BFS DFS

Ideas/Issues

Appendix

## COMP2521 24T1 Graphs (II)

Graph Traversal

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bfs and dfs path checking path finding

BFS

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Appendix

### Common problems on graphs:

- Is there a path between two vertices?
- What is the shortest path between two vertices?
- Is the graph connected?
- If we remove an edge, is the graph still connected?
- Which vertices are reachable from a particular vertex?
- Is there a cycle that passes through all vertices?

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**Appendix** 

All of the above problems can be solved by a systematic exploration of a graph via its edges.

This systematic exploration is called traversal or search.

BFS

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**Appendix** 

### **PROBLEM**

Is there a path between vertices src and dest?

DFS

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Appendix

## Possible approach:

- $oldsymbol{1}$  Examine vertices adjacent to src
- 2 If any of them is *dest*, we're done!
- **3** Otherwise, check vertices two edges away from src
- $oldsymbol{4}$  Repeat looking further and further away from src

The above summarises one form of graph traversal.

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Appendix

Two primary methods for graph traversal/search:

### Breadth-first search (BFS)

- Prioritises visiting all neighbours over path-following
  - "Go wide"
- Implemented iteratively (using a queue)

### Depth-first search (DFS)

- Prioritises path-following over visiting all neighbours
  - "Go deep"
- Implemented recursively or iteratively (using a stack)

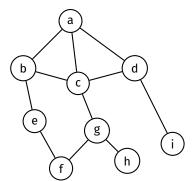
BFS

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In what order would BFS and DFS visit the vertices of this graph?



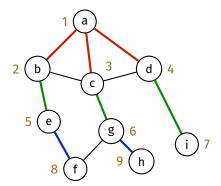
BFS vs. DFS

Graph Traversal BFS and DFS

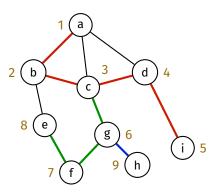
BFS

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Breadth-first search



Depth-first search

#### BFS

Pseudocode Analysis Path Finding

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**Appendix** 

Breadth-first search visits vertices in order of distance from the starting vertex.

It visits the starting vertex, then the neighbours of the starting vertex, then the neighbours of those neighbours, etc.

BFS is implemented iteratively using a queue.

RFS

#### Example Pseudocode Analysis

DF5

Ideas/Issues

Appendix

### Data structures used in BFS:

- Visited array
  - To keep track of which vertices have been visited
- Predecessor array
  - To keep track of the predecessor of each vertex
  - The predecessor of v is the vertex from which we reached v
    - i.e., the vertex before v on the path to v
- Queue
  - First-in-first-out data structure
  - Stores unvisited vertices in the order that they should be visited

#### BFS Example Pseudocode

Pseudocode Analysis Path Findin

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### Algorithm:

- 1 Create/initialise data structures:
  - Create visited array, initialised to false
  - Create predecessor array, initialised to -1
  - Create empty queue
- Mark starting vertex as visited and enqueue it
- 3 While the queue is not empty:
  - Dequeue a vertex
    - Let this vertex be v
  - **2 Explore** v that is, for each of v's unvisited neighbours:
    - Mark it as visited
    - 2 Set its predecessor to v
    - 3 Enqueue it

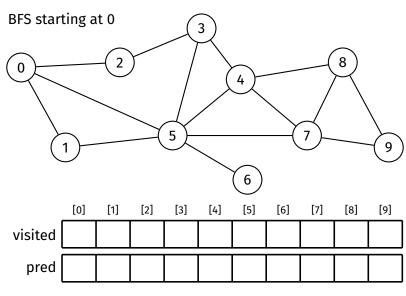
Example

Graph Traversal

BFS Example

Pseudocode Analysis Path Finding

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# Breadth-First Search Example

Graph Traversal

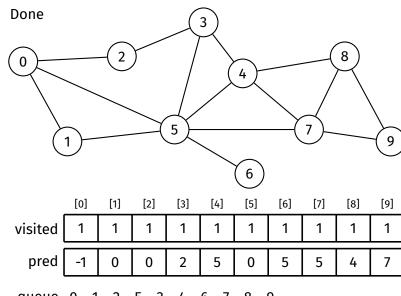
BFS Example

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queue 0 1 2 5 3 4 6 7 8 9



Pseudocode

```
Traversal
BFS
```

```
Pseudocode
DFS
Ideas/Issues
```

```
Appendix
```

```
bfs(G, src):
    Input: graph G, starting vertex src
    create visited array, initialised to false
    create predecessor array, initialised to -1
    create queue Q
    visited[src] = true
    enqueue src into Q
    while Q is not empty:
        v = dequeue from Q
        for each neighbour w of v in G where visited \lceil w \rceil = \text{false}:
            visited[w] = true
            predecessor[w] = v
            enqueue w into Q
```

Simplification

Graph Traversal

BFS Example

> Pseudocode Apalusia

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When using a predecessor array in BFS, the predecessor array can double as a visited array

predecessor[v] = -1 means v is not visited

**Simplification** 

```
Graph
Traversal
```

BFS Example Pseudocode

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```
bfs(G, src):
    Input: graph G, starting vertex src
    create predecessor array, initialised to -1
    create queue Q
    predecessor[src] = src // <- mark src as visited
    enqueue src into Q
    while Q is not empty:
        v = dequeue from Q
        for each neighbour w of v in G where predecessor[w] = -1:
             predecessor[w] = v
             enqueue \boldsymbol{w} into \boldsymbol{Q}
```

BFS Example

Pseudocoo

Path Findin

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Appendix

BFS is O(V + E) when using the adjacency list representation:

- Typical queue implementation has O(1) enqueue and dequeue
- Each vertex is visited at most once  $\Rightarrow O(V)$
- ullet For each vertex, all of its edges are considered once  $\Rightarrow O(E)$

BFS

example Pseudoco

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A BFS finds the shortest path between the starting vertex and all other vertices.

Shortest path in terms of the number of edges

The shortest path between src and dest can be found by tracing backwards through the predecessor array (from dest to src).

BFS

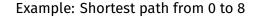
Example Pseudocode

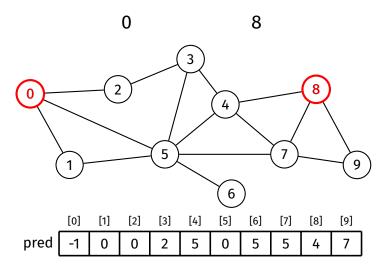
Analysis

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BFS

Example Pseudocode

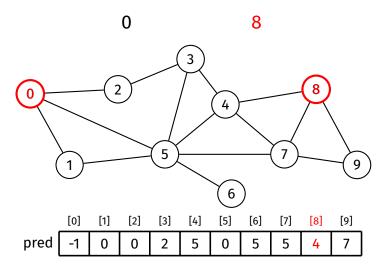
Analysis

Path Finding

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**BFS** 

Example Pseudocode

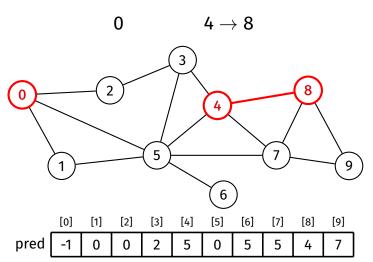
Analysis

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BFS

Example Pseudocode

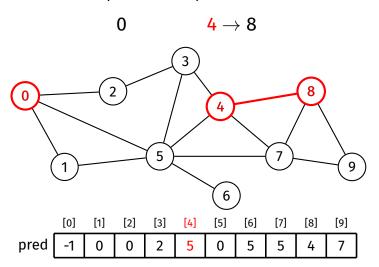
Analysis

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BFS

Example Pseudocode

Analysis

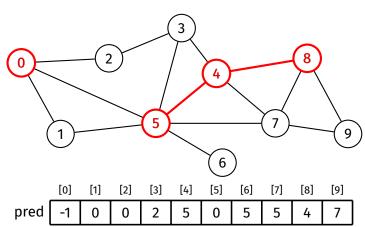
Path Finding

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$$0 \qquad 5 \rightarrow 4 \rightarrow 8$$



BFS

Example Pseudocode

Analysis

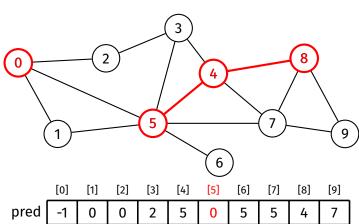
Path Finding

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$$0 \qquad \frac{5}{} \rightarrow 4 \rightarrow 8$$



BFS

Example Pseudocode

Analysis

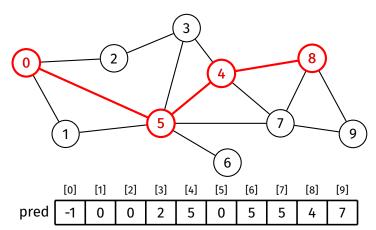
Path Finding

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$$0\longrightarrow 5\rightarrow 4\rightarrow 8$$



## Path-Finding with BFS

```
Graph
Traversal
```

**BFS** 

```
Pseudocode
Analysis
```

Path Finding

Ideas/Issues

```
bfsFindPath(G, src, dest):
    Input: graph G, vertices src and dest
... BFS starting from src ...

if predecessor[dest] \neq -1:
    v = dest
    while v \neq src:
        print v, "<-"
    v = dest
    print v = predecessor[v]
```

BFS

#### DFS

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Depth-first search goes as far down one path as possible until it reaches a dead end, then backtracks until it finds a new path to take, then repeats

DFS can be implemented recursively or iteratively.

Graph Traversal

BFS

#### Recursive

Pseudocode Example Analysis Path checkin Path finding

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Appendix

Depth-first search is described recursively as:

- 1 Mark current vertex as visited
  - The first time, this is the starting vertex
- 2 For each neighbour of the current vertex:
  - If it has not been visited:
    - Recursively traverse starting from that vertex

The recursion naturally induces backtracking.

Pseudocode

```
Graph
Traversal
```

BFS
DFS
Recursive

Pseudocode

Analysis
Path checki

Path checking Path finding Iterative

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Example

Graph Traversal

BFS DFS

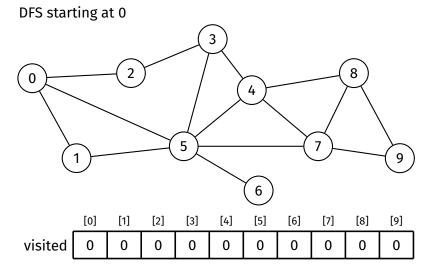
Recursive

Pseudoco Example Analysis

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Path checking
Path finding
Iterative

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**Appendix** 



visit order

Example

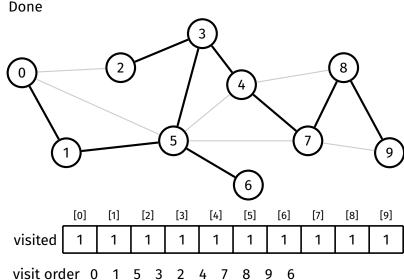
Graph Traversal

BFS

DFS Recursive

Example Analysis Path checking Path finding

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**Analysis** 

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Recursive

Pseudocoo

Analysis

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Recursive DFS is O(V + E) when using the adjacency list representation:

- Each vertex is visited at most once  $\Rightarrow O(V)$ 
  - Function is called on each vertex at most once
- For each vertex, all of its edges are considered once  $\Rightarrow O(E)$

## Path-Checking with Recursive DFS

Graph Traversal

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Path checking

Path findin

Ideas/Issues

**Appendix** 

Recursive DFS can be adapted to check if a path exists between two vertices.

### Idea:

- To check if a path exists between *src* and *dest*:
  - If src = dest, then there is a path (the empty path)
  - ullet Otherwise, for each neighbour of src, recursively check if there is a path from that neighbour to dest

BFS DFS

Recursive

Pseudocode

Analysis

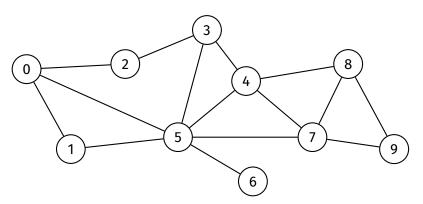
Path checking

Path finding

Ideas/Issues

**Appendix** 

Does there exist a path between 0 and 7 in this graph?



BFS DFS

Recursive

Pseudocod

Example Analysis

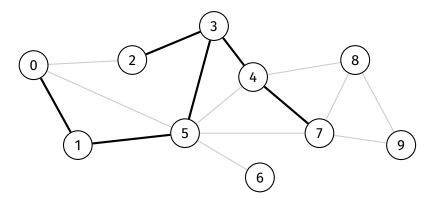
Path checking

Path finding Iterative

Ideas/Issues

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### Answer: Yes



## Path-Checking with Recursive DFS

Pseudocode

```
Traversal
           dfsHasPath(G, src, dest):
BFS
               Input: graph G, vertices src and dest
               Output: true if there is a path from src to dest
                        false otherwise
               create visited array, initialised to false
Path checking
               return dfsHasPathRec(G, src, dest, visited)
Ideas/Issues
           dfsHasPathRec(G, v, dest, visited):
Appendix
               Input: graph G, vertices v and dest, visited array
               visited[v] = true
               if v = dest:
                    return true
               for each neighbour w of v in G:
                    if visited[w] = false:
                        if dfsHasPathRec(G, w, dest, visited):
                            return true
               return false
```

# Path-Checking with Recursive DFS

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Path findi

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O(V + E) when using the adjacency list representation:

• Algorithm is just a modified recursive DFS with return statements

# Path-Finding with Recursive DFS

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Knowing whether a path exists can be useful.

Knowing what the path is can be even more useful.

#### Idea:

- Record the predecessor of each vertex during the DFS
- Trace backwards through the path after the DFS

# Path-Finding with Recursive DFS

Pseudocode

```
Graph
Traversal
BFS
```

```
Recursive
Pseudoco
```

Pseudocode Example Analysis Path checking

Path finding

Ideas/Issues

Appendix

```
dfsFindPath(G, src, dest):
    Input: graph G, vertices src and dest
    create predecessor array, initialised to -1
    predecessor[src] = src
    if dfsFindPathRec(G, src, dest, predecessor):
        v = dest
        while v \neq src:
            print v, "<-"
            v = predecessor[v]
        print src
```

```
Graph
Traversal
BFS
```

```
DFS
Recursive
```

```
Pseudocode
Example
```

Path checking

Path finding Iterative

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Appendix

```
dfsFindPathRec(G, v, dest, predecessor):
    if v = dest:
        return true

for each neighbour w of v in G:
    if predecessor[w] = -1:
        predecessor[w] = v
        if dfsFindPathRec(G, w, dest, predecessor):
        return true
```

return false

BFS DFS

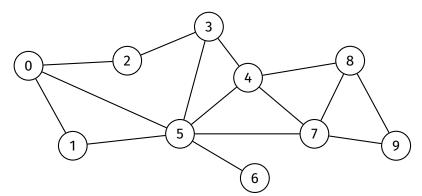
#### Recursive

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Path checking
Path finding

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Appendix

### Find a path from 0 to 7



# Path-Finding with Recursive DFS

Example

Graph Traversal

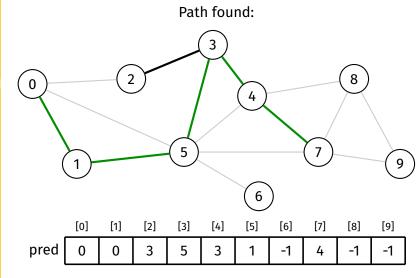
#### BFS DFS

# Recursive

Path checking Path finding

Ideas/Issues

**Appendix** 



Clearly, DFS is not guaranteed to find the shortest path.

## **Iterative Depth-First Search**

Graph Traversal

BFS

DFS

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Applyoid

Ideas/Issues

**Appendix** 

DFS can be implemented iteratively.

Iterative DFS is similar to BFS, but there are a few crucial differences:

- DFS uses a stack instead of a queue
- DFS marks a vertex as visited after removing it from the stack, not when adding it (which is what BFS does, but with a queue)

# Iterative Depth-First Search

Pseudocode

```
Traversal
            dfs(G, src):
BFS
                Input: graph G, vertex src
                create visited array, initialised to false
Pseudocode
Analysis
                create predecessor array, initialised to -1
Ideas/Issues
                create stack S
Appendix
                push src onto S
                while S is not empty:
                     v = pop from S
                     if visited[v] = true:
                         continue // i.e., return to start of loop
                     visited[v] = true
                     for each neighbour w of v in G where visited \lceil w \rceil = \text{false}:
                         predecessor[w] = v
                         push w onto S
```

# Iterative Depth-First Search

Analysis

Traversal

BES

#### DFS

Iterative

Analysis

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Appendix

Iterative DFS is O(V + E) when using the adjacency list representation.

- Typical stack implementation has O(1) push and pop
- Each vertex visited at most once  $\Rightarrow O(V)$
- For each vertex, all of its edges are considered  $\Rightarrow O(E)$

BFS

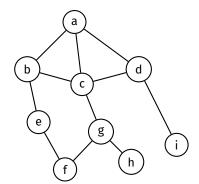
DFS

Ideas/Issues Spanning Trees Disconnected

Appendix

### The edges traversed in a graph traversal form a spanning tree.

### Consider the following graph:



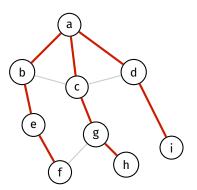
BFS

DFS

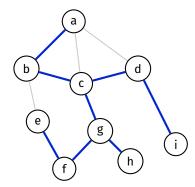
Ideas/Issues Spanning Trees Disconnected

Appendix

### A traversal starting at vertex 'a' forms the following spanning trees:



Breadth-first search



Depth-first search

BFS DFS

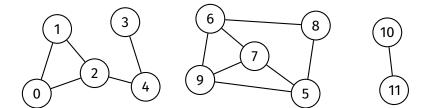
Ideas/Issues

Spanning Trees

Disconnected Graphs

**Appendix** 

If a graph is not connected, a graph traversal starting from a given vertex will not traverse the entire graph



BFS

Ideas/Issues

lueas/issues

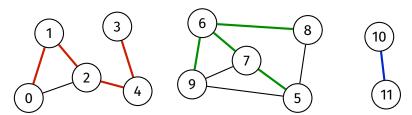
Disconnected Graphs

**Appendix** 

#### Solution

After initial traversal is complete, perform traversal again on an unvisited vertex, repeat until all vertices are visited

This produces a spanning forest



## **Disconnected Graphs**

```
Graph
Traversal
```

BFS DFS

Ideas/Issues

Spanning Trees
Disconnected
Graphs

Appendix

```
dfs(G):
    Input: graph G

    create predecessor array, initialised to -1

for each vertex v in G:
    if predecessor[v] = -1:
        dfsRec(G, v, predecessor)

...
```

BFS

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Ideas/Issues Spanning Trees

Disconnected Graphs

**Appendix** 

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BFS DFS

Ideas/Issues

#### **Appendix**

BFS Example

DFS Example Path-Checking Example

# **Appendix**

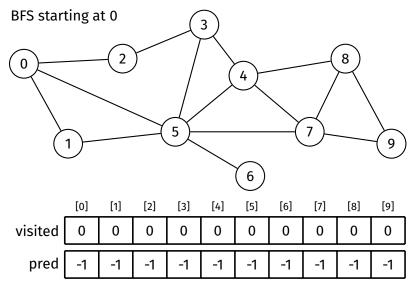
**BFS** 

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Appendix BFS Example

DFS Example Path-Checking Example





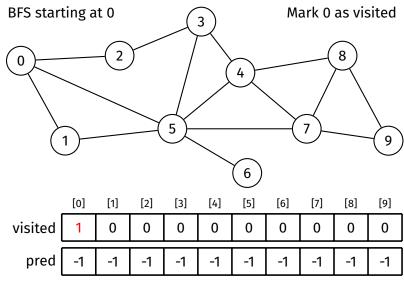
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BFS Example

DFS Example Path-Checking Example



BFS

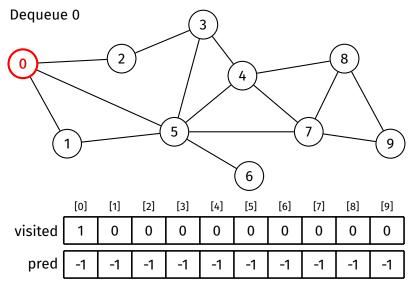
DFS

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BFS Example DFS Example

DFS Example Path-Checking Example



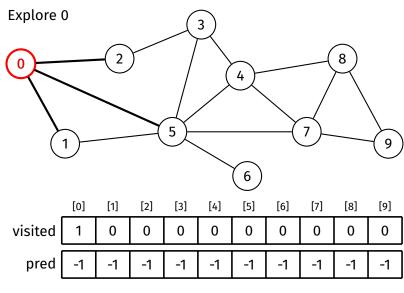
BFS DFS

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Appendix BFS Example

DFS Example Path-Checking Example



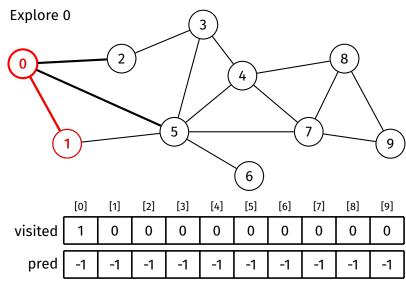
BFS

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Appendix BFS Example

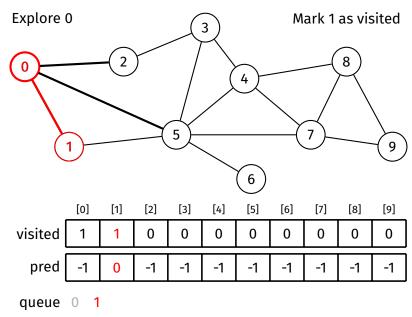
DFS Example Path-Checking Example



BFS DFS

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Appendix BFS Example



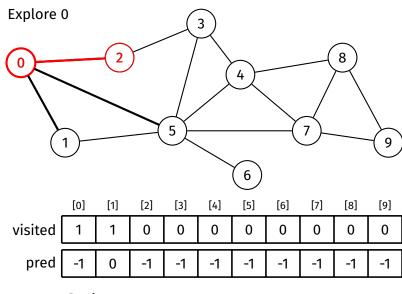
**BFS** 

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Appendix BFS Example

DFS Example Path-Checking Example



queue 0 1

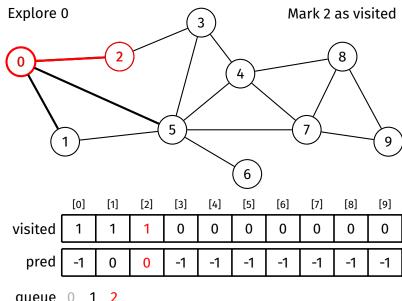


DFS

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**Appendix** BFS Example

DFS Example Path-Checking



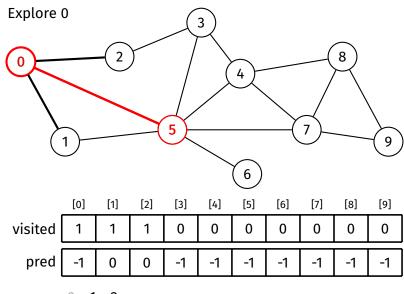


DFS

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Appendix BFS Example

DFS Example Path-Checking Example



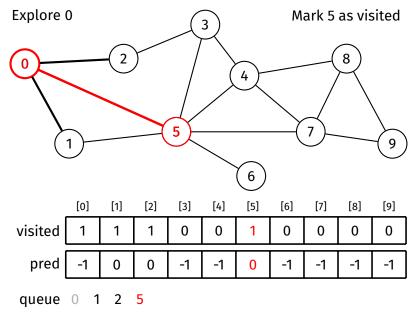
queue 0 1 2



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Appendix BFS Example

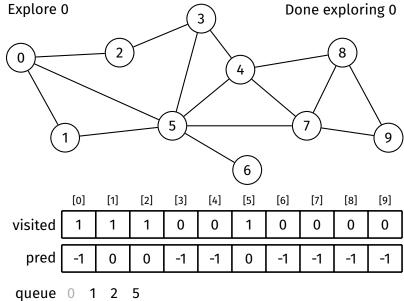




DFS

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**Appendix** BFS Example

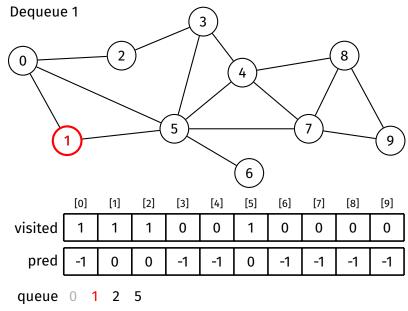




DFS

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Appendix BFS Example



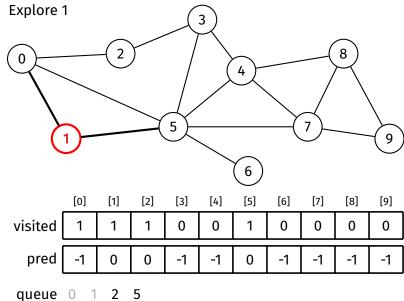


DFS

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**Appendix** BFS Example

DFS Example Path-Checking

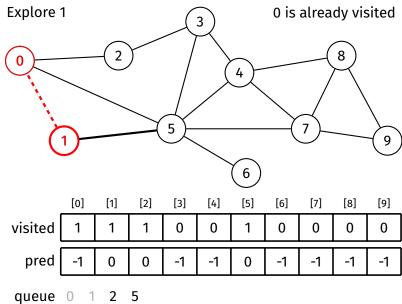




DFS

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**Appendix** BFS Example

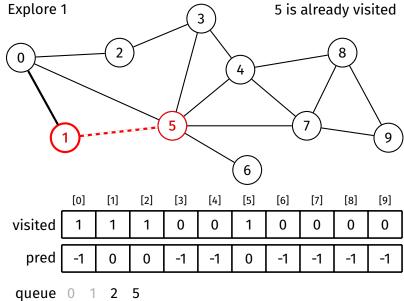




DFS

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**Appendix** BFS Example



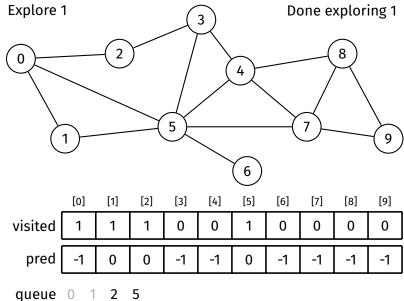


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**Appendix** 

BFS Example



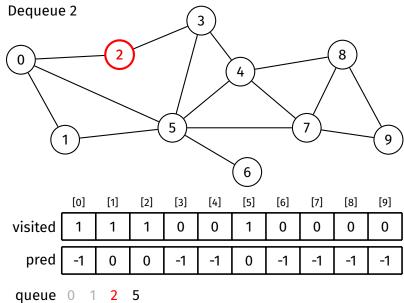
BFS

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**Appendix** BFS Example

DFS Example Path-Checking

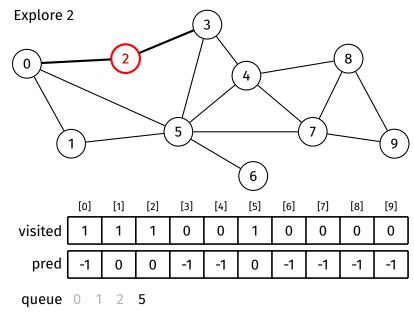




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#### Appendix BFS Example



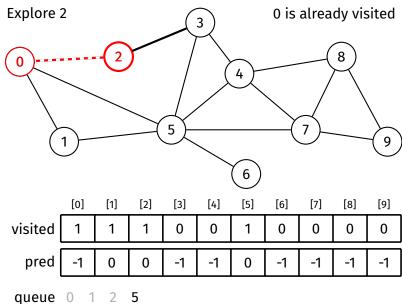
BFS

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**Appendix** BFS Example

DFS Example Path-Checking Example



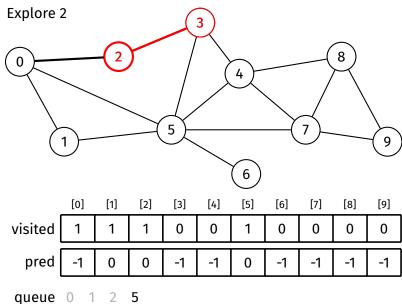
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**Appendix** BFS Example

DFS Example Path-Checking

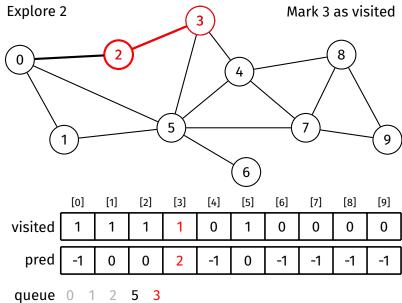


BFS

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**Appendix** BFS Example



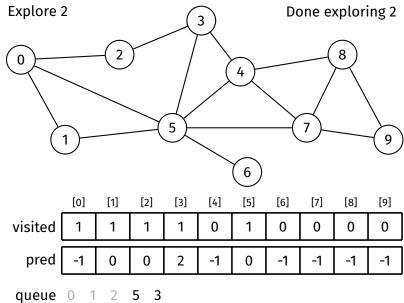


DFS

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**Appendix** 

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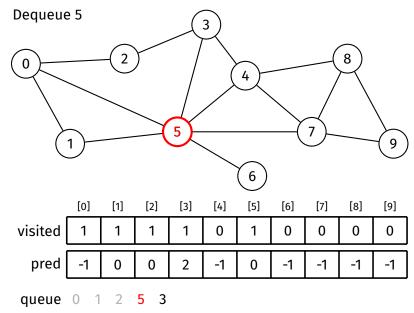


BFS

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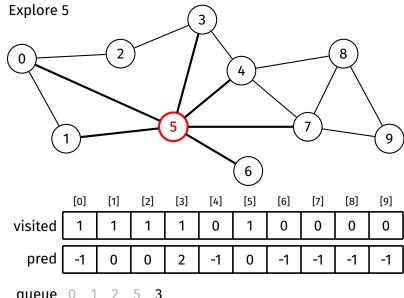


DFS

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**Appendix** BFS Example

DFS Example Path-Checking



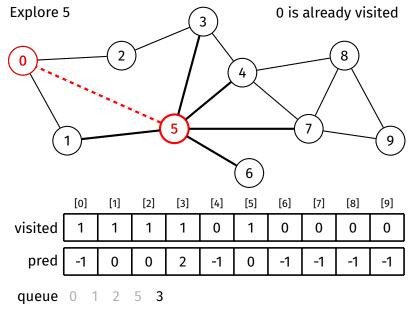
queue

**BFS** 

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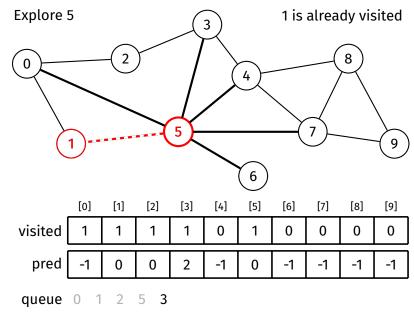


**BFS** 

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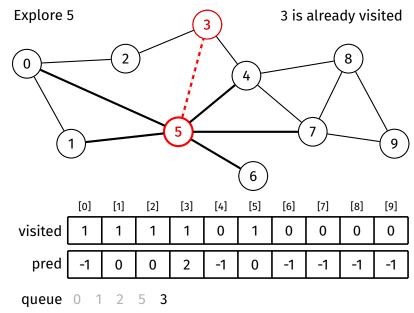


DFS

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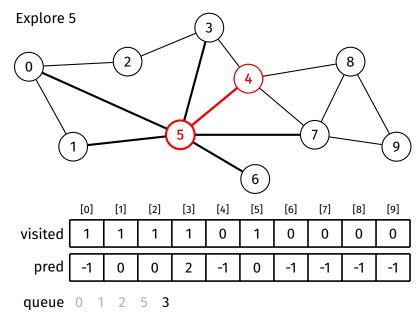




DFS

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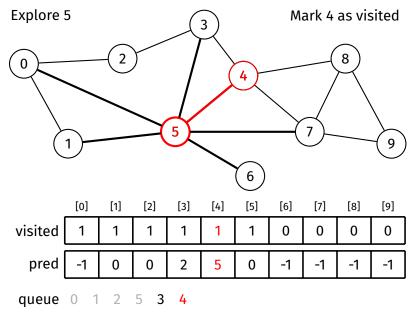


**BFS** 

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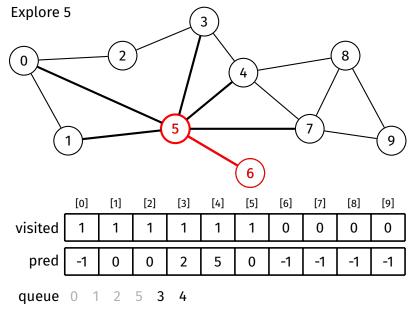




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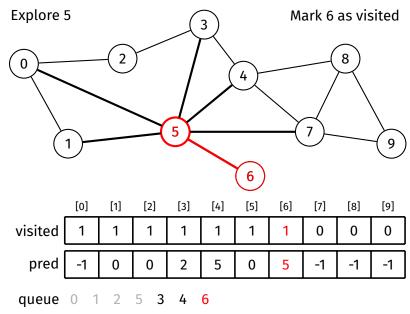


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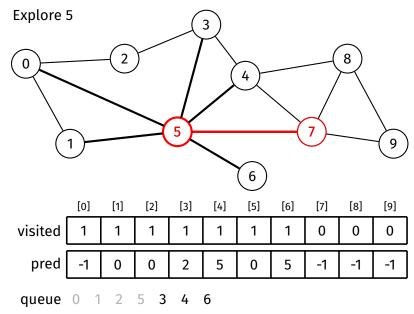




DFS

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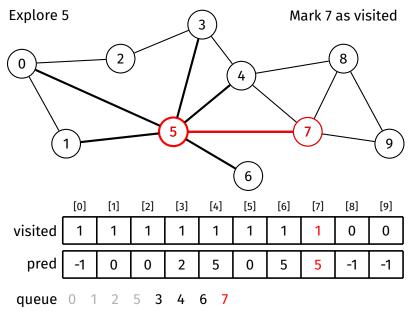




DFS

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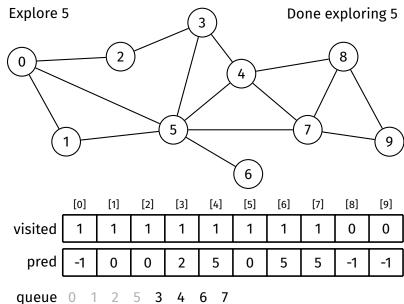




DFS

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## **Appendix** BFS Example



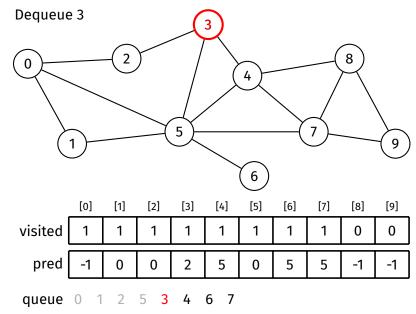


DFS

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DFS Example Path-Checking

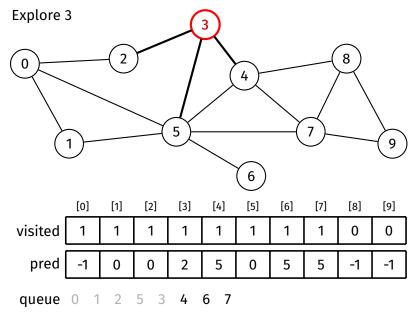


**BFS** 

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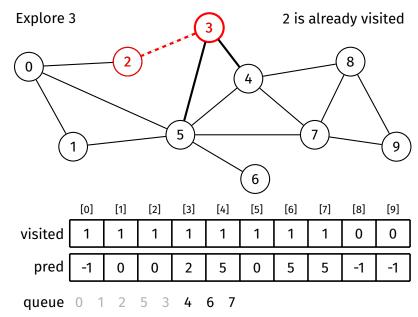




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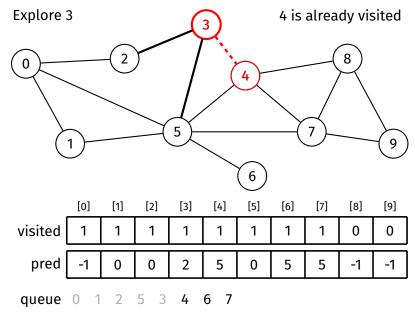




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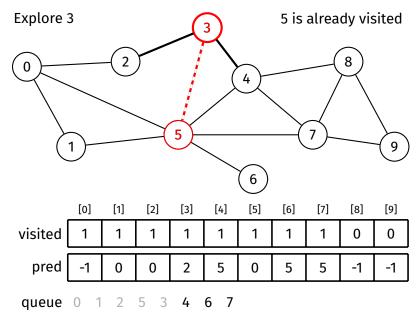


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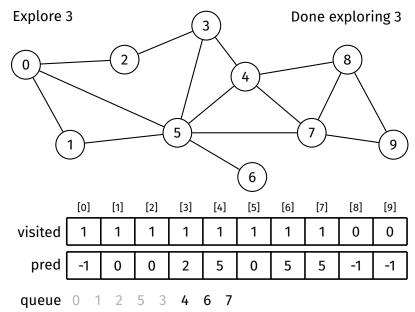


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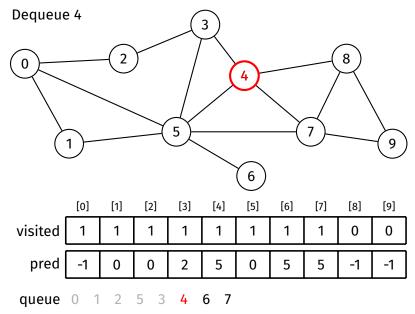


**BFS** 

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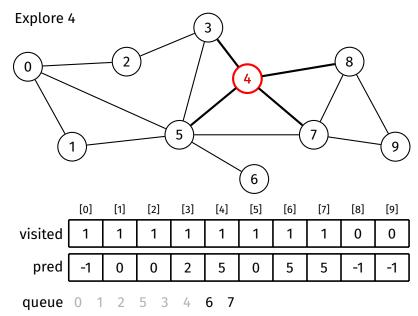




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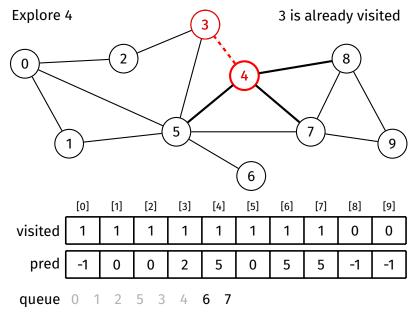




DFS

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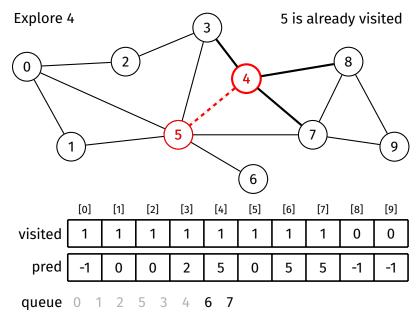




DFS

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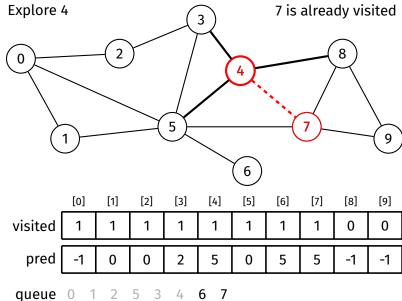




DFS

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**Appendix** BFS Example

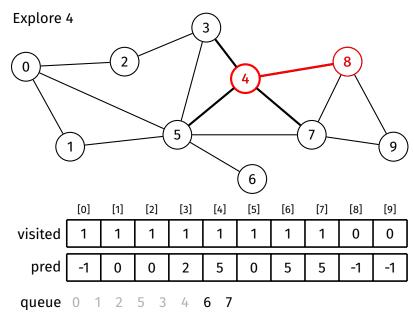




DFS

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## Appendix BFS Example





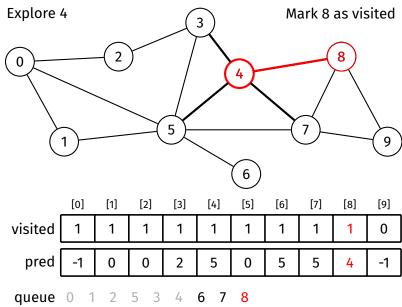
DFS

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Path-Checking Example



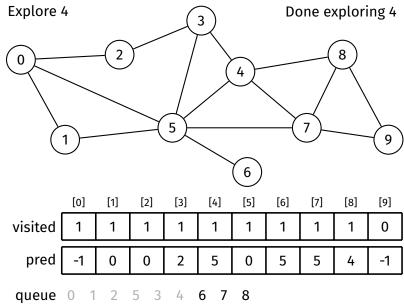


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Appendix BFS Example

DFS Example Path-Checking Example



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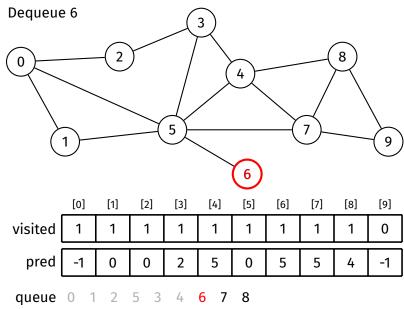
BFS

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DFS Example Path-Checking



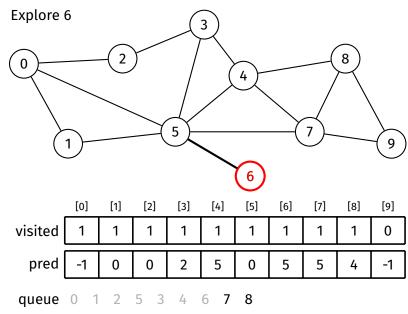




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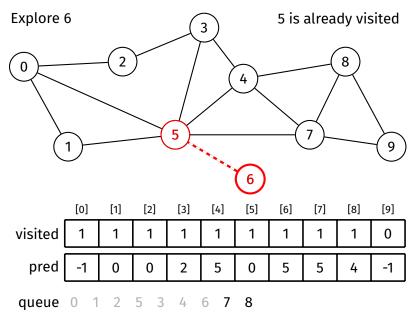




DFS

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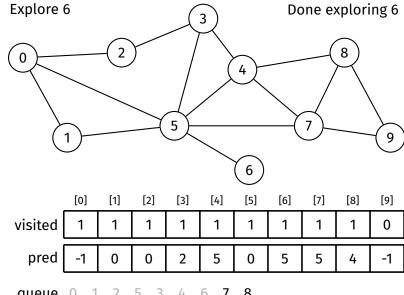


DFS

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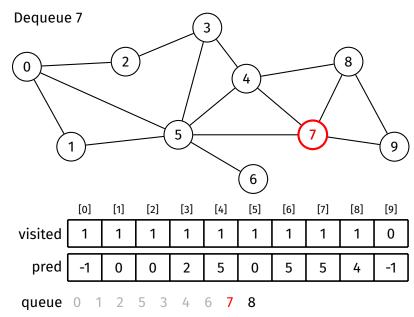
queue

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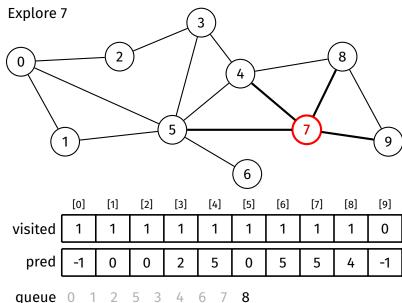


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**Appendix** BFS Example

DFS Example Path-Checking



queue



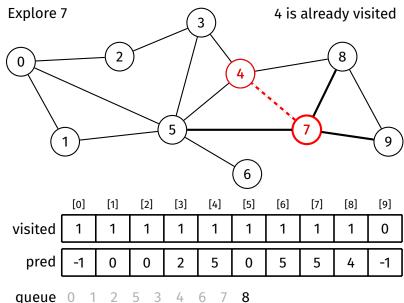
DFS

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**Appendix** 

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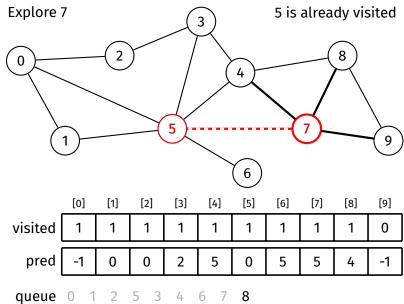
queue



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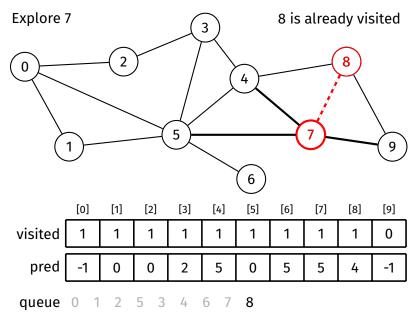
DFS

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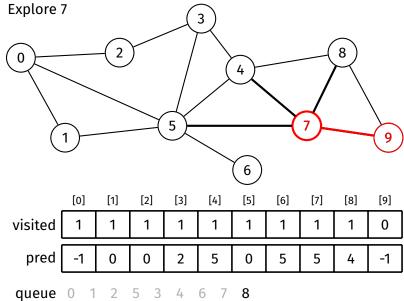


DFS

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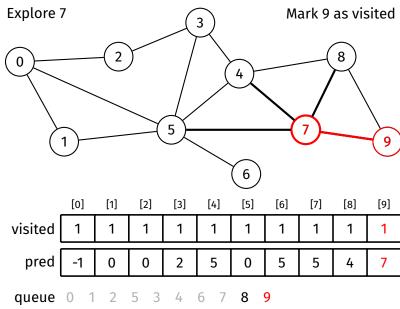


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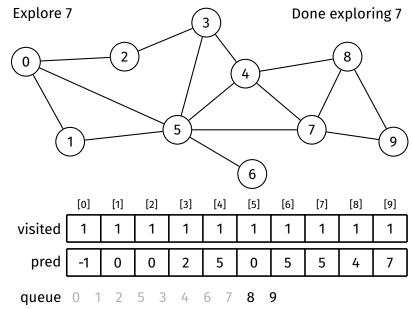




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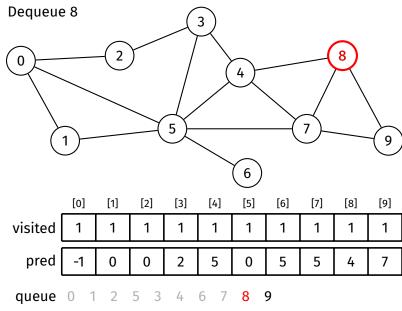




DFS

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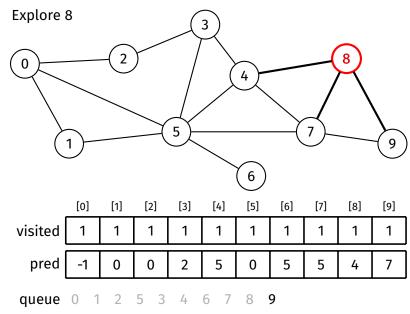
DFS

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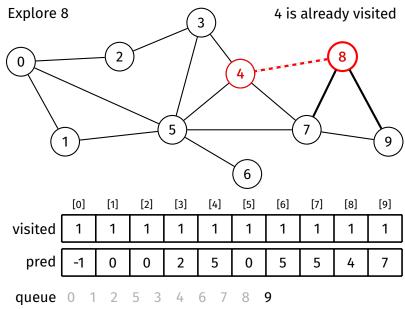




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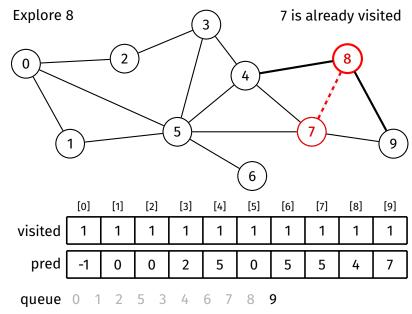




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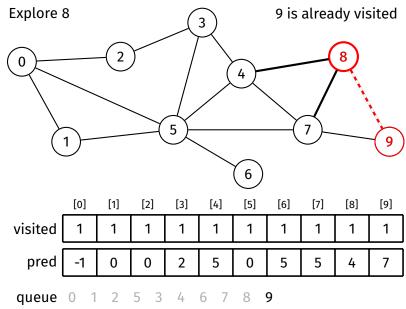




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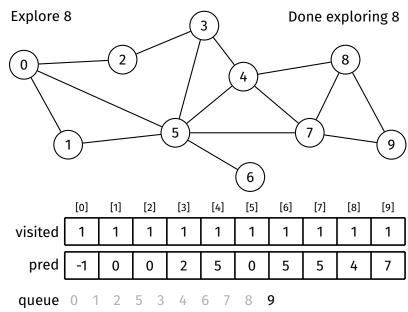


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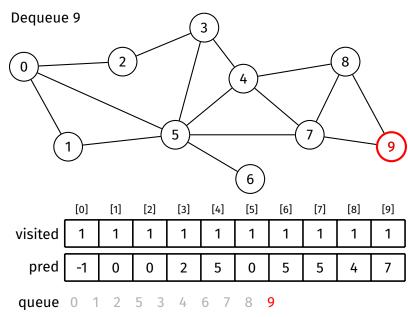
DFS

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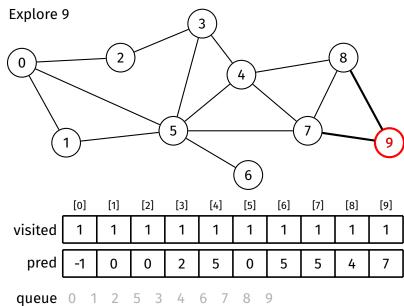


DFS

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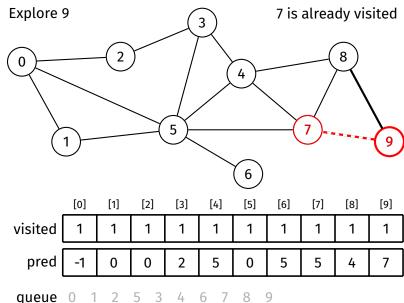


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DFS Example Path-Checking Example



queue

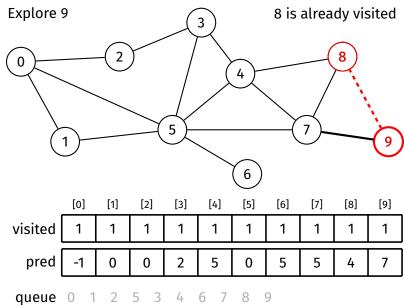


DFS

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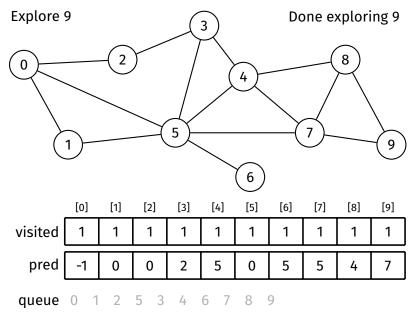




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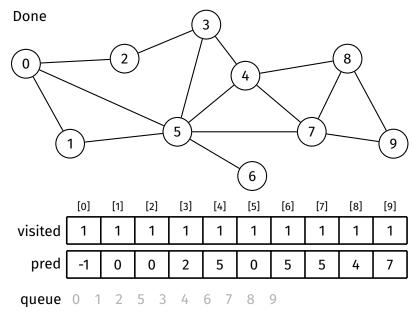




DFS

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BFS

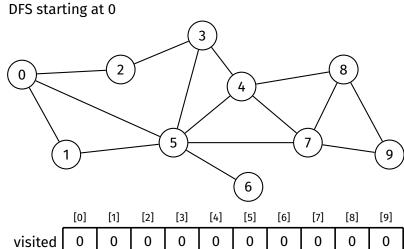
DFS

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DFS Example

Path-Checking Example



1

visited \_\_\_

visit order

call stack

BFS DFS

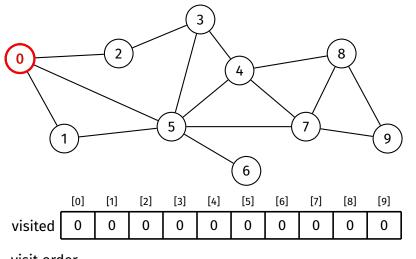
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**Appendix** 

BFS Example

DFS Example

Path-Checking Example



visit order

dfs(0)

call stack

BFS

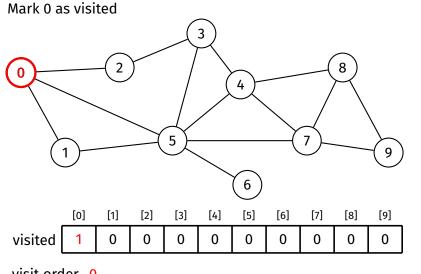
DFS

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**Appendix** 

BFS Example DFS Example

Path-Checking



dfs(0)

call stack

visit order 0

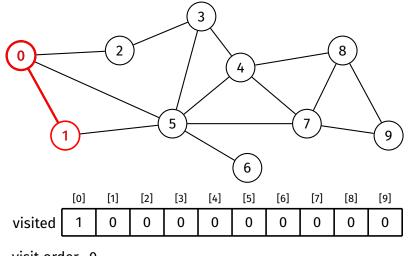
BFS DFS

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**Appendix** BFS Example

DFS Example

Path-Checking Example



dfs(0)

call stack

visit order 0

1 has not been visited

**BFS** 

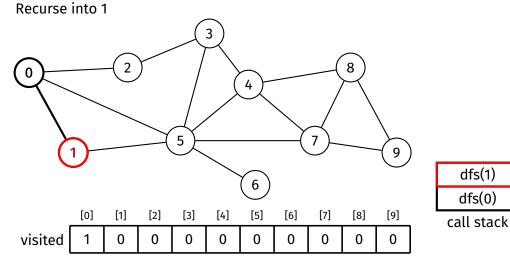
DFS

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Path-Checking Example



visit order 0

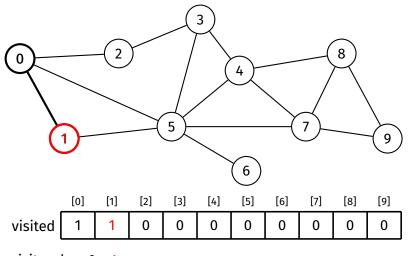
BFS DFS

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DFS Example

Path-Checking



dfs(1) dfs(0) call stack

visit order 0 1

Mark 1 as visited

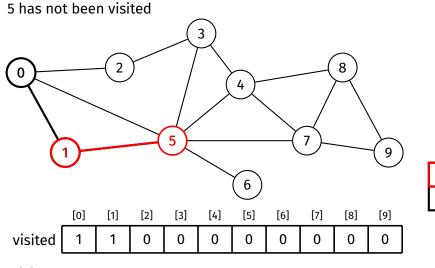
BFS DFS

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dfs(1) dfs(0)

call stack

visit order 0 1

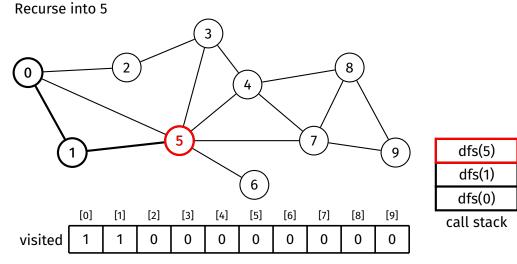
BFS DFS

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Path-Checking



visit order 0 1

BFS

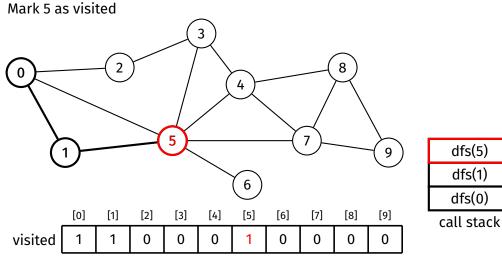
DFS

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visit order 0 1 5

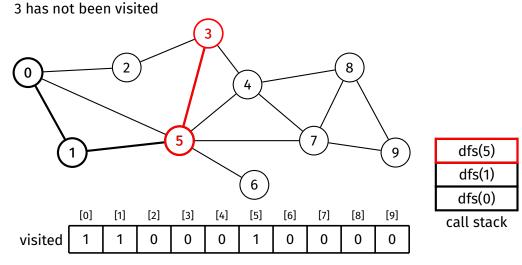
BFS DFS

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visit order 0 1 5

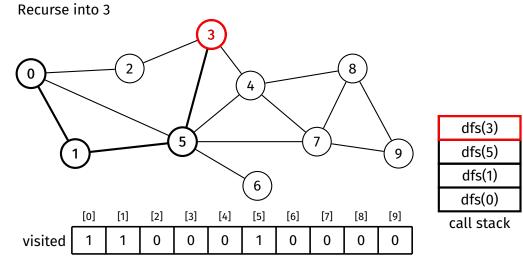
BFS DFS

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visit order 0 1 5

BFS

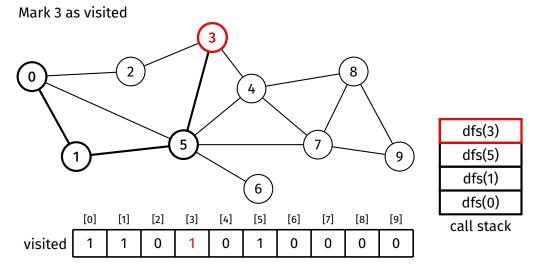
DFS

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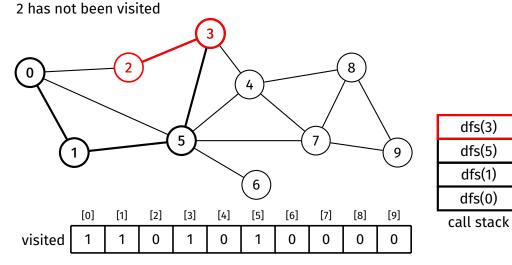
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DFS

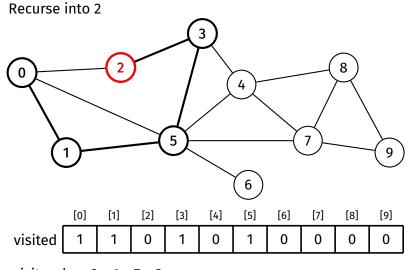
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Path-Checking Example



dfs(0)call stack

dfs(2)

dfs(3)

dfs(5) dfs(1)

BFS DFS

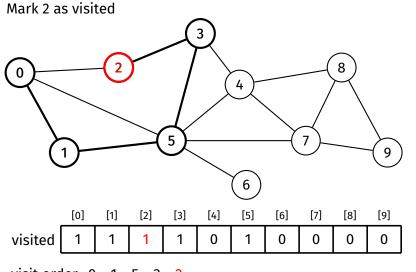
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BFS Example

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Path-Checking Example



dfs(3)dfs(5) dfs(1) dfs(0)call stack

dfs(2)

**BFS** 

DFS

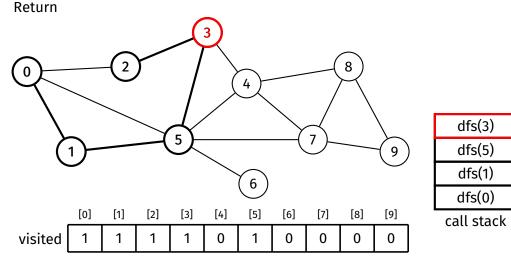
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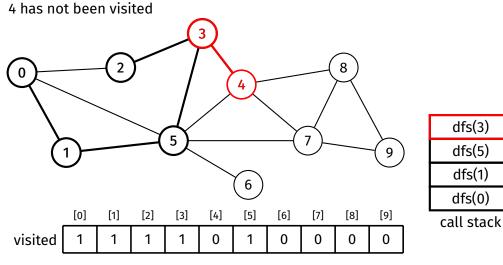
BFS DFS

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DFS Example

Path-Checking Example



dfs(4)

dfs(3)

dfs(5) dfs(1)

dfs(0)

Graph Traversal

**BFS** 

DFS

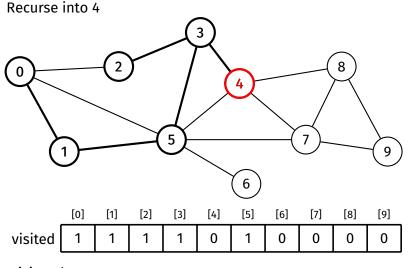
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BFS Example

DFS Example

Path-Checking Example



call stack

BFS

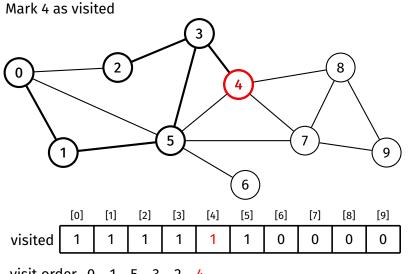
DFS

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**Appendix** 

BFS Example DFS Example

Path-Checking Example



dfs(3)dfs(5) dfs(1) dfs(0)call stack

dfs(4)

visit order 0 1

**BFS** 

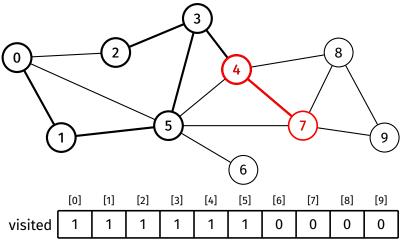
DFS

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DFS Example

Path-Checking Example



dfs(3)
dfs(5)
dfs(1)
dfs(0)

dfs(4)

call stack

visit order 0 1 5 3 2 4

7 has not been visited

BFS

DFS

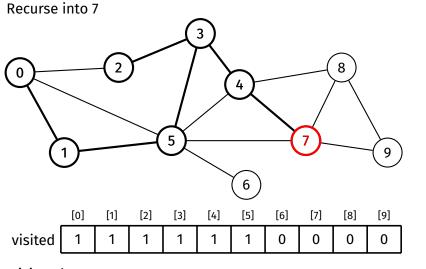
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Path-Checking Example



dfs(4)
dfs(3)
dfs(5)
dfs(1)
dfs(0)
call stack

dfs(7)

visit order 0 1 5 3 2 4

BFS

DFS

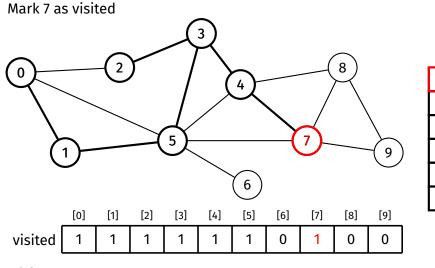
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Path-Checking Example



dfs(4)
dfs(3)
dfs(5)
dfs(1)
dfs(0)
call stack

dfs(7)

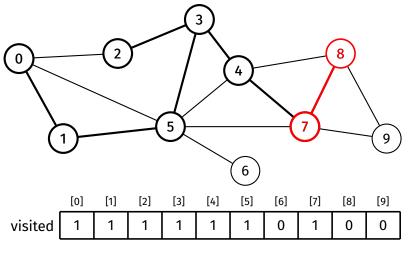
BFS DFS

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DFS Example

Path-Checking Example



dfs(4)
dfs(3)
dfs(5)
dfs(1)
dfs(0)
call stack

dfs(7)

visit order 0 1 5 3 2 4 7

8 has not been visited

dfs(8)

dfs(7)

dfs(4) dfs(3)

dfs(5) dfs(1)

Graph Traversal

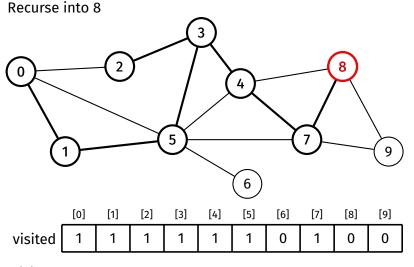
BFS DFS

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**Appendix** BFS Example

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Path-Checking Example



dfs(0)call stack

visit order 0 1 5 3 2 4 7 Traversal

BFS

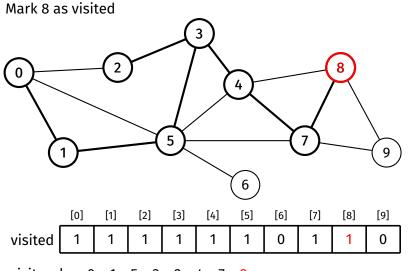
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dfs(4) dfs(3)dfs(5) dfs(1) dfs(0)call stack

dfs(8)

dfs(7)

**BFS** 

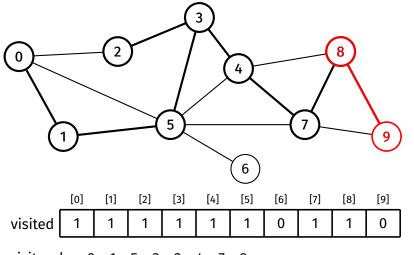
DFS

Ideas/Issues

Appendix

BFS Example
DFS Example

Path-Checking Example



dfs(4) dfs(3) dfs(5) dfs(1) dfs(0)

call stack

dfs(8)

dfs(7)

visit order 0 1 5 3 2 4 7 8

9 has not been visited

BFS

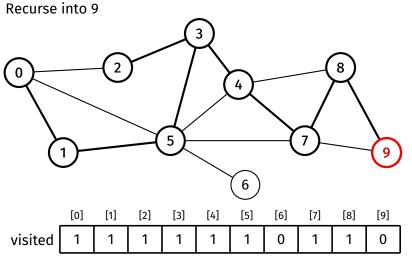
DFS

Ideas/Issues

Appendix

BFS Example
DFS Example

Path-Checking Example



dfs(9) dfs(8) dfs(7)dfs(4) dfs(3)dfs(5) dfs(1) dfs(0)call stack

Mark 9 as visited

Traversal

BFS

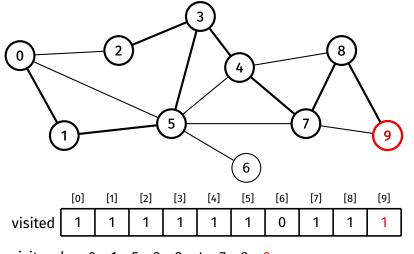
DFS

Ideas/Issues

**Appendix** 

BFS Example DFS Example

Path-Checking Example



dfs(9) dfs(8) dfs(7)dfs(4) dfs(3)

dfs(5)

dfs(1)

dfs(0)call stack

visit order 0 5 3 2

BFS

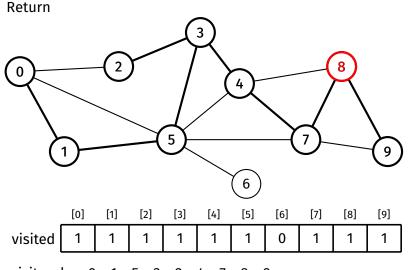
DFS

Ideas/Issues

Appendix

BFS Example
DFS Example

Path-Checking Example



dfs(4)
dfs(3)
dfs(5)
dfs(1)
dfs(0)
call stack

dfs(8)

dfs(7)

**BFS** 

DFS

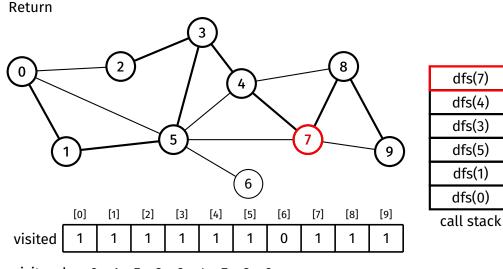
Ideas/Issues

lueas/issui

Appendix BFS Example

DFS Example

Path-Checking



BFS

DFS

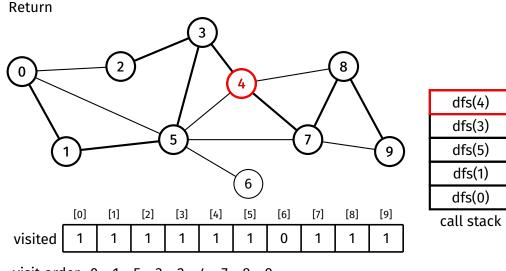
Ideas/Issues

Appendix

BFS Example

DFS Example

Path-Checking



Return

Graph Traversal

BFS

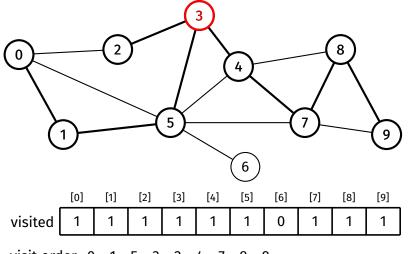
DFS

Ideas/Issues

Appendix

BFS Example
DFS Example

Path-Checking



dfs(5) dfs(1) dfs(0) call stack

dfs(3)

BFS

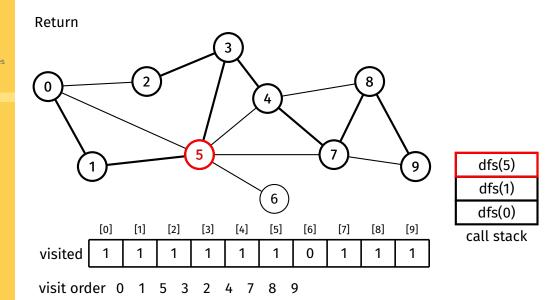
DFS

Ideas/Issues

Appendix

BFS Example

DFS Example



BFS

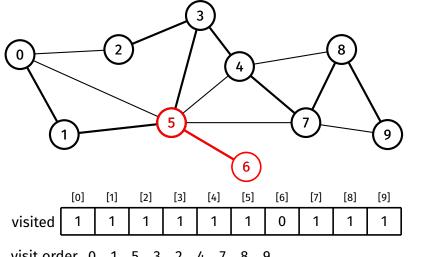
DFS

Ideas/Issues

**Appendix** 

BFS Example DFS Example

Path-Checking Example



dfs(5) dfs(1) dfs(0)

call stack

visit order 0 1 5 3 2

6 has not been visited

BFS

DFS

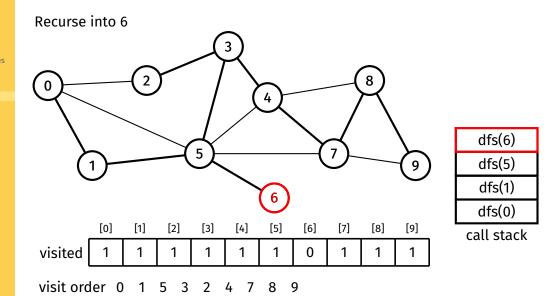
Ideas/Issues

Appendix

BFS Example

DFS Example

Path-Checking Example



BFS

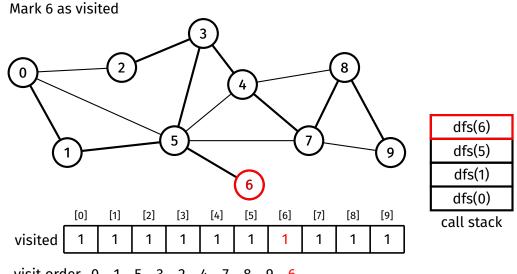
DFS

Ideas/Issues

**Appendix** BFS Example

DFS Example

Path-Checking Example



visit order 0 1 5 3 2

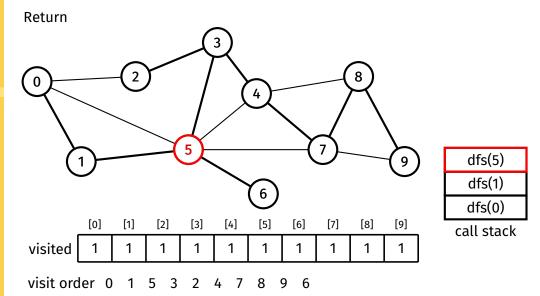
BFS

DFS

Ideas/Issues

**Appendix** BFS Example

DFS Example



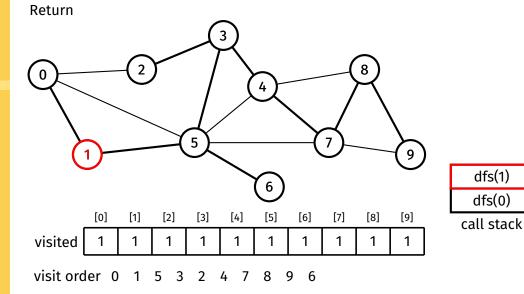
BFS

DFS

Ideas/Issues

Appendix BFS Example

DFS Example



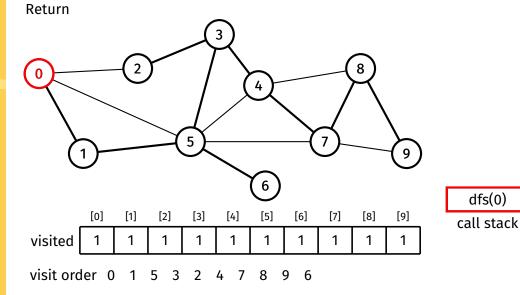
BFS

DFS

Ideas/Issues

Appendix BFS Example

DFS Example



BFS

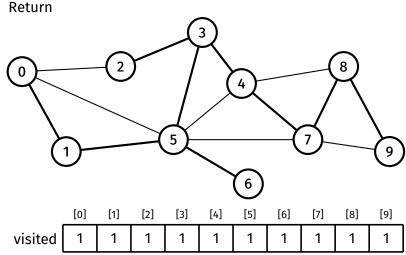
DFS

Ideas/Issues

**Appendix** BFS Example

DFS Example

Path-Checking



visit order 0 1 5 3 2

BFS DFS

Ideas/Issues

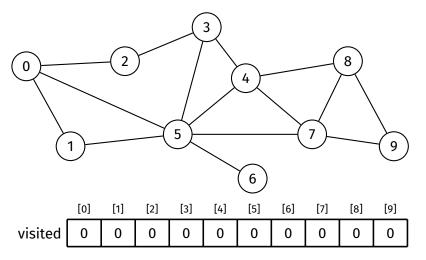
10003/13300

Appendix BFS Example

DEC Evernel

Path-Checking Example

### Is there a path between 0 and 7?



### Path-Checking with Recursive DFS

Example

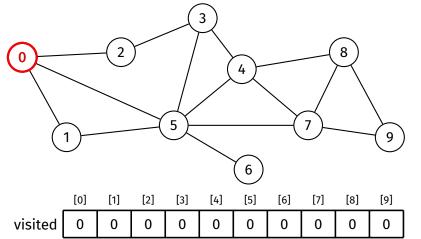
Graph Traversal

BFS DFS

Ideas/Issues

**Appendix** BFS Example

Path-Checking Example



path(0, 7)?

BFS DFS

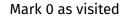
Ideas/Issues

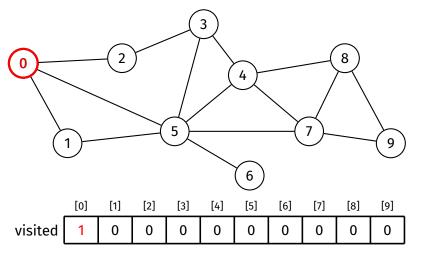
lueas/issue

Appendix BFS Example

DEC Evample

Path-Checking Example





path(0, 7)?

# Path-Checking with Recursive DFS

Example

Graph Traversal

BFS DFS

Ideas/Issues

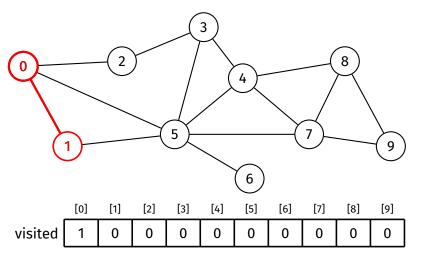
10003/13300

Appendix BFS Example

BES Example

Path-Checking Example

### 1 has not been visited



path(0, 7)?

# Path-Checking with Recursive DFS

Example

Graph Traversal

BFS DFS

Ideas/Issues

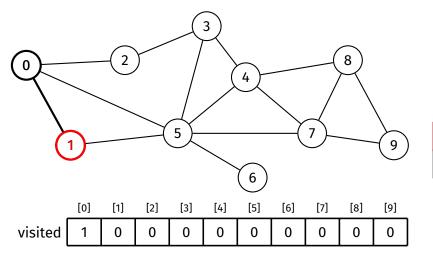
10005/15500

Appendix BFS Example

DEC E-----

Path-Checking Example

#### Recurse into 1



path(1, 7)? path(0, 7)? call stack

BFS DFS

Ideas/Issues

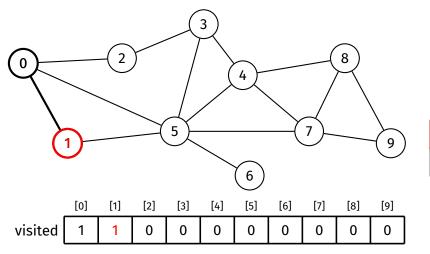
10005/15500

Appendix BFS Example

BFS Example

Path-Checking Example

### Mark 1 as visited



path(1, 7)? path(0, 7)? call stack

## Path-Checking with Recursive DFS

Example

Graph Traversal

BFS DFS

Ideas/Issues

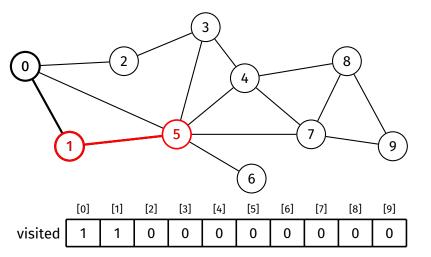
14645/15546

Appendix BFS Example

BFS Example

Path-Checking Example

### 5 has not been visited



path(1, 7)? path(0, 7)? call stack

BFS DFS

Ideas/Issues

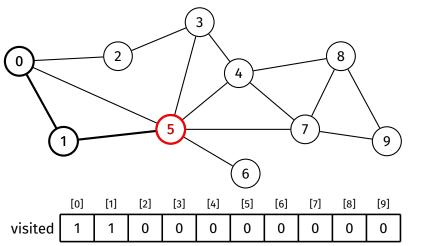
lueas/issue

Appendix BFS Example

DES Example

Path-Checking Example

### Recurse into 5





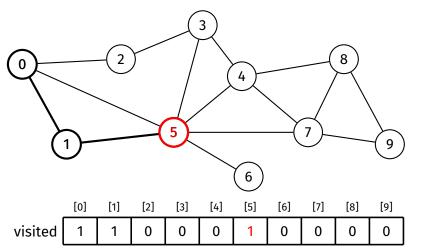
BFS DFS

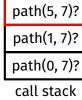
Ideas/Issues

**Appendix** BFS Example

Path-Checking Example

### Mark 5 as visited





# Path-Checking with Recursive DFS

Example

Graph Traversal

BFS DFS

Ideas/Issues

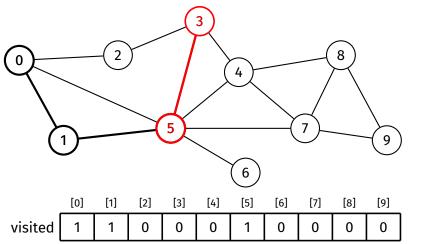
14645/15546

Appendix BFS Example

BFS Example

Path-Checking Example

#### 3 has not been visited





Traversal

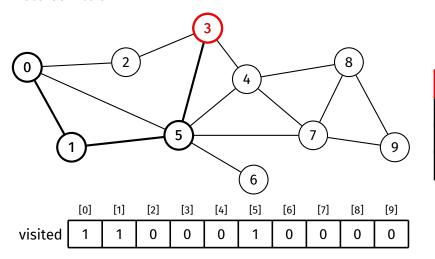
BFS DFS

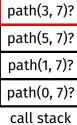
Ideas/Issues

**Appendix** BFS Example

Path-Checking Example

### Recurse into 3





### Path-Checking with Recursive DFS

Example

Graph Traversal

BFS DFS

Ideas/Issues

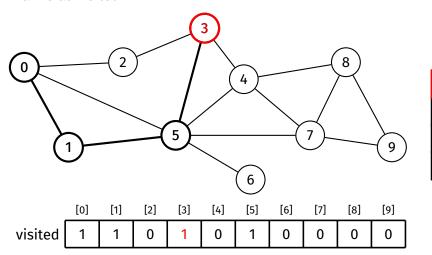
lueas/issue

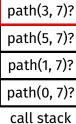
Appendix BFS Example

BES Example

Path-Checking Example

### Mark 3 as visited





BFS DFS

100

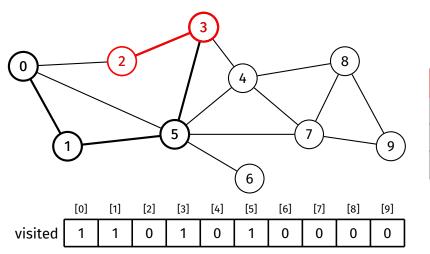
Ideas/Issues

Appendix BFS Example

DEC E-----

Path-Checking Example

### 2 has not been visited



path(3, 7)?

path(5, 7)?

path(1, 7)?

path(0, 7)?

call stack

## Path-Checking with Recursive DFS

Example

Graph Traversal

BFS DFS

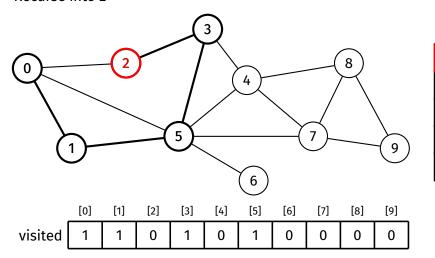
Ideas/Issues

Appendix BFS Example

DES Evample

Path-Checking Example

#### Recurse into 2



path(3, 7)?
path(5, 7)?
path(1, 7)?
path(0, 7)?
call stack

path(2, 7)?

BFS DFS

Ideas/Issues

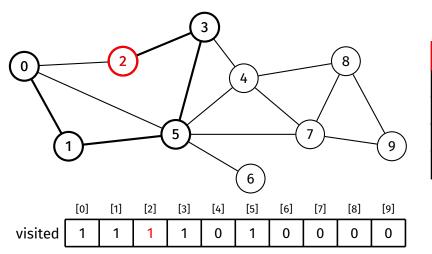
lueas/issue

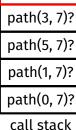
Appendix BFS Example

DES Evample

Path-Checking Example

#### Mark 2 as visited





path(2, 7)?

BFS DFS

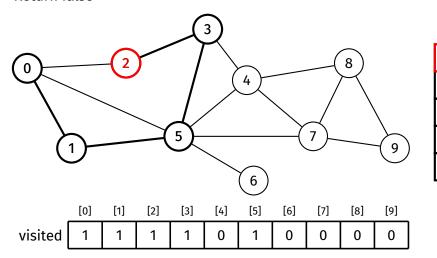
Ideas/Issues

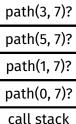
Appendix BFS Example

DES Example

Path-Checking Example

### Return false





path(2, 7)?

Example

Graph Traversal

BFS DFS

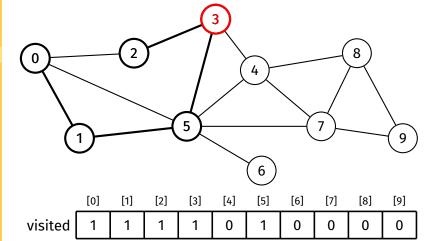
Ideas/Issues

lueas/issue

Appendix BFS Example

BFS Example

Path-Checking Example



path(3, 7)?

path(5, 7)?

path(1, 7)?

path(0, 7)?

call stack

BFS DFS

100

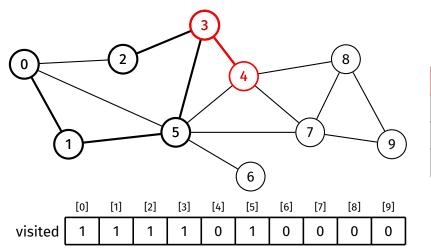
Ideas/Issues

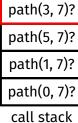
Appendix BFS Example

DES Evample

Path-Checking Example

#### 4 has not been visited





Example

Graph Traversal

BFS DFS

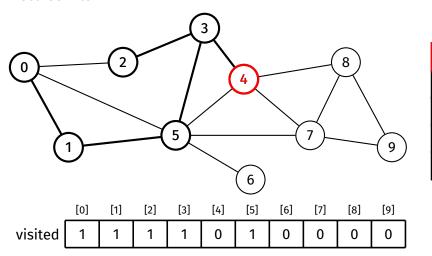
Ideas/Issues

Appendix BFS Example

DES Evample

Path-Checking Example

#### Recurse into 4



path(3, 7)?
path(5, 7)?
path(1, 7)?
path(0, 7)?
call stack

path(4, 7)?

BFS DFS

Ideas/Issues

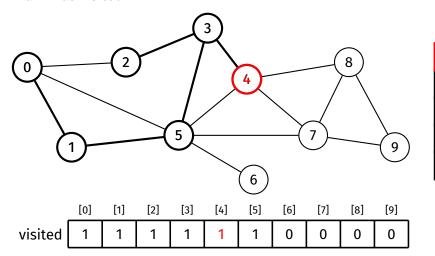
lueas/issue

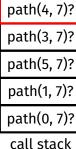
Appendix BFS Example

DEC Evample

Path-Checking Example

### Mark 4 as visited





Example

Graph Traversal

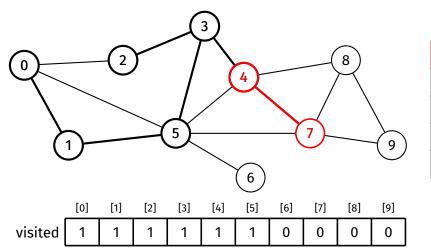
BFS DFS

Ideas/Issues

**Appendix** BFS Example

Path-Checking Example

### 7 has not been visited



path(4, 7)?
path(3, 7)?
path(5, 7)?
path(1, 7)?
path(0, 7)?
call stack

Example

Graph Traversal

BFS DFS

Ideas/Issues

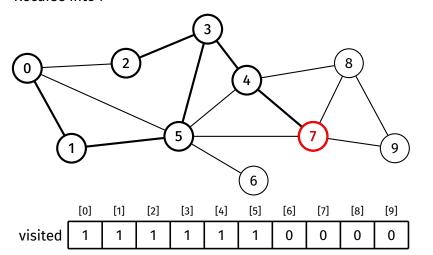
lueas/issue

Appendix BFS Example

DFS Example

Path-Checking Example

### Recurse into 7



path(4, 7)?
path(3, 7)?
path(5, 7)?
path(1, 7)?
path(0, 7)?
call stack

path(7, 7)?

BFS DFS

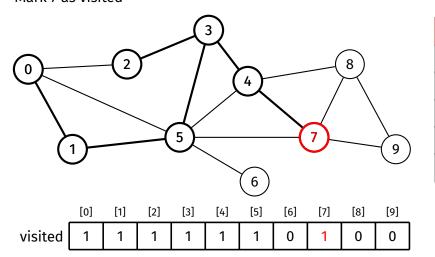
Ideas/Issues

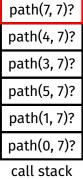
Appendix

BFS Example

Path-Checking Example

#### Mark 7 as visited





Example

Graph Traversal

BFS DFS

Ideas/Issues

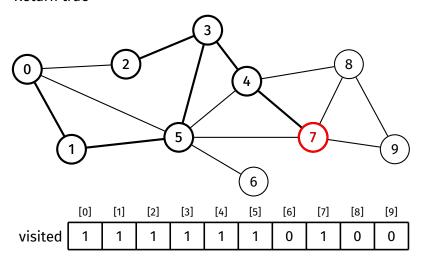
lueas/issue

Appendix BFS Example

BES Example

Path-Checking Example

#### Return true



path(4, 7)?
path(3, 7)?
path(5, 7)?
path(1, 7)?
path(0, 7)?
call stack

path(7, 7)?

BFS DFS

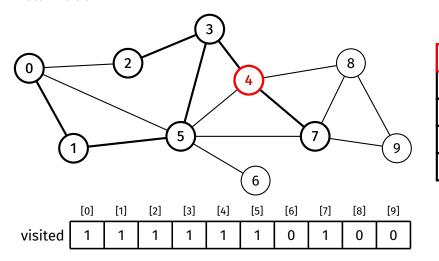
Ideas/Issues

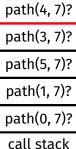
Appendix BFS Example

BES Example

Path-Checking Example

#### Return true





BFS DFS

100

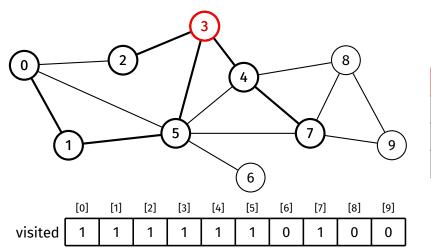
Ideas/Issues

Appendix BFS Example

DEC Evernel

Path-Checking Example

#### Return true



path(3, 7)?
path(5, 7)?
path(1, 7)?
path(0, 7)?
call stack

BFS DFS

Ideas/Issues

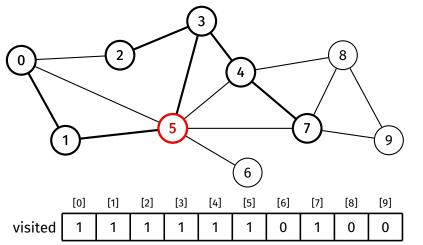
lueas/issue

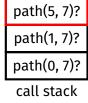
Appendix

BFS Example

Path-Checking Example

### Return true





BFS DFS

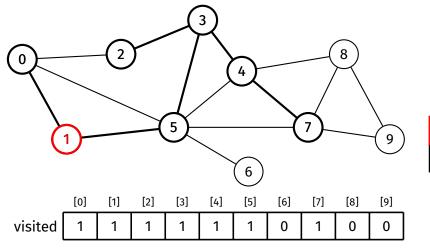
Ideas/Issues

Appendix BFS Example

DEC Evernel

Path-Checking Example

#### Return true



path(1, 7)? path(0, 7)? call stack

Example

Graph Traversal

BFS DFS

Ideas/Issues

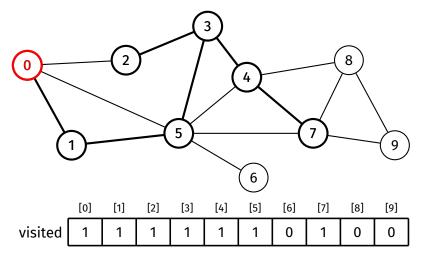
lueas/issue

Appendix BFS Example

DEC Evample

Path-Checking Example

### Return true



path(0, 7)?

call stack

Example

Graph Traversal

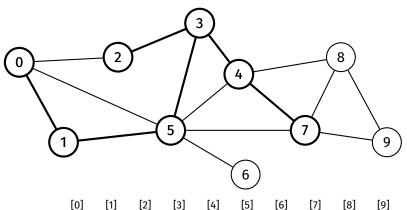
BFS DFS

Ideas/Issues

Answer: Yes

**Appendix** BFS Example

Path-Checking Example



[9]

[0] [1] [2] [3] [4] [5] [6] [7] [8] visited 0

call stack