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# COMP2521 24T1 Analysis of Algorithms

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### Motivation

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• Program efficiency is critical for many applications:

• Finance, robotics, games, database systems, ...

- We may want to compare programs to decide which one to use
- We may want to determine whether a program will be "fast enough"

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### What determines how fast a program runs?

- The operating system?
- Compilers?
- Hardware?
  - E.g., CPU, GPU, cache
- Load on the machine?
- Most important: the data structures and algorithms used

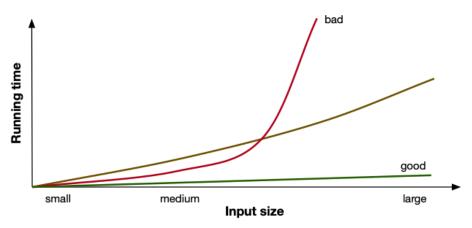
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- The running time of an algorithm tends to be a function of input size
- Typically: larger input  $\Rightarrow$  longer running time
  - Small inputs: fast running time , regardless of algorithm
  - Larger inputs: slower, but how much slower?



Algorithm Efficiency

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### • Best-case performance

- Not very useful
- Usually only occurs for specific types of input
- Average-case performance
  - Difficult; need to know how the program is used
- Worst-case performance
  - Most important; determines how long the program could possibly run

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Time complexity is

the amount of time it takes to run an algorithm, as a function of the input size

# **Time Complexity**

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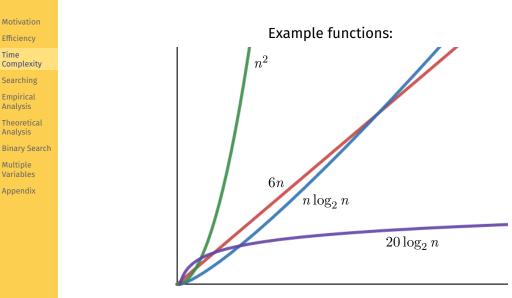
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The time complexity of an algorithm can be analysed in two ways:

- Empirically: Measuring the time that a program implementing the algorithm takes to run
- Theoretically: Counting the number of operations or "steps" performed by the algorithm as a function of input size

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Searching

The search problem:

Given an array of size *n* and a value, return the index containing the value if it exists, otherwise return -1.

[0]	[1]	[2]	[3]	[4]	[5]	[6]
2	16	11	1	9	4	15

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- 1 Write a program that implements the algorithm
- 2 Run the program with inputs of varying size and composition
- 3 Measure the running time of the algorithm
- 4 Plot the results

# **Timing Execution**

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We can measure the running time of an algorithm using *clock*(3).

• The *clock()* function determines the amount of processor time used since the start of the process.

#include <time.h>

```
clock_t start = clock();
// algorithm code here...
clock_t end = clock();
```

double seconds = (double)(end - start) / CLOCKS\_PER\_SEC;

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Absolute times will differ between machines, between languages ...so we're not interested in absolute time.

We are interested in the *relative* change as the input size increases

**Timing Execution** 

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### Let's empirically analyse the following search algorithm:

```
// Returns the index of the given value in the array if it exists,
// or -1 otherwise
int linearSearch(int arr[], int size, int val) {
    for (int i = 0; i < size; i++) {
        if (arr[i] == val) {
            return i;
        }
    }
    return -1;
}
```

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**Empirical Analysis** 

### Sample results:

Input Size	Running Time		
1,000,000	0.002		
10,000,000	0.023		
100,000,000	0.240		
200,000,000	0.471		
300,000,000	0.702		
400,000,000	0.942		
500,000,000	1.196		
1,000,000,000	2.384		

The worst-case running time of linear search grows linearly as the input size increases.

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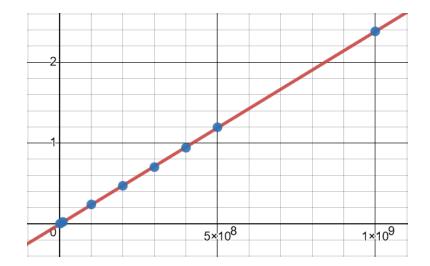
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# **Empirical Analysis**

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# Limitations of Empirical Analysis

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- Requires implementation of algorithm
- Different choice of input data  $\Rightarrow$  different results
  - Choosing good inputs is extremely important
- Timing results affected by runtime environment
  - E.g., load on the machine
- In order to compare two algorithms...
  - Need "comparable" implementation of each algorithm
  - Must use same inputs, same hardware, same O/S, same load

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- Uses high-level description of algorithm (pseudocode)
  - Can use the code if it is implemented already
- Characterises running time as a function of input size
- Allows us to evaluate the efficiency of the algorithm
  - Independent of the hardware/software environment

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- Pseudocode is a plain language description of the steps in an algorithm
- Uses structural conventions of a regular programming language
  - if statements, loops
- Omits language-specific details
  - variable declarations
  - allocating/freeing memory

## Pseudocode

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### Pseudocode for linear search:

```
linearSearch(A, val):
    Input: array A of size n, value val
    Output: index of val in A if it exists
        -1 otherwise
```

```
for i from 0 up to n-1:
if A[i] = val:
return i
```

return -1

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# **Primitive Operations**

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## Every algorithm uses a core set of basic operations.

### Examples:

- Assignment
- Indexing into an array
- Calling/returning from a function
- Evaluating an expression
- Increment/decrement

### We call these operations **primitive** operations.

Assume that primitive operations take the same constant amount of time.

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# Counting Primitive Operations

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### How many primitive operations are performed by this line of code?

for (int i = 0; i < n; i++)

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# Counting Primitive Operations

### How many primitive operations are performed by this line of code?

for (int i = 0; i < n; i++)

The assignment i = 0 occurs 1 time The comparison i < n occurs n + 1 times The increment i++ occurs n times

Total: 1 + (n + 1) + n primitive operations

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By inspecting the pseudocode, we can determine the maximum number of primitive operations executed by an algorithm as a function of the input size.

linearSearch(A, val):
 Input: array A of size n, value val
 Output: index of val in A if it exists
 -1 otherwise

```
for i from 0 up to n-1:

if A[i] = val:

return i
1 + (n + 1) + n
2n
```

return -1 1 4n + 3 (total)

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# **Counting Primitive Operations**

Linear search requires 4n + 3 primitive operations in the worst case.

If the time taken by a primitive operation is c, then the time taken by linear search in the worst case is c(4n + 3).

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### We are mainly interested in how the running time of an algorithm changes as the input size increases.

This is called the **asymptotic behaviour** of the running time.

# Asymptotic Analysis

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Asymptotic Analysis Lower-Order Terms

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### Asymptotic behaviour is not affected by lower-order terms.

- For example, suppose the running time of an algorithm is 4n + 100.
- As *n* increases, the lower-order term (i.e., 100) becomes less significant (i.e., becomes a smaller proportion of the running time)

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Asymptotic behaviour is not affected by constant factors.

Example: Suppose the running time T(n) of an algorithm is  $n^2$ .

• What happens when we double the input size?

$$T(2n) = (2n)^2$$
$$= 4n^2$$
$$= 4T(n)$$

When we double the input size, the time taken quadruples.

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Asymptotic Analysis Constant Factors

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Example: Now suppose the running time T(n) of an algorithm is  $10n^2$ .

• Now what happens when we double the input size?

$$T(2n) = 10 \times (2n)^2$$
$$= 10 \times 4n^2$$
$$= 4 \times 10n^2$$
$$= 4 T(n)$$

When we double the input size, the time taken also quadruples!

# Asymptotic Analysis

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### To summarise:

- Asymptotic behaviour is unaffected by lower-order terms
- Asymptotic behaviour is unaffected by constant factors

This means we can ignore lower-order terms and constant factors when characterising the asymptotic behaviour of an algorithm.

### Examples:

- If T(n) = 100n + 500, ignoring lower-order terms and constant factors gives n
- If  $T(n) = 5n^2 + 2n + 3$ , ignoring lower-order terms and constant factors gives  $n^2$

Asymptotic Analysis

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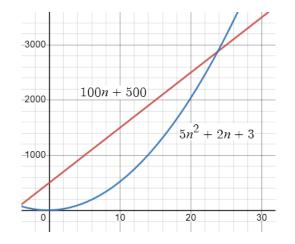
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### Big-Oh notation is used to classify the asymptotic behaviour of an algorithm,

and this is how we usually express time complexity in this course.

For example, linear search is O(n) in the worst case.

# **Big-Oh Notation**

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## Big-Oh notation allows us to easily compare the efficiency of algorithms

• For example, if algorithm A has a time complexity of O(n) and algorithm B has a time complexity of  $O(n^2)$ , then we can say that for sufficiently large inputs, algorithm A will perform better.

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# Formally, big-Oh is actually a notation used to describe the asymptotic relationship between functions.

### Formally:

Given functions f(n) and g(n), we say that f(n) is O(g(n)) if:

• There are positive constants *c* and *n*<sub>0</sub> such that:

•  $f(n) \leq c \cdot g(n)$  for all  $n \geq n_0$ 

### Informally:

Given functions f(n) and g(n), we say that f(n) is O(g(n)) if for sufficiently large n, f(n) is bounded above by some multiple of g(n).

# **Big-Oh Notation**



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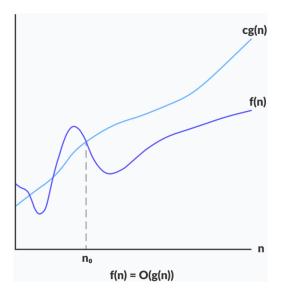
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f(n) is O(g(n))if f(n) is asymptotically less than or equal to g(n)

f(n) is  $\Omega(g(n))$ if f(n) is asymptotically greater than or equal to g(n)

> f(n) is  $\Theta(g(n))$ if f(n) is asymptotically equal to g(n)

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Multiple Variables Since time complexity is not affected by constant factors, instead of counting primitive operations, we can simply count line executions.

Worst-case time complexity: O(n)

Analysing Complexity

# **Analysing Complexity**

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To determine the worst-case time complexity of an algorithm:

- Determine the number of line executions performed in the worst case in terms of the input size
- Discard lower-order terms and constant factors
- The worst-case time complexity is then the big-Oh of the term that remains

# **Common Functions**

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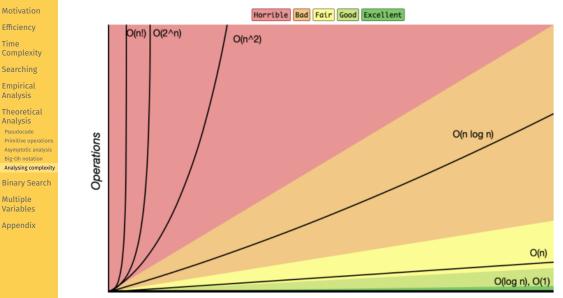
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## Commonly encountered functions in algorithm analysis:

- Constant: 1
- Logarithmic:  $\log n$
- Linear: *n*
- N-Log-N:  $n \log n$
- Quadratic:  $n^2$
- Cubic:  $n^3$
- Exponential:  $2^n$
- Factorial: *n*!

Time

## **Common Functions**



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**Back to Linear Search** 

Linear search requires 4n + 3 primitive operations in the worst case.

Therefore, linear search is O(n) in the worst case.

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# Searching in a Sorted Array

Is there a faster algorithm for searching an array?

Yes... if the array is sorted.

[0]	[1]	[2]	[3]	[4]	[5]	[6]
1	2	4	9	11	15	16

## Let's start in the middle.

- If a[N/2] = val, we found val; we're done!
- Otherwise, we split the array:

... if val < a[N/2], we search the left half (a[0] to a[(N/2) - 1)])... if val > a[N/2], we search the right half (a[(N/2) + 1)] to a[N - 1])

**Binary Search** 



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## Binary search is a more efficient search algorithm for sorted arrays:

```
int binarySearch(int arr[], int size, int val) {
    int lo = 0;
    int hi = size - 1;
    while (lo <= hi) {</pre>
        int mid = (lo + hi) / 2;
        if (val < arr[mid]) {</pre>
            hi = mid - 1;
        } else if (val > arr[mid]) {
            lo = mid + 1;
        } else {
             return mid;
        }
    }
    return -1;
}
```

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Binary Search Example

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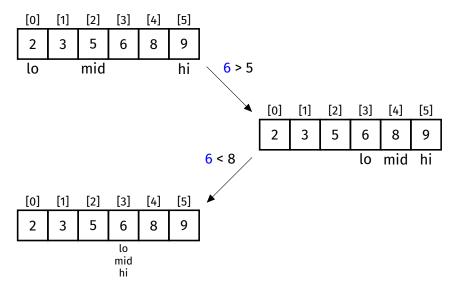
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## Successful search for 6:



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Unsuccessful search for 7: [0] [1] [2] [3] [4] [5] 3 5 2 6 8 9 7 > 5 mid lo hi [0] [1] [2] [3] [4] [5] 2 3 5 6 8 9 7 < 8 mid hi lo [0] [1] [2] [3] [4] [5] 3 5 6 8 9 2 7 > 6 lo mid hi [0] [1] [2] [3] [4] [5] 2 3 5 6 8 9 hi lo ▲□▶ ▲□▶ ▲三▶ ▲三▶ - 三 - のへで

Binary Search Example

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## How many iterations of the loop?

- Best case: 1 iteration
  - Item is found right away
- Worst case:  $\log_2 n$  iterations
  - Item does not exist
  - Every iteration, the size of the subarray being searched is halved

**Binary Search** 

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Analysis

## Thus, binary search is $O(\log_2 n)$ or simply $O(\log n)$

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Binary Search O(log n)

$$O(\log_2 n) = O(\log n)$$

Why drop the base?

According to the change of base formula:

$$\log_a n = \frac{\log_b n}{\log_b a}$$

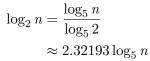
If *a* and *b* are constants,  $\log_a n$  and  $\log_b n$  differ by a constant factor

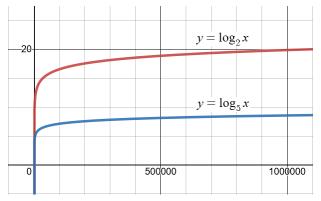
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# Binary Search $O(\log n)$









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What if an algorithm takes multiple arrays as input?

If there is no constraint on the relative sizes of the arrays, their sizes would be given as two variables, usually n and m

**Multiple Variables** 

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Example time complexities with two variables:

O(n+m)O(nm)

 $O(\max(n, m))$ 

 $O(\min(n,m))$ 

 $O(n\log m)$ 

 $O(n\log m + m\log n)$ 

# Multiple Variables

Example

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Problem:

Given two arrays, where each array contains no repeats, find the number of elements in common

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# **Multiple Variables**

Example

```
numCommonElements(A, B):
    Input: array A of size n
        array B of size m
    Output: number of elements in common
```

```
numCommon = 0

for i from 0 up to n-1:

for j from 0 up to m-1:

if A[i] = B[j]:

numCommon = numCommon + 1
```

return numCommon

Time complexity: O(nm)

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Searching

Empirical Analysis

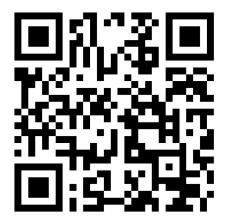
Theoretical Analysis

**Binary Search** 

Multiple Variables

Appendix

## https://forms.office.com/r/5c0fb4tvMb



Feedback

Motivation Efficiency

Time Complexity

Searching

Empirical Analysis

Theoretical Analysis

**Binary Search** 

Multiple Variables

Appendix Exercise

# Appendix

# **Predicting Time**

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#### COMP2521 24T1

- Motivation
- Efficiency
- Time Complexity
- Searching
- Empirical Analysis
- Theoretical Analysis
- **Binary Search**
- Multiple Variables
- Appendix Exercise

If I know my algorithm is quadratic (i.e.,  $O(n^2)$ ), and I know that for a dataset of 1000 items, it takes 1.2 seconds to run ...

- how long for 2000?
- how long for 10,000?
- how long for 100,000?
- how long for 1,000,000?

(answers on the next slide)

**Predicting Time** 

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#### COMP2521 24T1

- Motivation
- Efficiency
- Time Complexity
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- Binary Search
- Multiple Variables
- Appendix Exercise

- If I know my algorithm is quadratic (i.e.,  $O(n^2)$ ), and I know that for a dataset of 1000 items, it takes 1.2 seconds to run ...
  - how long for 2000? 4.8 seconds
  - how long for 10,000? 120 seconds (2 mins)
  - how long for 100,000? 12000 seconds (3.3 hours)
  - how long for 1,000,000? 1200000 seconds (13.9 days)