2 4 7 8 9

Return

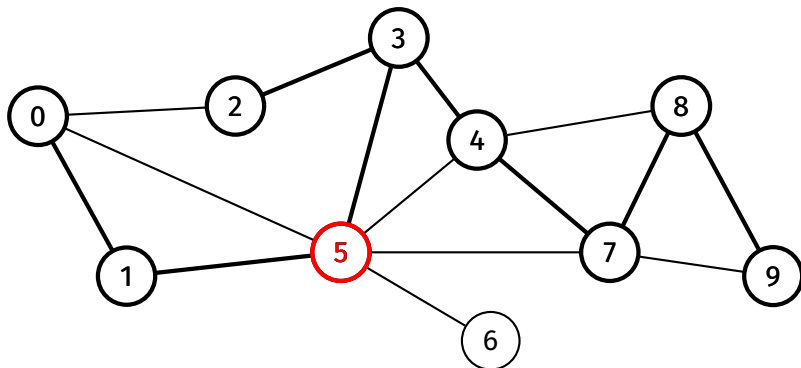


call stack

	[0]	[1]	[2]	[3]	[4]	[5]	[6]	[7]	[8]	[9]
visited	1	1	1	1	1	1	0	1	1	1

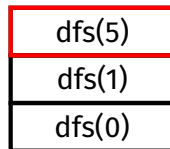
visit order 0 1 5 3 2 4 7 8 9

Return



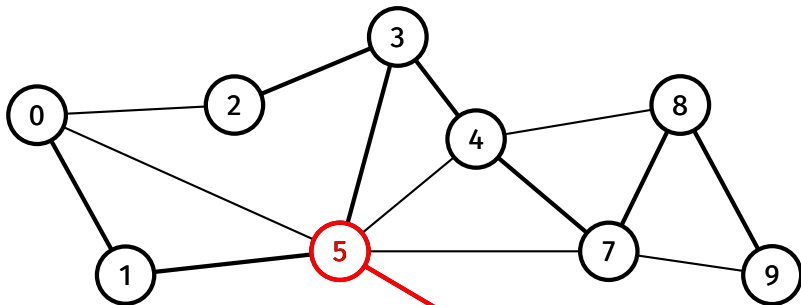
	[0]	[1]	[2]	[3]	[4]	[5]	[6]	[7]	[8]	[9]
visited	1	1	1	1	1	1	0	1	1	1

visit order 0 1 5 3 2 4 7 8 9



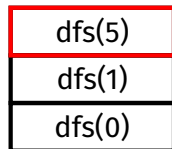
call stack

6 has not been visited



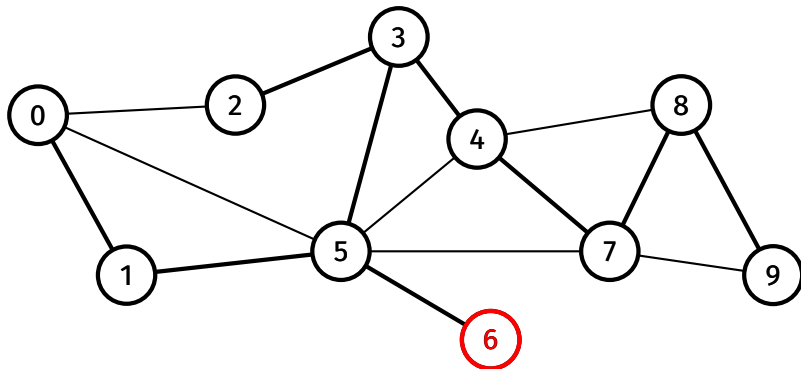
	[0]	[1]	[2]	[3]	[4]	[5]	[6]	[7]	[8]	[9]
visited	1	1	1	1	1	1	0	1	1	1

visit order 0 1 5 3 2 4 7 8 9



call stack

Recurse into 6



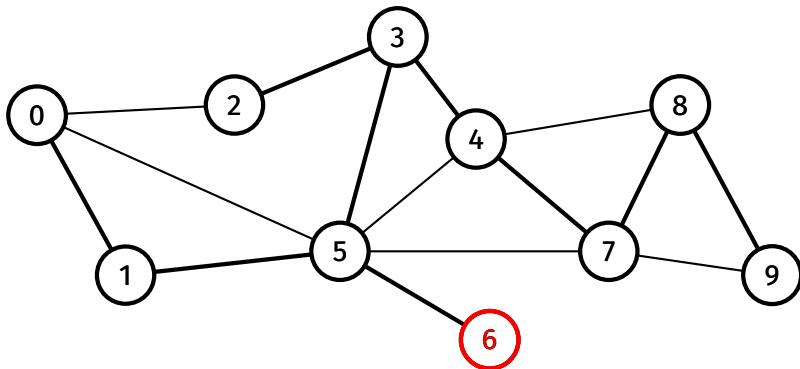
	[0]	[1]	[2]	[3]	[4]	[5]	[6]	[7]	[8]	[9]
visited	1	1	1	1	1	1	0	1	1	1

visit order 0 1 5 3 2 4 7 8 9

dfs(6)
dfs(5)
dfs(1)
dfs(0)

call stack

Mark 6 as visited



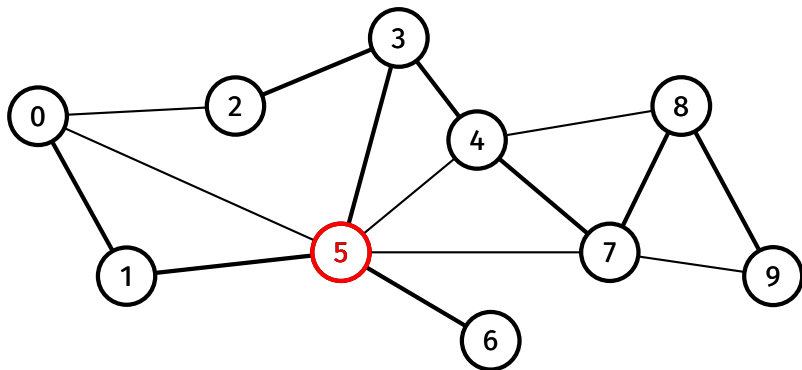
	[0]	[1]	[2]	[3]	[4]	[5]	[6]	[7]	[8]	[9]
visited	1	1	1	1	1	1	1	1	1	1

visit order 0 1 5 3 2 4 7 8 9 6

dfs(6)
dfs(5)
dfs(1)
dfs(0)

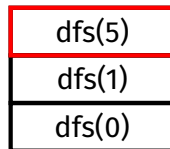
call stack

Return



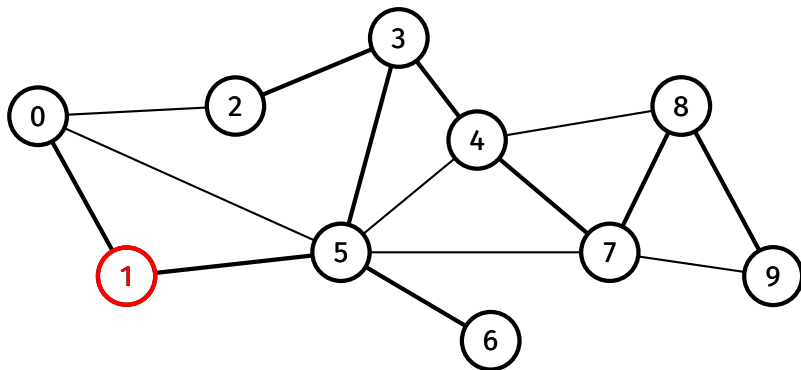
	[0]	[1]	[2]	[3]	[4]	[5]	[6]	[7]	[8]	[9]
visited	1	1	1	1	1	1	1	1	1	1

visit order 0 1 5 3 2 4 7 8 9 6



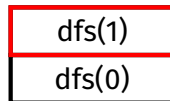
call stack

Return



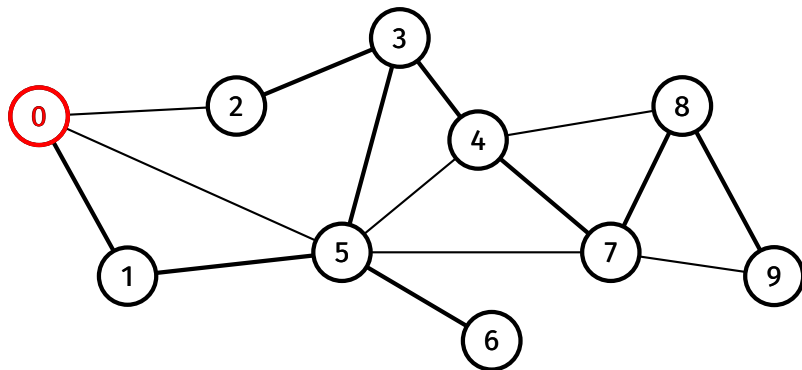
	[0]	[1]	[2]	[3]	[4]	[5]	[6]	[7]	[8]	[9]
visited	1	1	1	1	1	1	1	1	1	1

visit order 0 1 5 3 2 4 7 8 9 6



call stack

Return



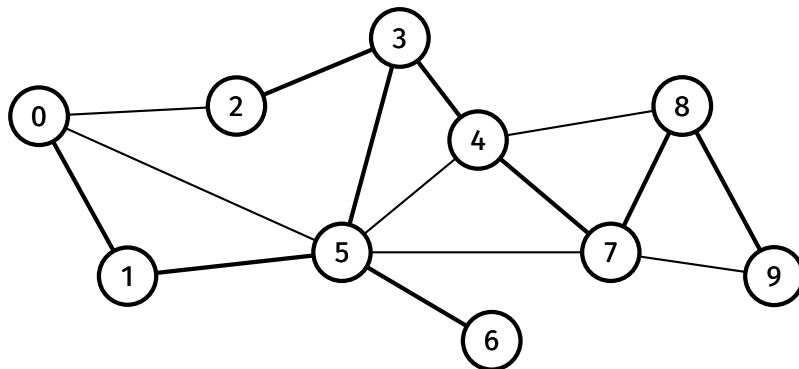
	[0]	[1]	[2]	[3]	[4]	[5]	[6]	[7]	[8]	[9]
visited	1	1	1	1	1	1	1	1	1	1

visit order 0 1 5 3 2 4 7 8 9 6

dfs(0)

call stack

Return

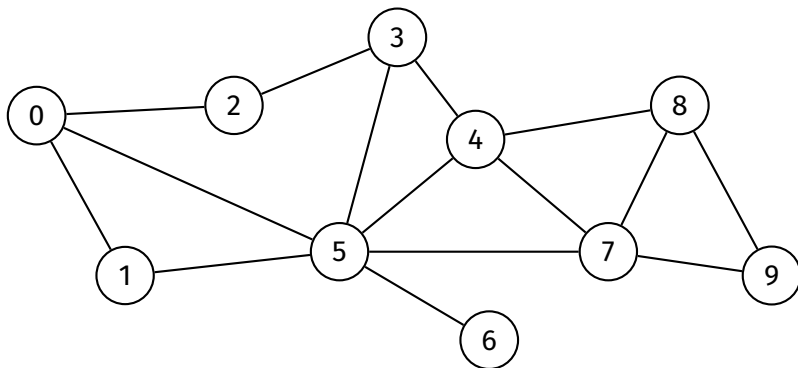


	[0]	[1]	[2]	[3]	[4]	[5]	[6]	[7]	[8]	[9]
visited	1	1	1	1	1	1	1	1	1	1

call stack

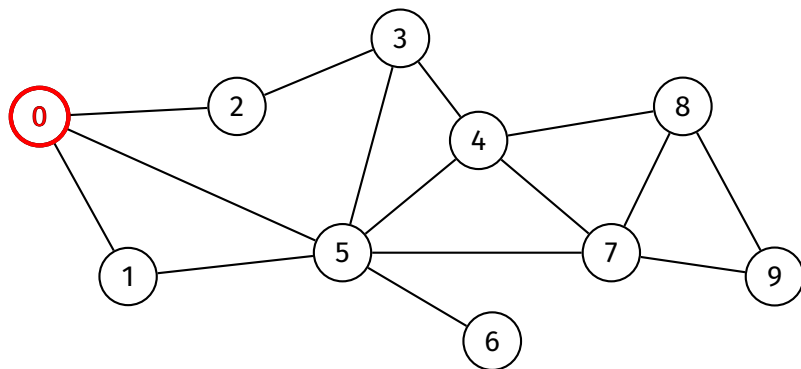
visit order 0 1 5 3 2 4 7 8 9 6

Is there a path between 0 and 7?



call stack

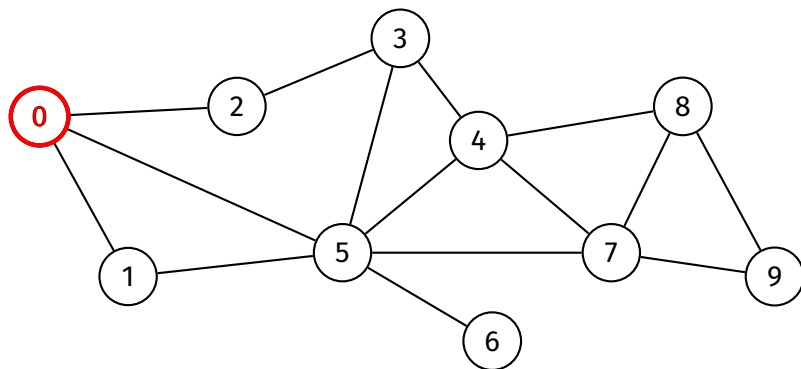
	[0]	[1]	[2]	[3]	[4]	[5]	[6]	[7]	[8]	[9]
visited	0	0	0	0	0	0	0	0	0	0

**path(0, 7)?**

call stack

	[0]	[1]	[2]	[3]	[4]	[5]	[6]	[7]	[8]	[9]
visited	0	0	0	0	0	0	0	0	0	0

Mark 0 as visited

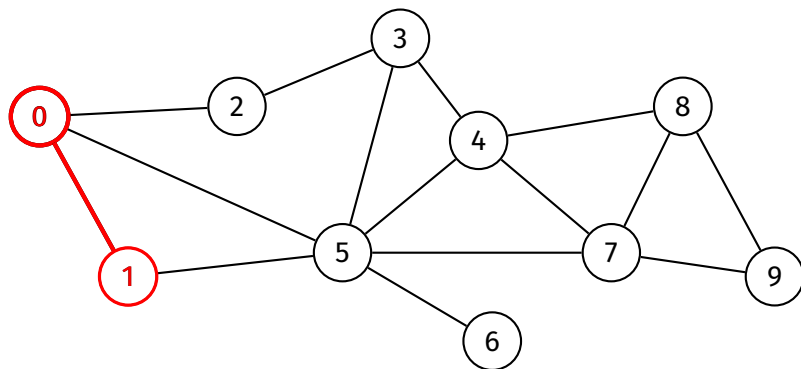


path(0, 7)?

call stack

	[0]	[1]	[2]	[3]	[4]	[5]	[6]	[7]	[8]	[9]
visited	1	0	0	0	0	0	0	0	0	0

1 has not been visited

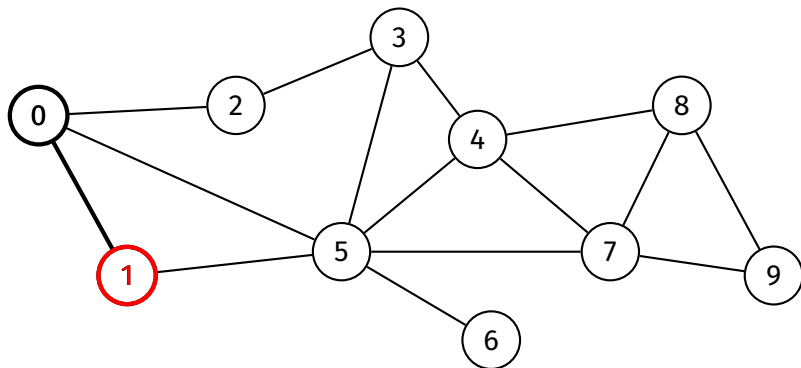


path(0, 7)?

call stack

	[0]	[1]	[2]	[3]	[4]	[5]	[6]	[7]	[8]	[9]
visited	1	0	0	0	0	0	0	0	0	0

Recurse into 1



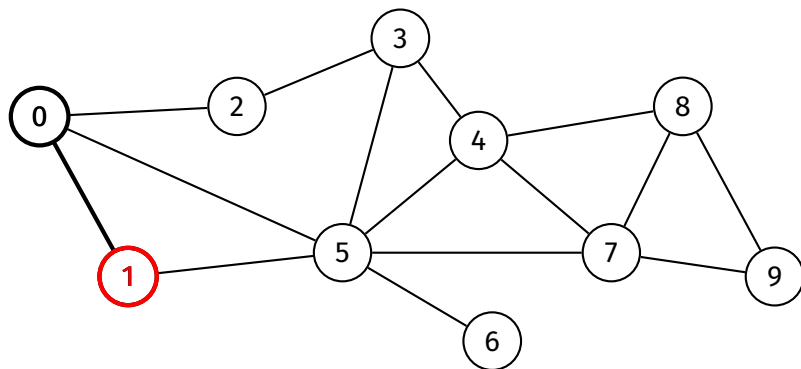
path(1, 7)?

path(0, 7)?

call stack

	[0]	[1]	[2]	[3]	[4]	[5]	[6]	[7]	[8]	[9]
visited	1	0	0	0	0	0	0	0	0	0

Mark 1 as visited



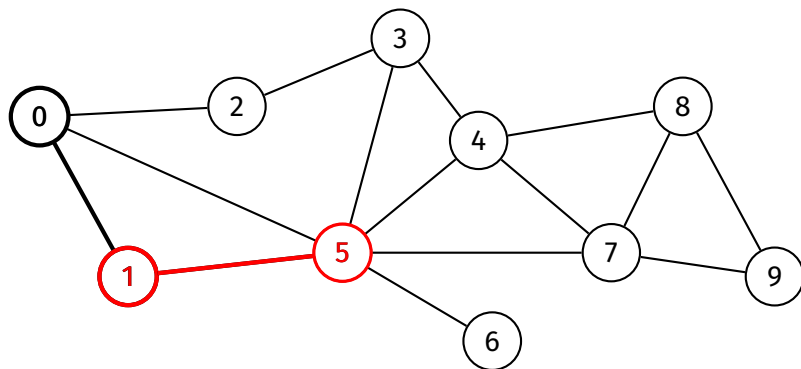
path(1, 7)?

path(0, 7)?

call stack

	[0]	[1]	[2]	[3]	[4]	[5]	[6]	[7]	[8]	[9]
visited	1	1	0	0	0	0	0	0	0	0

5 has not been visited



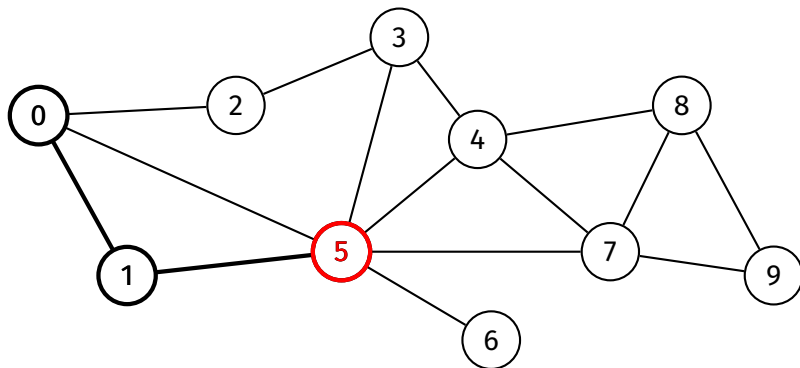
path(1, 7)?

path(0, 7)?

call stack

	[0]	[1]	[2]	[3]	[4]	[5]	[6]	[7]	[8]	[9]
visited	1	1	0	0	0	0	0	0	0	0

Recurse into 5



path(5, 7)?

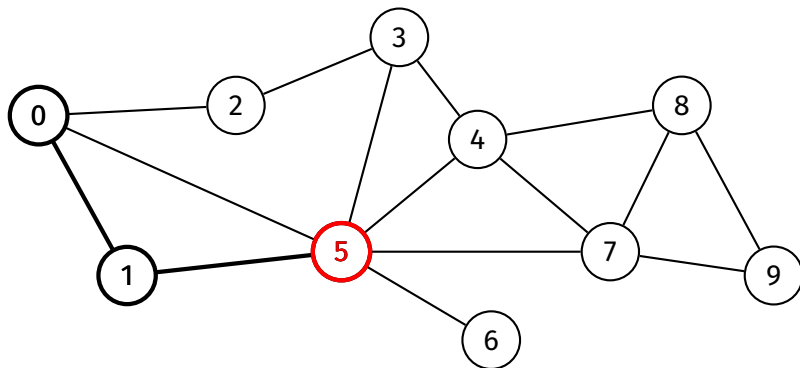
path(1, 7)?

path(0, 7)?

call stack

	[0]	[1]	[2]	[3]	[4]	[5]	[6]	[7]	[8]	[9]
visited	1	1	0	0	0	0	0	0	0	0

Mark 5 as visited



path(5, 7)?

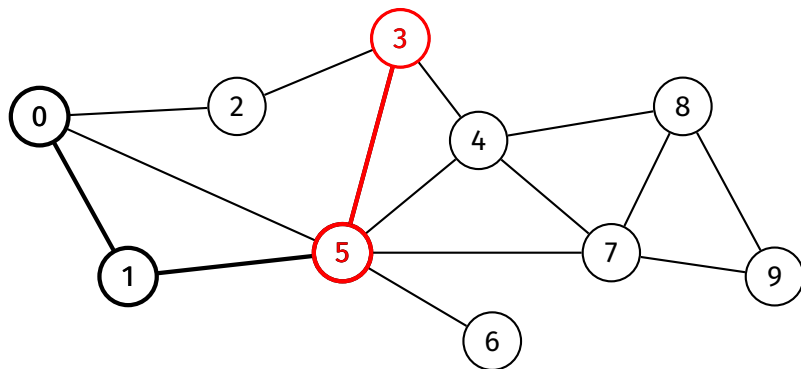
path(1, 7)?

path(0, 7)?

call stack

	[0]	[1]	[2]	[3]	[4]	[5]	[6]	[7]	[8]	[9]
visited	1	1	0	0	0	1	0	0	0	0

3 has not been visited



path(5, 7)?

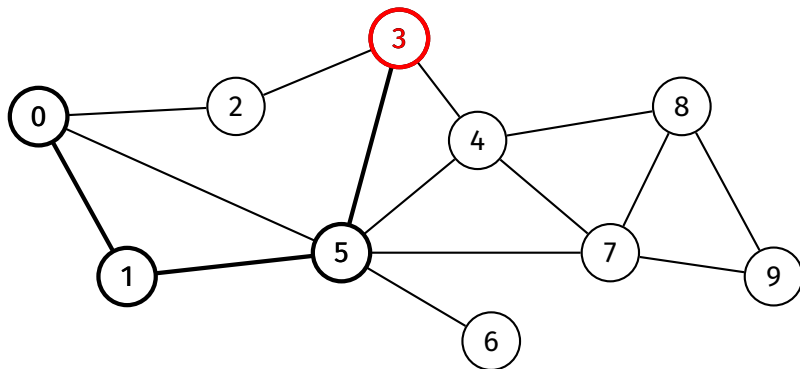
path(1, 7)?

path(0, 7)?

call stack

	[0]	[1]	[2]	[3]	[4]	[5]	[6]	[7]	[8]	[9]
visited	1	1	0	0	0	1	0	0	0	0

Recurse into 3



path(3, 7)?

path(5, 7)?

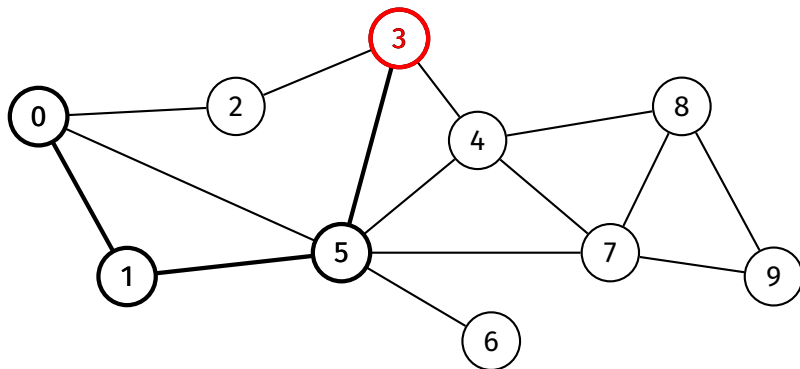
path(1, 7)?

path(0, 7)?

call stack

	[0]	[1]	[2]	[3]	[4]	[5]	[6]	[7]	[8]	[9]
visited	1	1	0	0	0	1	0	0	0	0

Mark 3 as visited



path(3, 7)?

path(5, 7)?

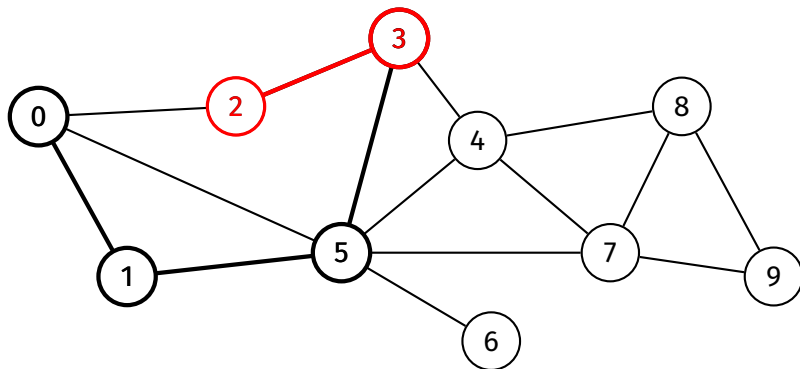
path(1, 7)?

path(0, 7)?

call stack

	[0]	[1]	[2]	[3]	[4]	[5]	[6]	[7]	[8]	[9]
visited	1	1	0	1	0	1	0	0	0	0

2 has not been visited



path(3, 7)?

path(5, 7)?

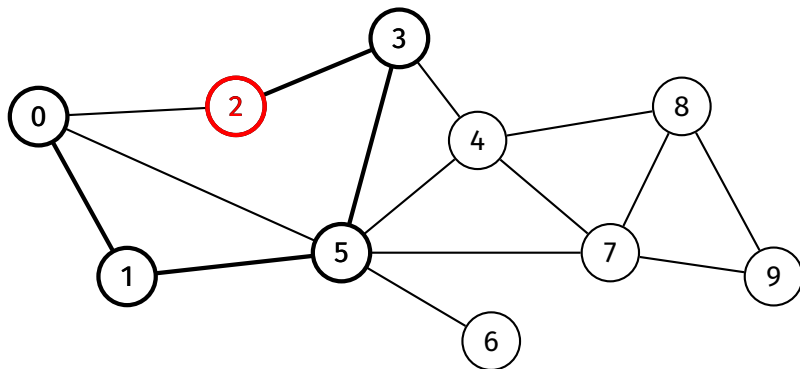
path(1, 7)?

path(0, 7)?

call stack

	[0]	[1]	[2]	[3]	[4]	[5]	[6]	[7]	[8]	[9]
visited	1	1	0	1	0	1	0	0	0	0

Recurse into 2



path(2, 7)?

path(3, 7)?

path(5, 7)?

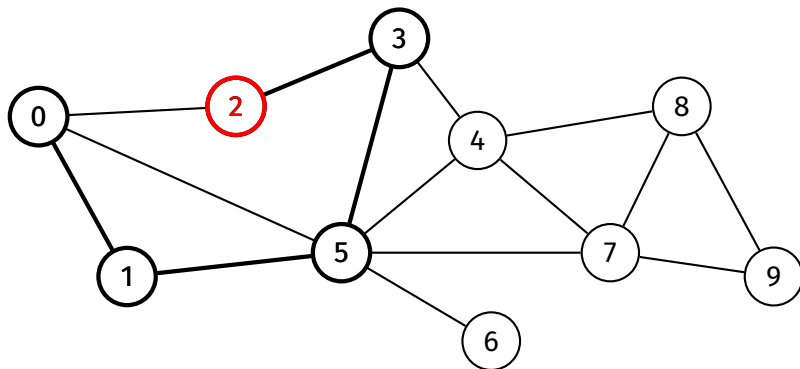
path(1, 7)?

path(0, 7)?

call stack

	[0]	[1]	[2]	[3]	[4]	[5]	[6]	[7]	[8]	[9]
visited	1	1	0	1	0	1	0	0	0	0

Mark 2 as visited



path(2, 7)?

path(3, 7)?

path(5, 7)?

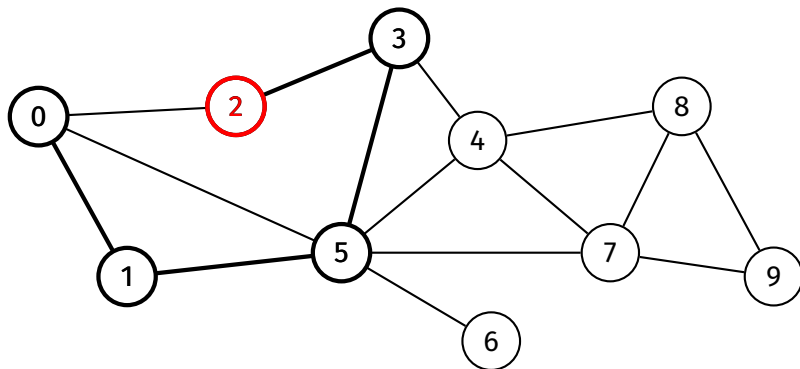
path(1, 7)?

path(0, 7)?

call stack

	[0]	[1]	[2]	[3]	[4]	[5]	[6]	[7]	[8]	[9]
visited	1	1	1	1	0	1	0	0	0	0

Return false



path(2, 7)?

path(3, 7)?

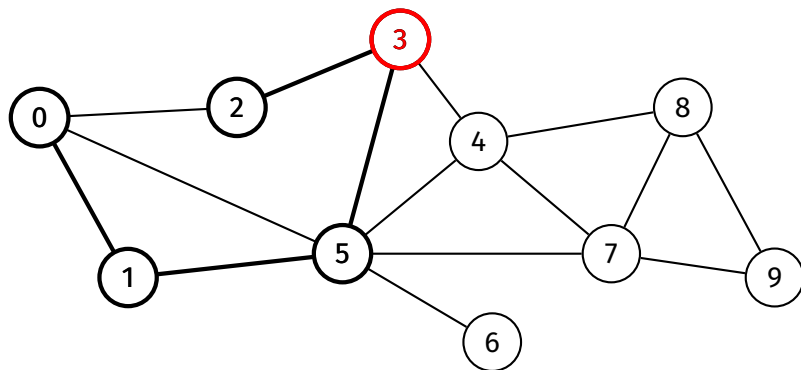
path(5, 7)?

path(1, 7)?

path(0, 7)?

call stack

	[0]	[1]	[2]	[3]	[4]	[5]	[6]	[7]	[8]	[9]
visited	1	1	1	1	0	1	0	0	0	0



path(3, 7)?

path(5, 7)?

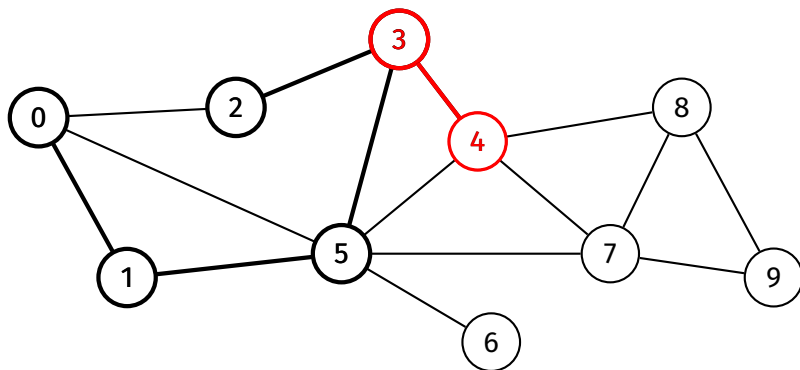
path(1, 7)?

path(0, 7)?

call stack

	[0]	[1]	[2]	[3]	[4]	[5]	[6]	[7]	[8]	[9]
visited	1	1	1	1	0	1	0	0	0	0

4 has not been visited



path(3, 7)?

path(5, 7)?

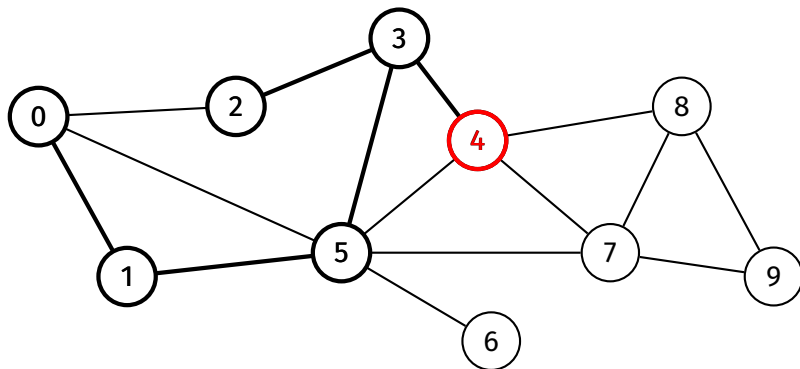
path(1, 7)?

path(0, 7)?

call stack

	[0]	[1]	[2]	[3]	[4]	[5]	[6]	[7]	[8]	[9]
visited	1	1	1	1	0	1	0	0	0	0

Recurse into 4



path(4, 7)?

path(3, 7)?

path(5, 7)?

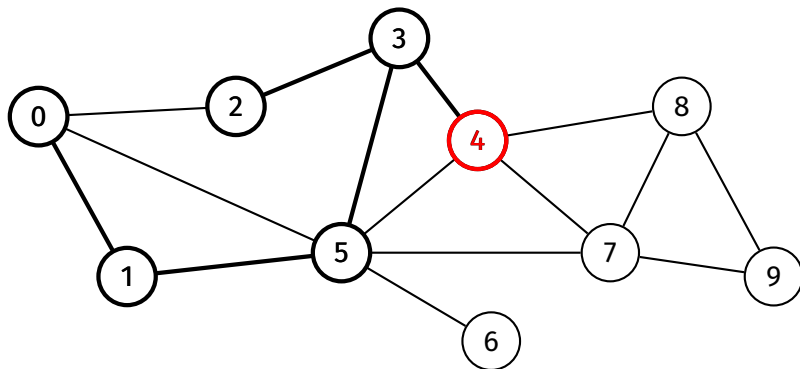
path(1, 7)?

path(0, 7)?

call stack

	[0]	[1]	[2]	[3]	[4]	[5]	[6]	[7]	[8]	[9]
visited	1	1	1	1	0	1	0	0	0	0

Mark 4 as visited



path(4, 7)?

path(3, 7)?

path(5, 7)?

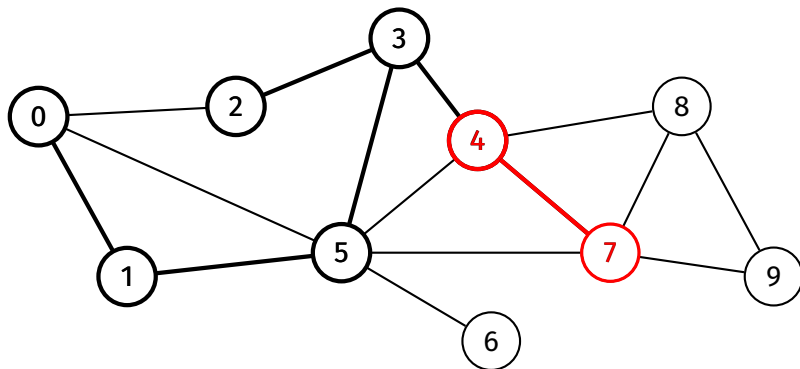
path(1, 7)?

path(0, 7)?

call stack

	[0]	[1]	[2]	[3]	[4]	[5]	[6]	[7]	[8]	[9]
visited	1	1	1	1	1	1	0	0	0	0

7 has not been visited



	[0]	[1]	[2]	[3]	[4]	[5]	[6]	[7]	[8]	[9]
visited	1	1	1	1	1	1	0	0	0	0

path(4, 7)?

path(3, 7)?

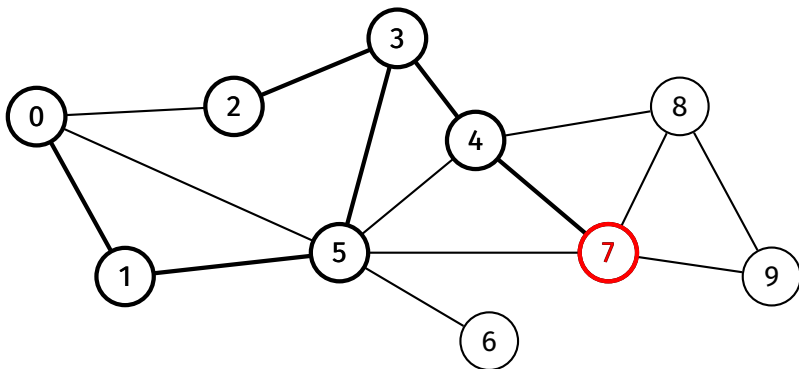
path(5, 7)?

path(1, 7)?

path(0, 7)?

call stack

Recurse into 7



	[0]	[1]	[2]	[3]	[4]	[5]	[6]	[7]	[8]	[9]
visited	1	1	1	1	1	1	0	0	0	0

path(7, 7)?

path(4, 7)?

path(3, 7)?

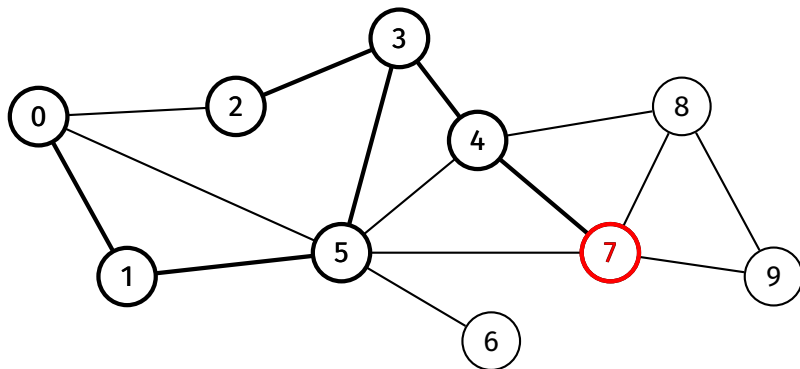
path(5, 7)?

path(1, 7)?

path(0, 7)?

call stack

Mark 7 as visited



	[0]	[1]	[2]	[3]	[4]	[5]	[6]	[7]	[8]	[9]
visited	1	1	1	1	1	1	0	1	0	0

path(7, 7)?

path(4, 7)?

path(3, 7)?

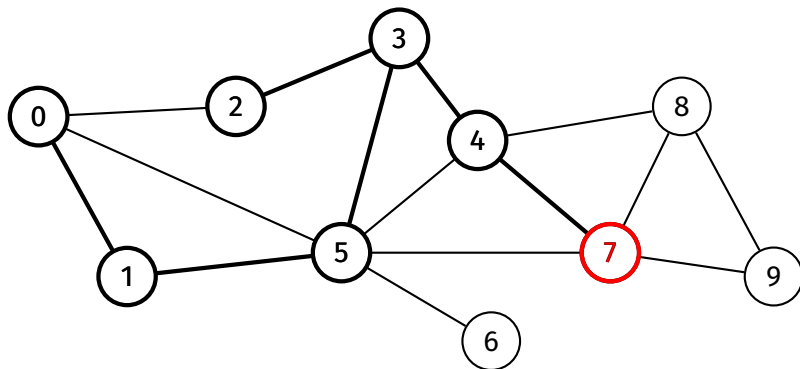
path(5, 7)?

path(1, 7)?

path(0, 7)?

call stack

Return true



	[0]	[1]	[2]	[3]	[4]	[5]	[6]	[7]	[8]	[9]
visited	1	1	1	1	1	1	0	1	0	0

path(7, 7)?

path(4, 7)?

path(3, 7)?

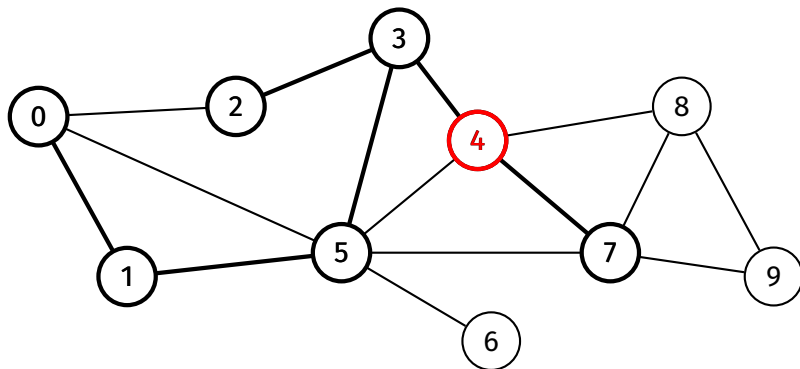
path(5, 7)?

path(1, 7)?

path(0, 7)?

call stack

Return true



path(4, 7)?

path(3, 7)?

path(5, 7)?

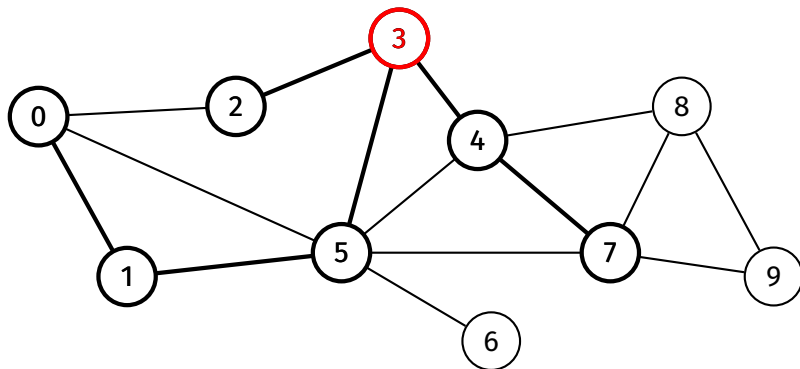
path(1, 7)?

path(0, 7)?

call stack

	[0]	[1]	[2]	[3]	[4]	[5]	[6]	[7]	[8]	[9]
visited	1	1	1	1	1	1	0	1	0	0

Return true



path(3, 7)?

path(5, 7)?

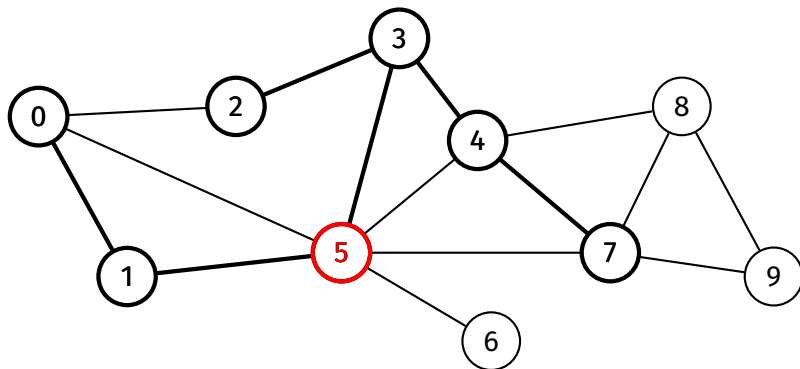
path(1, 7)?

path(0, 7)?

call stack

	[0]	[1]	[2]	[3]	[4]	[5]	[6]	[7]	[8]	[9]
visited	1	1	1	1	1	1	0	1	0	0

Return true



path(5, 7)?

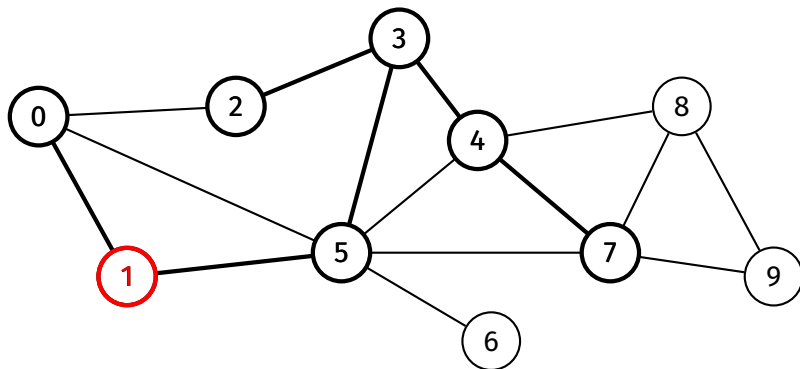
path(1, 7)?

path(0, 7)?

call stack

	[0]	[1]	[2]	[3]	[4]	[5]	[6]	[7]	[8]	[9]
visited	1	1	1	1	1	1	0	1	0	0

Return true



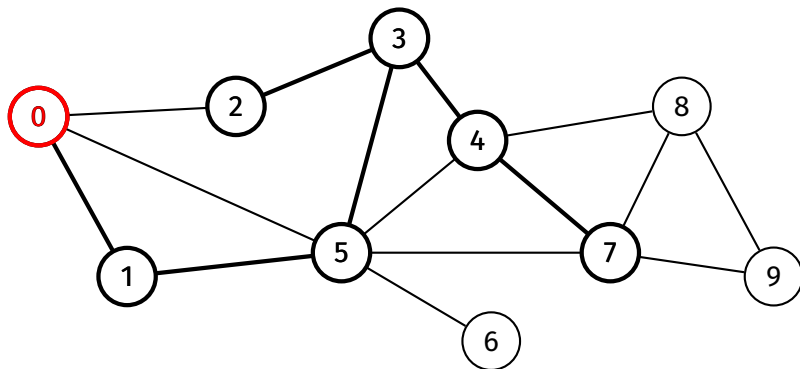
path(1, 7)?

path(0, 7)?

call stack

	[0]	[1]	[2]	[3]	[4]	[5]	[6]	[7]	[8]	[9]
visited	1	1	1	1	1	1	0	1	0	0

Return true

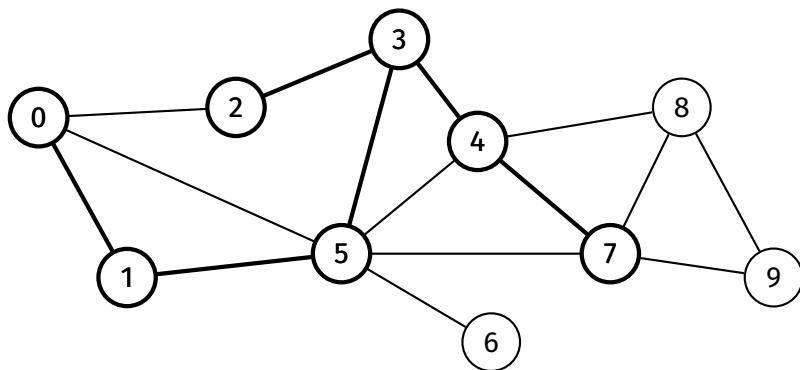


path(0, 7)?

call stack

	[0]	[1]	[2]	[3]	[4]	[5]	[6]	[7]	[8]	[9]
visited	1	1	1	1	1	1	0	1	0	0

Answer: Yes



call stack

	[0]	[1]	[2]	[3]	[4]	[5]	[6]	[7]	[8]	[9]
visited	1	1	1	1	1	1	0	1	0	0